

Velocity Space Studies of Fast-ion Transport During a Sawtooth Crash

by C.M. Muscatello^a

Adviser: W.W. Heidbrink^a

Co-authors: Ya.I. Kolesnichenko^b, V.V. Lutsenko^b,
M.A. Van Zeeland^c, Yu.V. Yakovenko^b

Special thanks to the entire DIII-D team

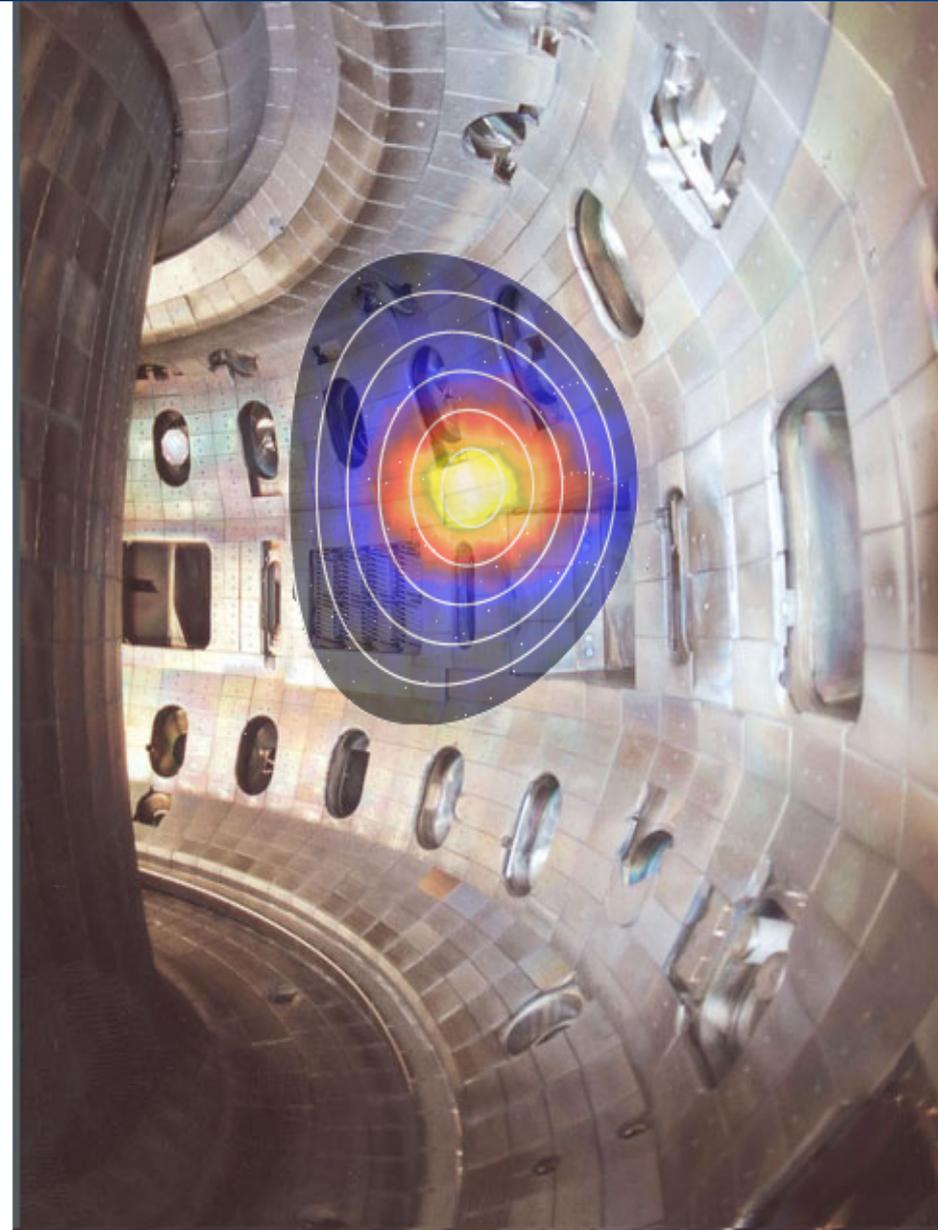
^{a)}University of California, Irvine, CA USA

^{b)}Institute for Nuclear Research, Kyiv, Ukraine

^{c)}General Atomics, San Diego, CA, USA

at the Transport Task Force Workshop
San Diego, CA

April 8th 2011



Sawtooth-Induced Fast-ion Transport is Not News

1987-1995

(general investigations on superthermal ion populations)

JET – beam D, ICRF heated minority ions, fusion products of D-D reactions

DIII-D – beam D

TFTR – fusion-produced T

1995-2010

(studies began dissecting fast-ion velocity space)

TFTR – trapped and passing D-T alphas

TEXTOR – pitch resolved beam H

DIII-D Introduces Capabilities to Resolve Fast-ion Velocity Space

- **Revisit sawteeth for validation of transport models and build confidence in basic understanding of energetic ion dynamics**
- **New fast-ion deuterium-alpha (FIDA) system added during 2009-2010 campaign to complement previous systems**
 - The systems weight velocity-space differently providing reasonable discernment of different fast-ion populations

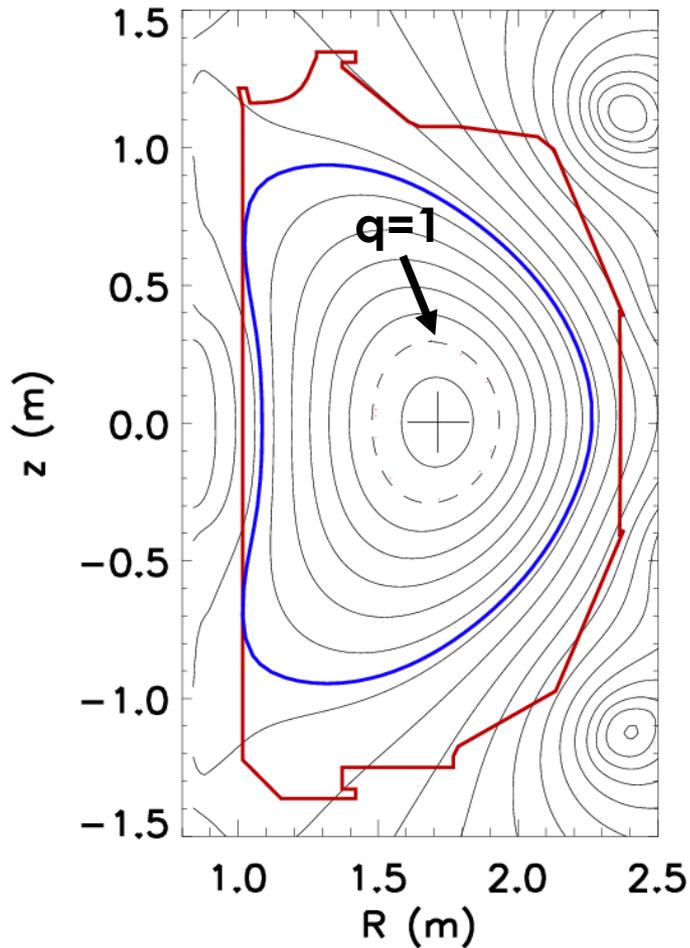
Outline

- Experimental setup and results: measured velocity-space dependence of fast-ion transport at a sawtooth crash
- Theory: drift-kinetic simulation of sawtooth-induced fast-ion transport and analytic treatment of particle drifts
- Summary

Outline

- **Experimental setup and results: measured velocity-space dependence of fast-ion transport at a sawtooth crash**
- Theory: drift-kinetic simulation of sawtooth-induced fast-ion transport and analytic treatment of particle drifts
- Summary

Low- n_e L-mode Discharge With Uniform Sawteeth



#141182:

$B_t = 1.9$ T

$I_p = 1.3$ MA

$\beta = 0.003$

$q_{95} = 4.0$

$\langle T_e(0)^{\text{precrash}} \rangle = 3.7$ keV

$\langle n_e(0)^{\text{precrash}} \rangle = 3.4\% \cdot 10^{19} \text{m}^{-3}$

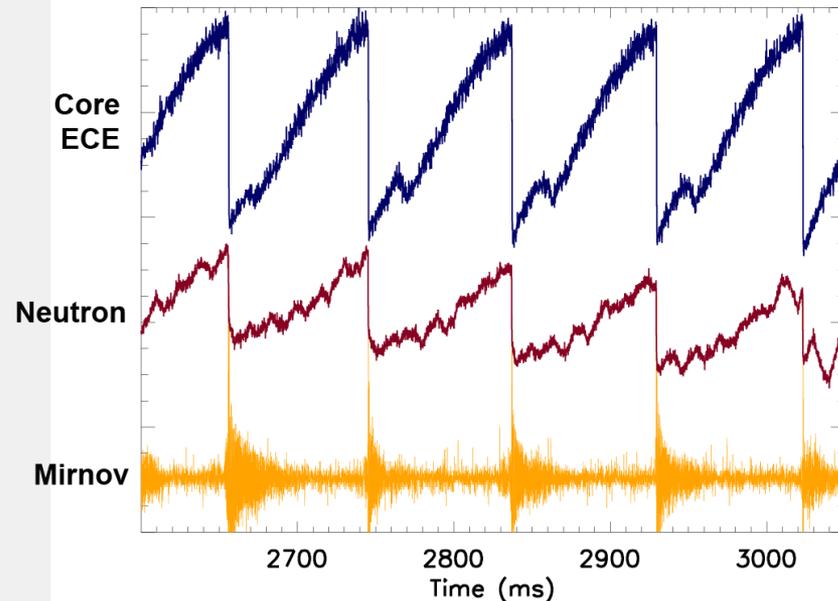
$\langle P_{\text{inj}} \rangle = 3.2$ MW

$\langle E_{\text{inj}} \rangle = 75$ keV

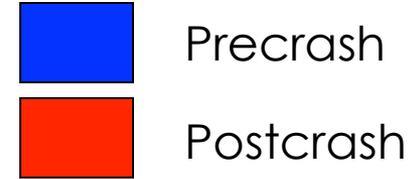
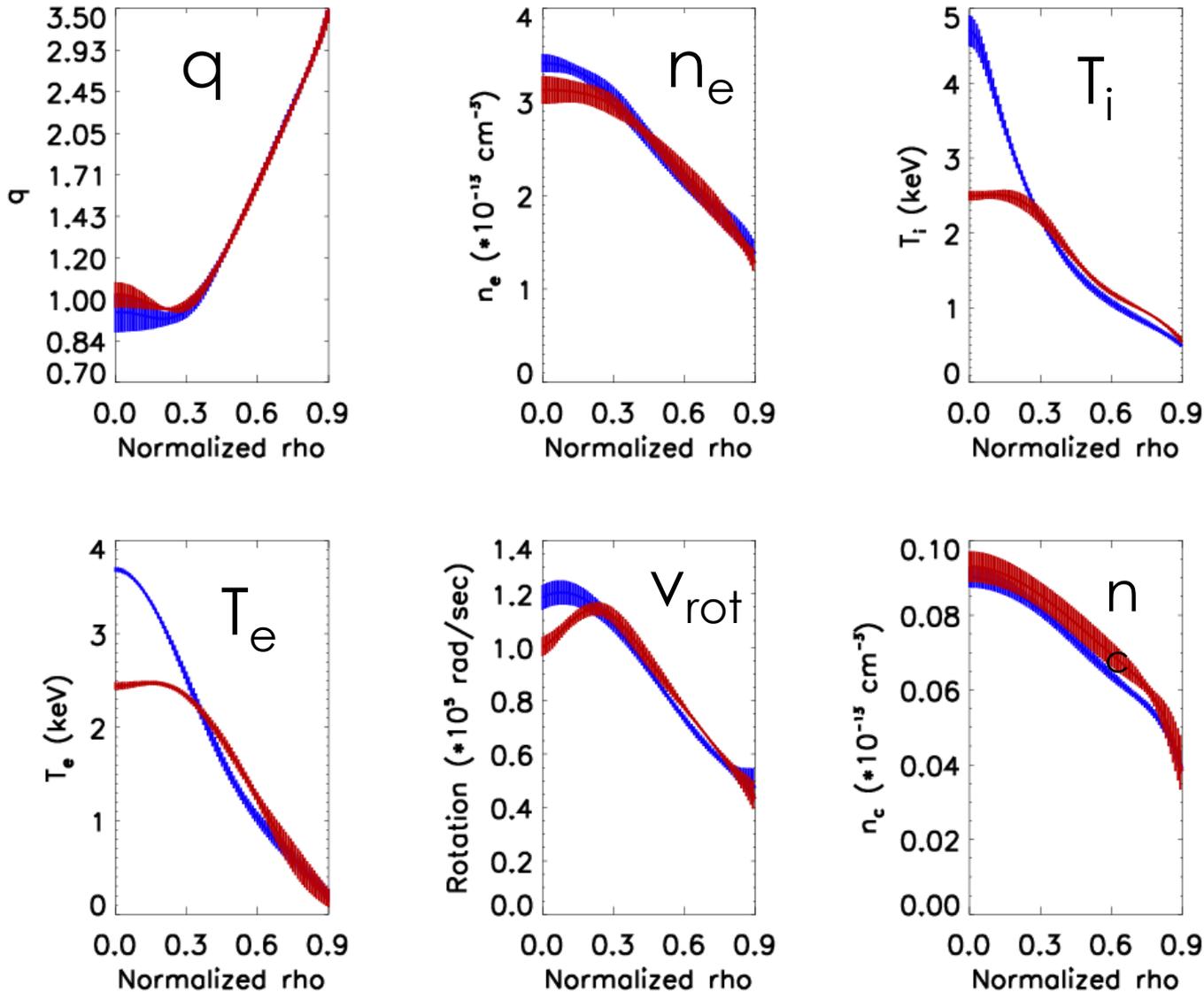
$\langle T_{\text{sawtooth}} \rangle = 85$ ms

$\langle \Delta n/n \rangle = -0.15$

- NBI is the only auxiliary heating source
- No other MHD activity detected (such as tearing modes, fishbones, AEs)
- n_e , I_p , B_t held constant to generate repeatable sawteeth



Clear Change in Many Plasma Profiles During a Crash



141182:

$$\langle \Delta n_e(0)/n_e(0) \rangle = -0.10$$

$$\langle \Delta T_i(0)/T_i(0) \rangle = -0.47$$

$$\langle \Delta T_e(0)/T_e(0) \rangle = -0.34$$

$$\langle \Delta v_r(0)/v_r(0) \rangle = -0.15$$

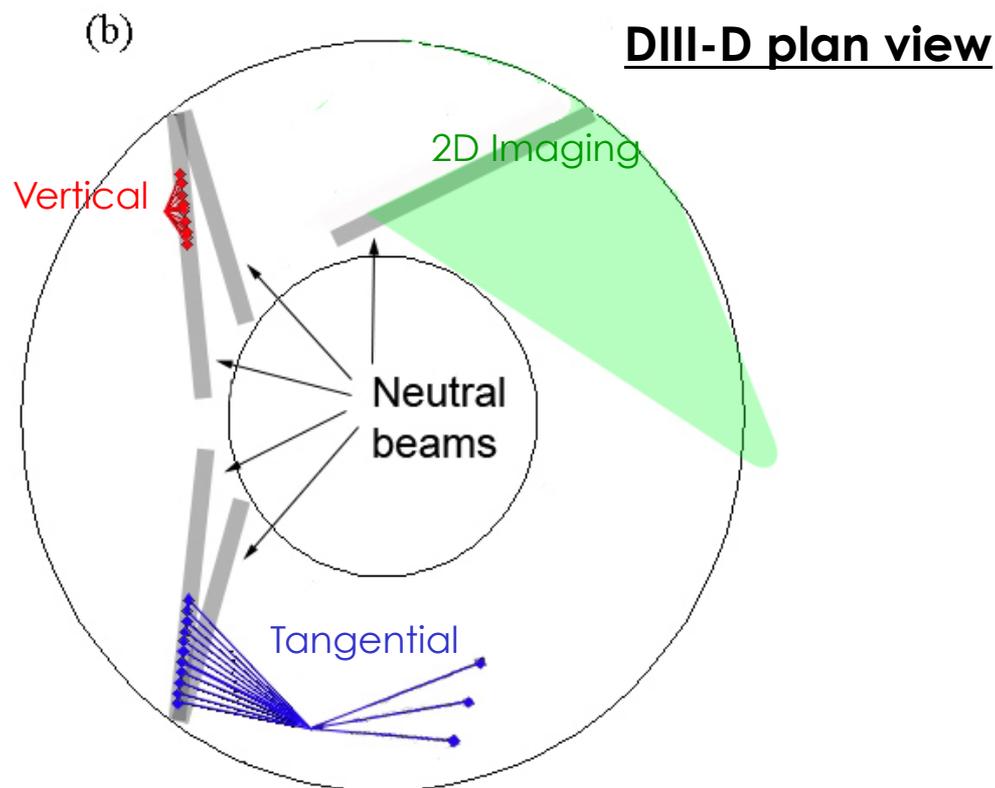
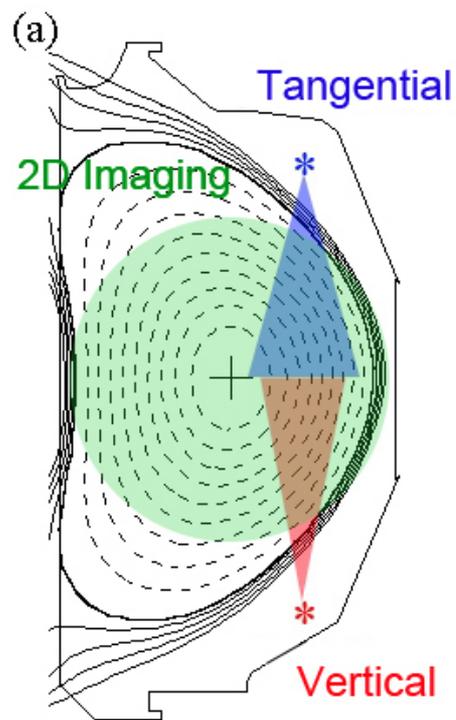
$$\langle \Delta n_c(0)/n_c(0) \rangle = 0.03$$

Employed FIDA Suite to Compare Different Parts of Velocity Space

Fast-ion deuterium-alpha (FIDA): spectroscopic-based diagnostic tool utilizing charge-exchange between injected D^0 and fast D^+ population to infer dynamics

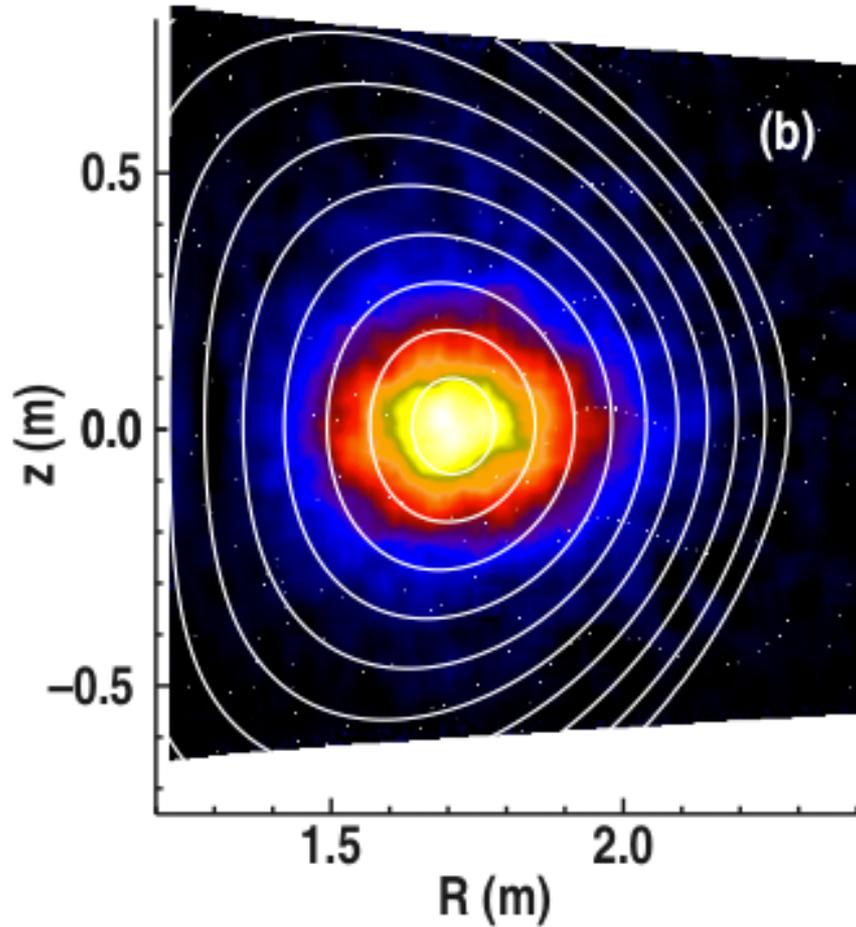
- Each geometry provides unique instrumental weighting in phase space

DIII-D poloidal plane

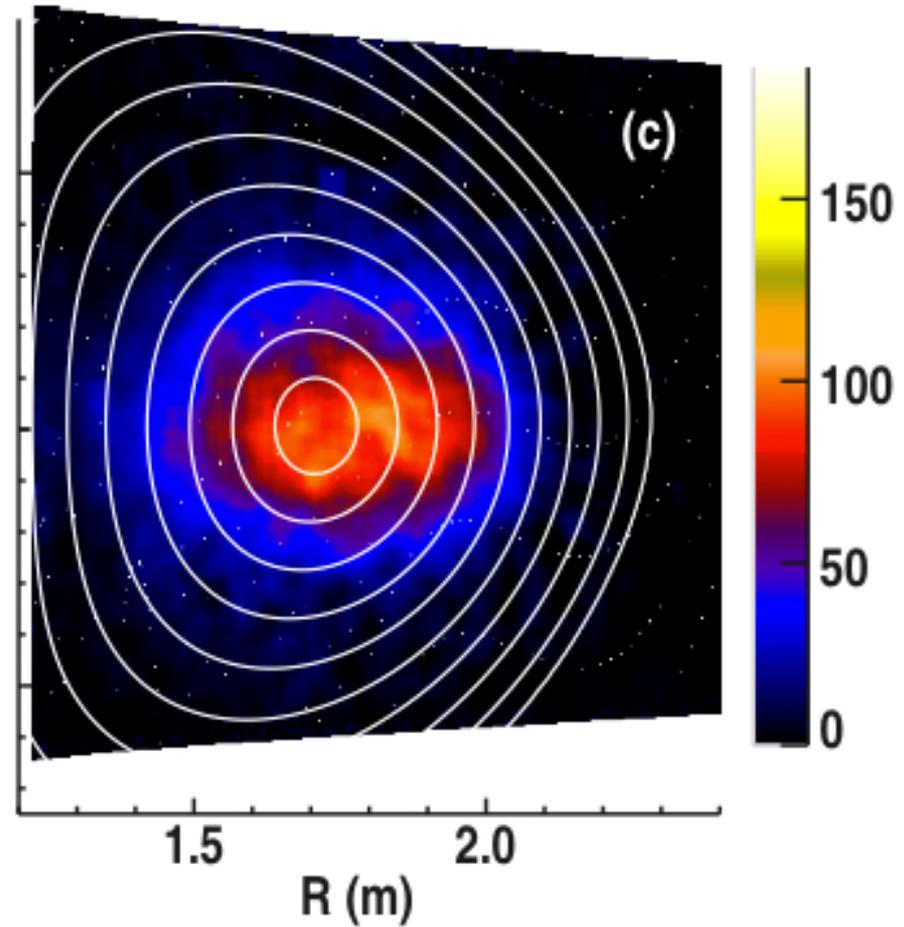


Fast-ion Profile Flattens at a Crash

FIDA Before ST

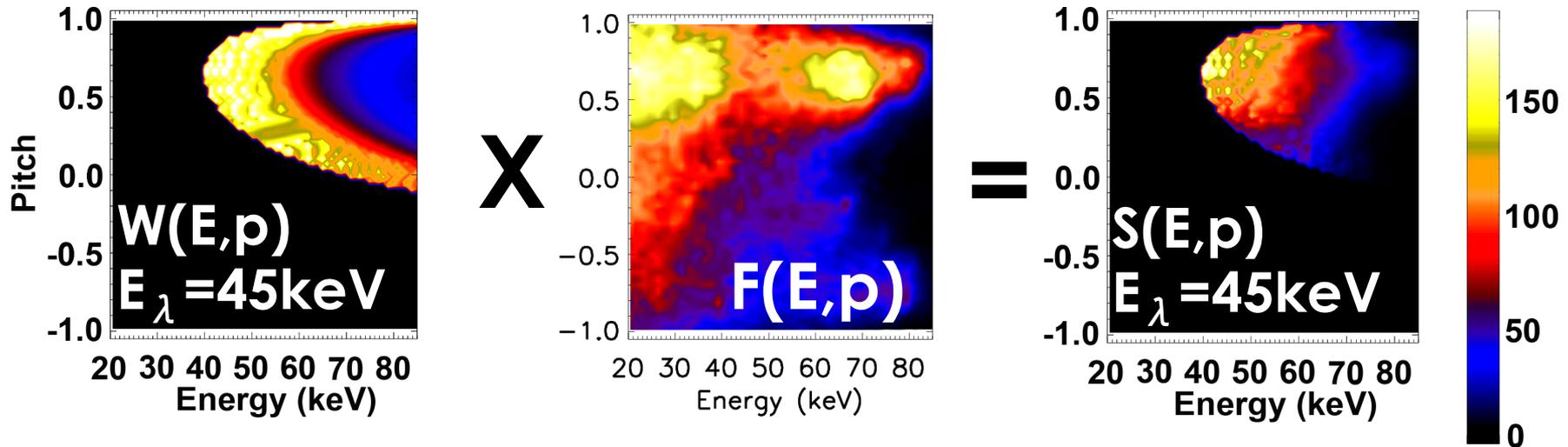


FIDA After ST

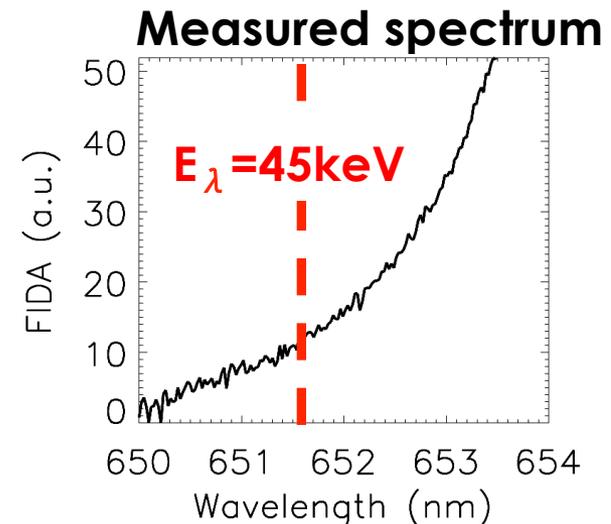


Interpreting FIDA Signal as a Velocity-space Weight Function

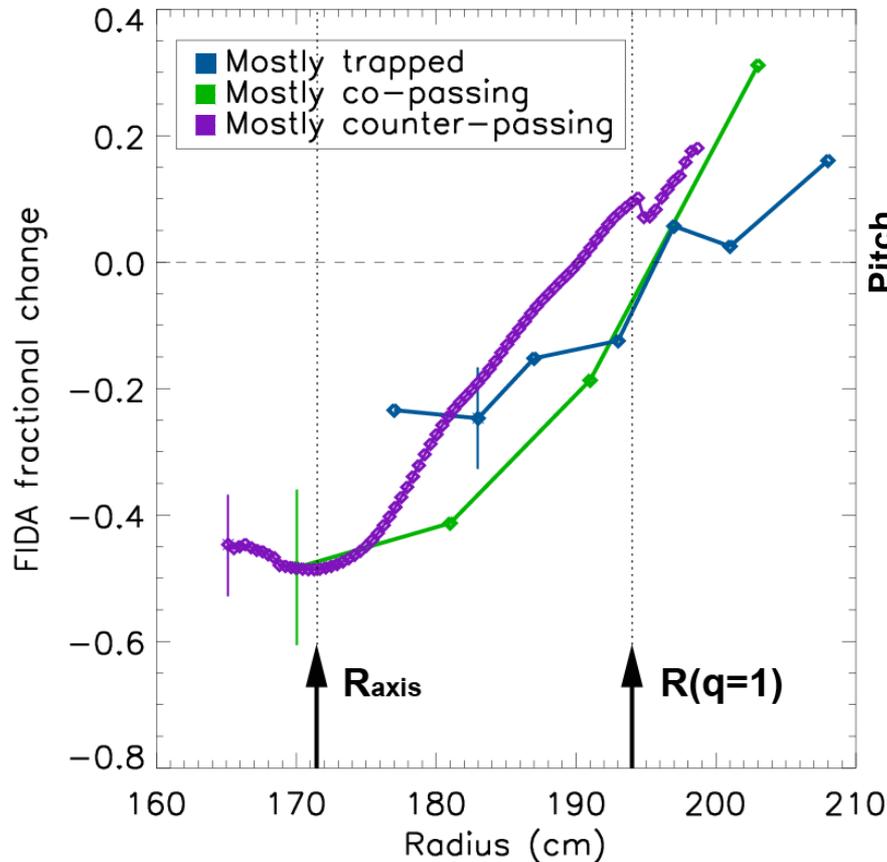
$$\text{Signal} \propto \iint W(E,p) * F(E,p) dE dp$$



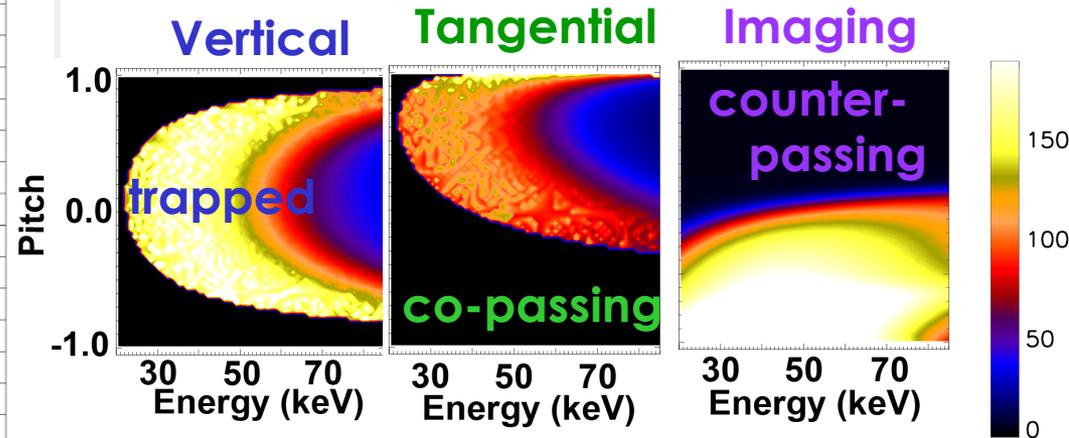
E_λ : fast-ion energy component measured along line-of-sight



Passing Ions Experience Greatest Redistribution



Instrument weights



$$\text{pitch} \equiv V_{||} / V$$

$$\text{fractional change} \equiv \frac{\langle \text{postcrash} \rangle - \langle \text{precrash} \rangle}{\langle \text{precrash} \rangle}$$

- ~ 50% reduction in the core co- & counter-**passing** fast-ion signal

- ~25% reduction in the central-most **trapped** fast-ion signal

Stronger Passing-ion Transport is a *General* Trend Under Many Conditions

- Database of 30+ shots
- Various plasma shapes and conditions
- Fractional change database of FIDA signals for mostly trapped ions and co-passing ions

Parameter regimes

$B_t = 1.86\text{-}2.05\text{ T}$

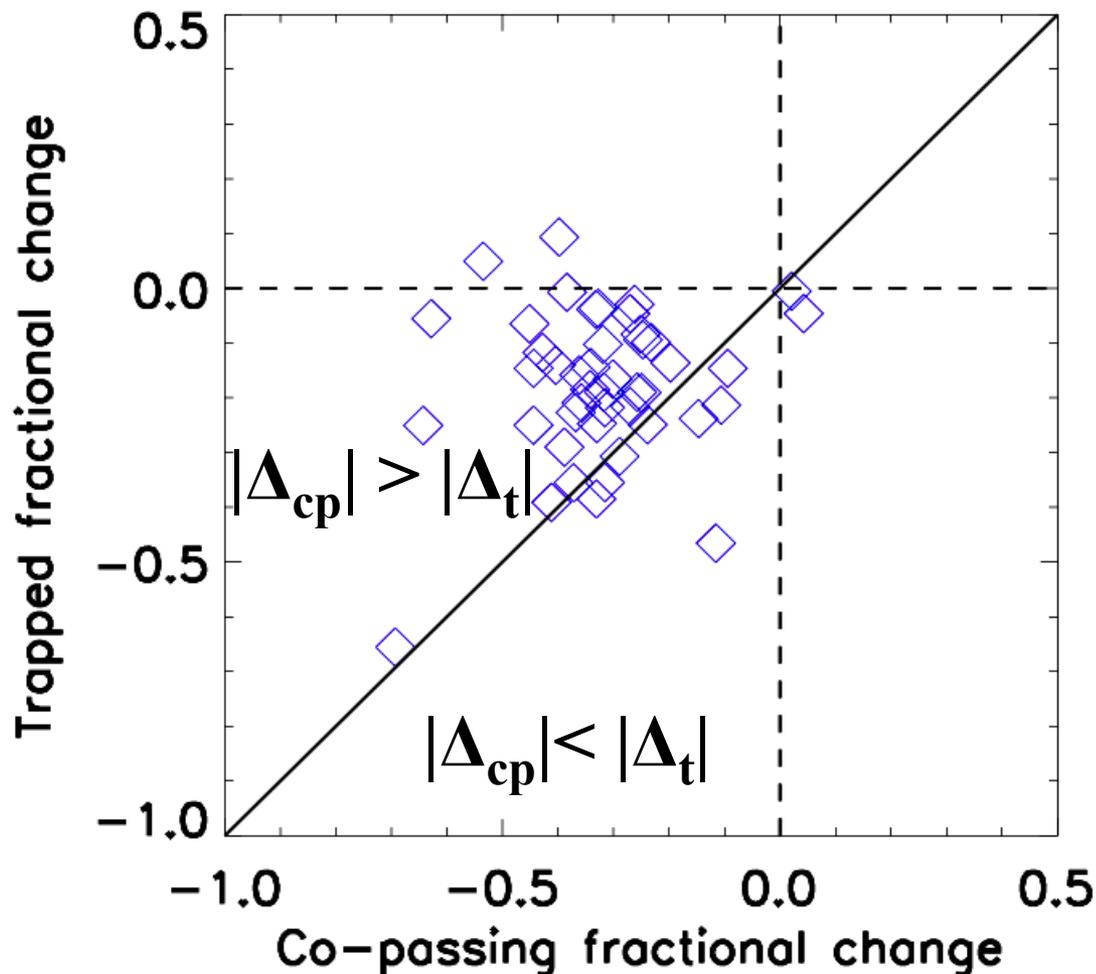
$I_p = 1.16\text{-}1.34\text{ MA}$

$\langle \Delta T_e(0)/T_e(0) \rangle = 0.21\text{-}0.37$

$\langle T_e(0)^{\text{precrash}} \rangle = 2 - 5\text{ keV}$

$\langle n_e(0)^{\text{precrash}} \rangle = 2 - 4\%_{00} 10^{19}\text{m}^{-3}$

$\langle T_{\text{sawtooth}} \rangle = 48\text{-}108\text{ ms}$



Outline

- The DIII-D FIDA suite incorporates 3 systems which weight velocity-space differently. Experiments indicate that passing fast ions experience stronger sawtooth-induced transport than trapped ions
- **Theory: drift-kinetic simulation of sawtooth-induced fast-ion transport and analytic treatment of particle drifts**
- Summary

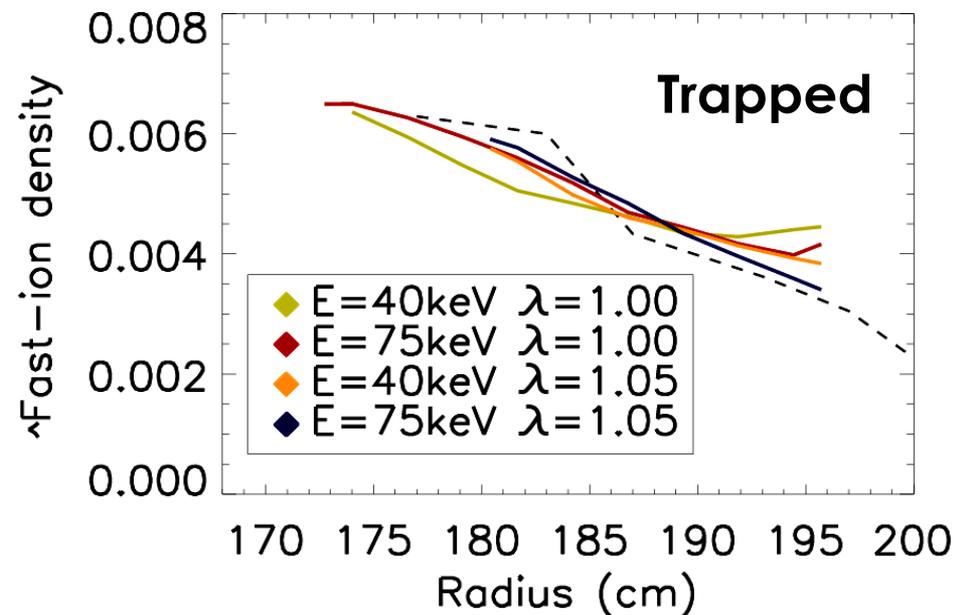
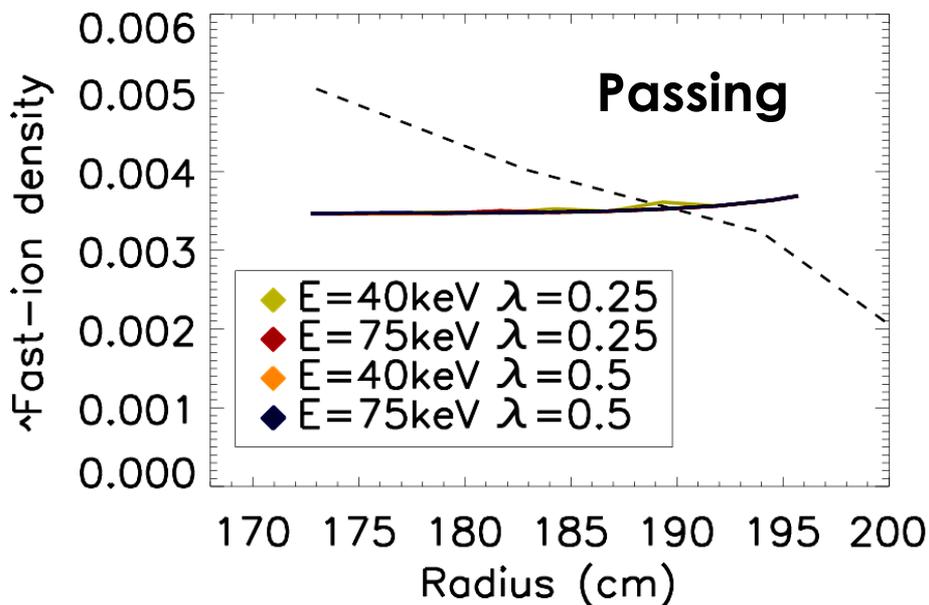
Numerical Simulation Solves Bounce/Transit-averaged Drift-kinetic Equation

- OFSEF[1] code employs Kadomtsev sawtooth crash model to evolve the fields and solves the following kinetic equation

$$\partial f / \partial t = (-\mathbf{v}_{||}^0 - \mathbf{v}_D - \mathbf{v}_{||}^1 - \mathbf{v}_E) \cdot \partial f / \partial \mathbf{x} - e(\mathbf{v} \cdot \mathbf{E}(\mathbf{x}, t)) \partial f / \partial \mathcal{E}$$

f – fast-ion distribution function
 $\mathbf{v}_{||}^0$ – velocity along unperturbed flux surfaces
 \mathbf{v}_D – toroidal drift velocity
 $\mathbf{v}_{||}^1$ – velocity along perturbed flux surfaces
 $\mathbf{v}_E = \mathbf{E} \times \mathbf{B}$ drift due to evolving perturbation
 \mathcal{E} – fast-ion energy

General Feature of the Simulation Shows that Passing Ions are More Readily Redistributed than Trapped Ions



$$\lambda \equiv \mu B_0 / E$$

- Passing particle transport is insensitive to different energies and pitches

- Trapped particle transport depends on energy and pitch
- Smaller values of E and smaller values of λ produce flattest postcrash profiles

Fast-ion Transport at a Crash is Driven by $\mathbf{E} \times \mathbf{B}$ Drift

- Underlying perturbation $\delta \mathbf{B}$ takes on helical $n=m=1$ mode structure
- Assuming ideal conditions (except for thin layer) electric field ($\mathbf{E} = -\mathbf{u} \times \mathbf{B}$) generated by bulk plasma motion (\mathbf{u})
- Cross-field transport during crash driven by $\mathbf{E} \times \mathbf{B}$ drift and fast ions frozen to flux surfaces move with them
- However, some types of orbits are more prone to flux attachment than others....

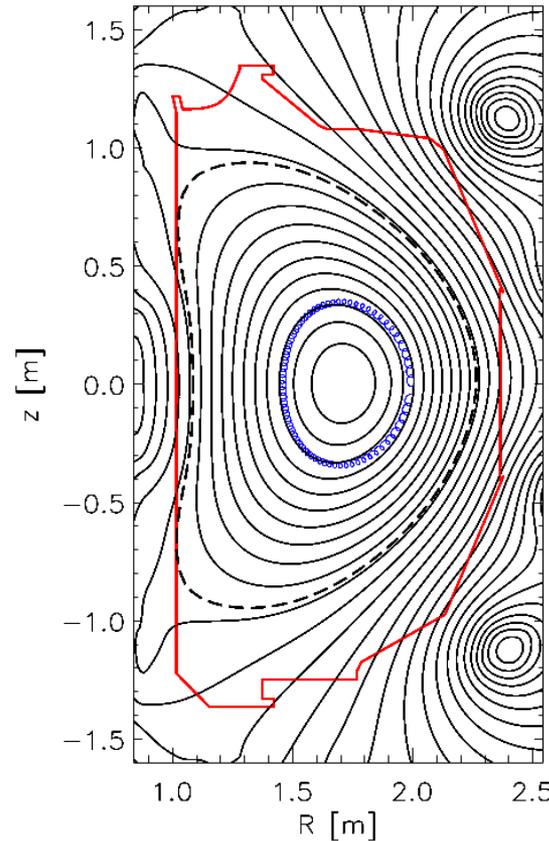
Potential for Transport of *Passing* Ions Depends on Parallel and Drift Motions

τ_{Ψ} – **longitudinal time** –
transit-averaged period
along a *perturbed* flux
surface

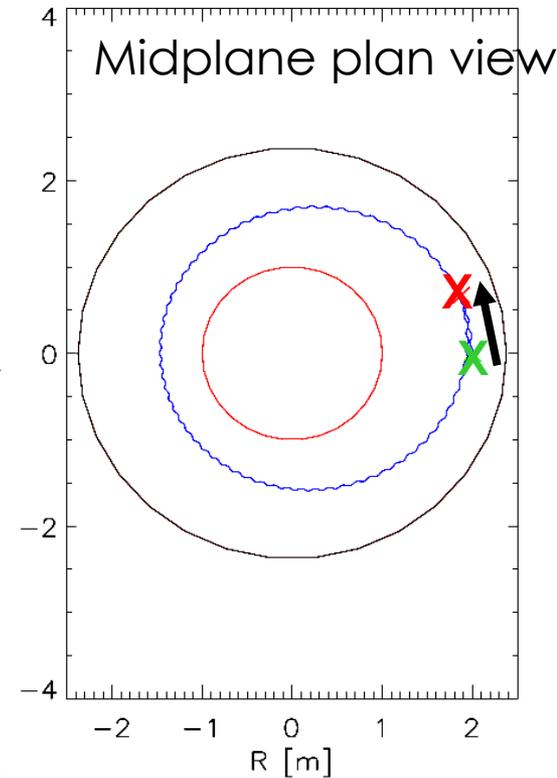
τ_{pr} – **toroidal precession
time** – *transit-averaged*
toroidal period

Strong transport:

$$\tau_{\Psi} \ll \tau_{pr}$$



Above: 1
poloidal transit



Above: toroidal
distance
traveled in 1
poloidal period

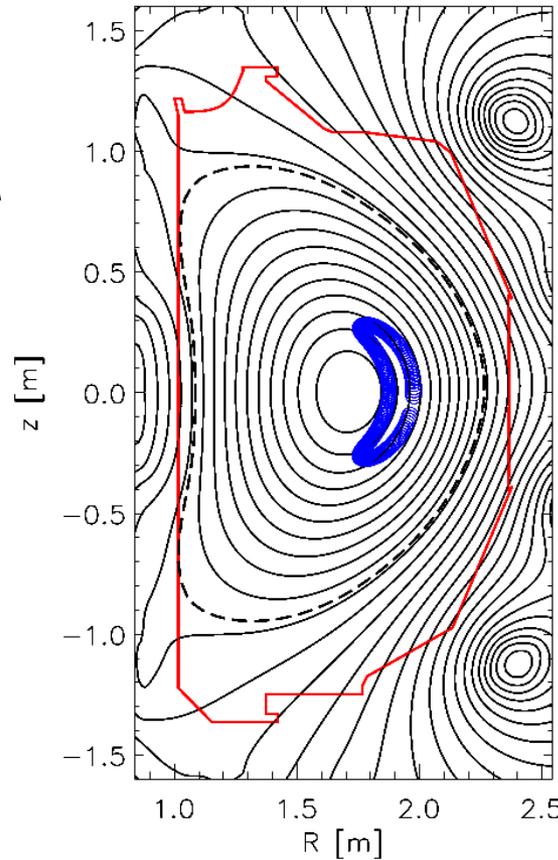
Potential for Transport of *Trapped* Ions Depends on Crash Time and Drift Motions

τ_{cr} – **crash time** –
presumably synonymous
with the reconnection time

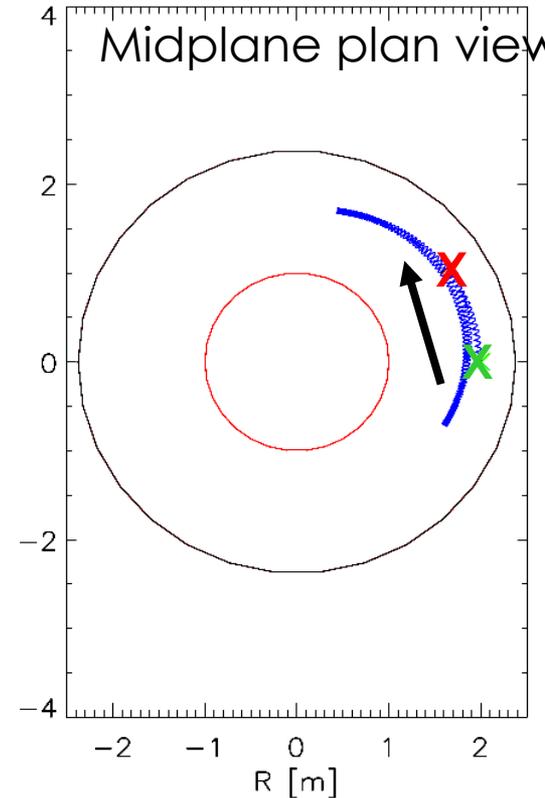
τ_{pr} – **toroidal precession
time** – *bounce-averaged*
toroidal period

Strong transport:

$$\tau_{cr} \ll \tau_{pr}$$



Above: 1
poloidal bounce



Above: toroidal
distance
traveled in 1
poloidal period

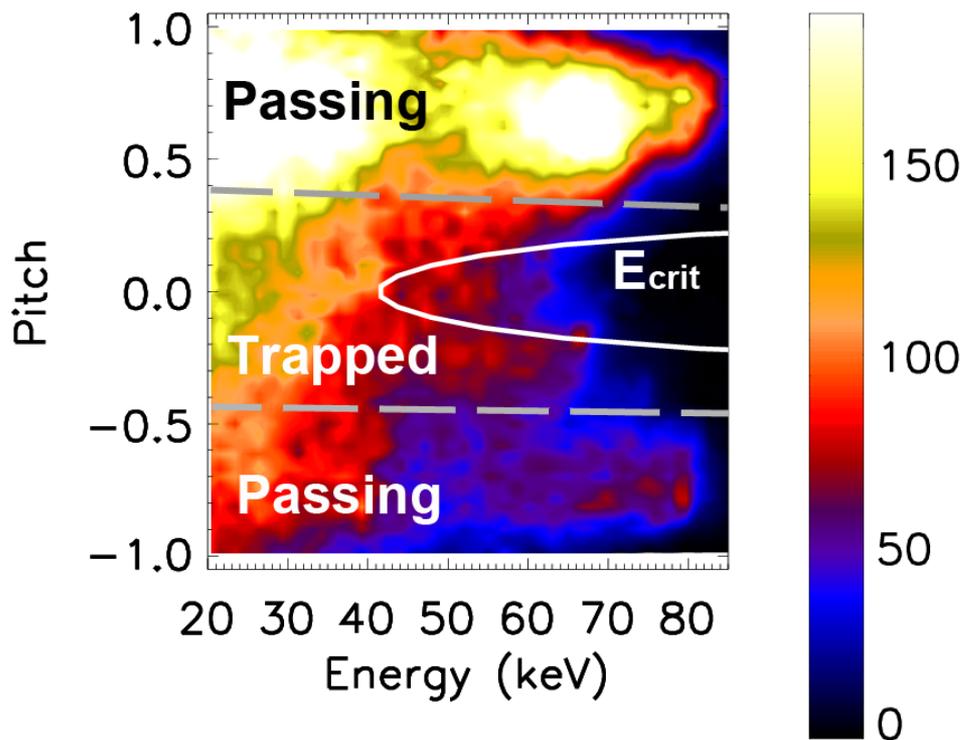
Timescale Comparison can be Recast in Terms of Energy and Pitch

Criteria for **strong** redistribution of fast-ions

- **Passing:** $\tau_{\Psi} \ll \tau_{pr} \rightarrow E \ll E(\chi)_{crit,passing}$
- **Trapped:** $\tau_{cr} \ll \tau_{pr} \rightarrow E \ll E(\chi)_{crit,trapped}$

Pitch:

$$\chi \equiv V_{\parallel} / V$$

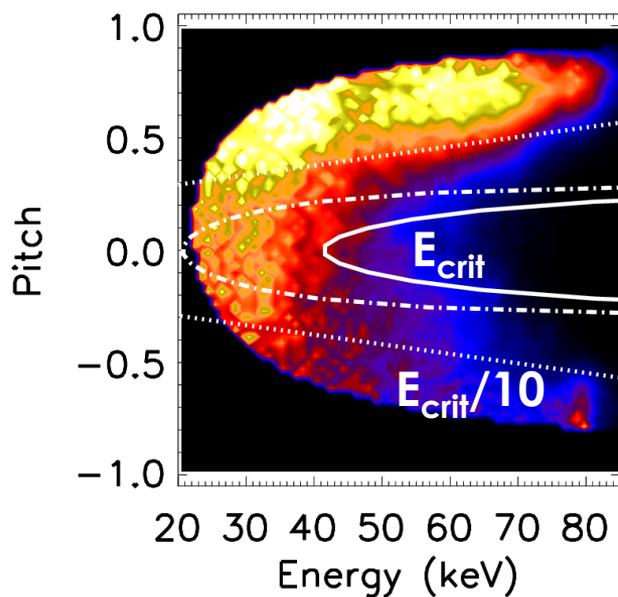


- Classical slowing-down fast-ion distribution function calculated by TRANSP
- Trapped/passing boundaries (dashed) calculated by g.c. orbit code (Van Zeeland)
- Analytic E_{crit} (solid) calculated for trapped and passing regions
 - $E_{crit}^{trapped} \approx 40 \text{ keV}$
 - $E_{crit}^{passing} \approx 200 \text{ keV}$

Different Transport Observed by FIDA Systems can be Explained by E_{crit}

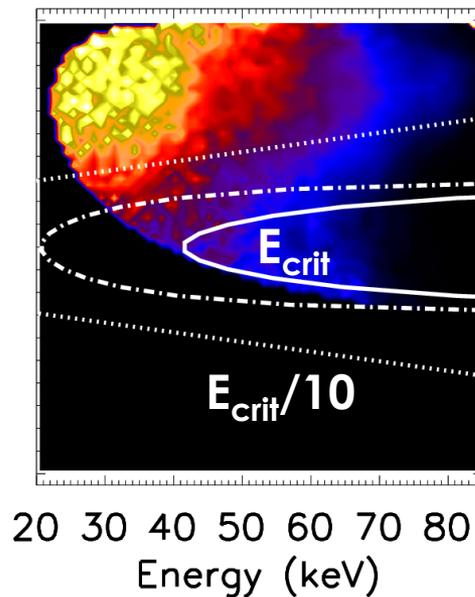
Mostly trapped

- Large fraction of detected particles do **not** satisfy $E \ll E_{crit} \approx 40$ keV
- Only moderate transport expected



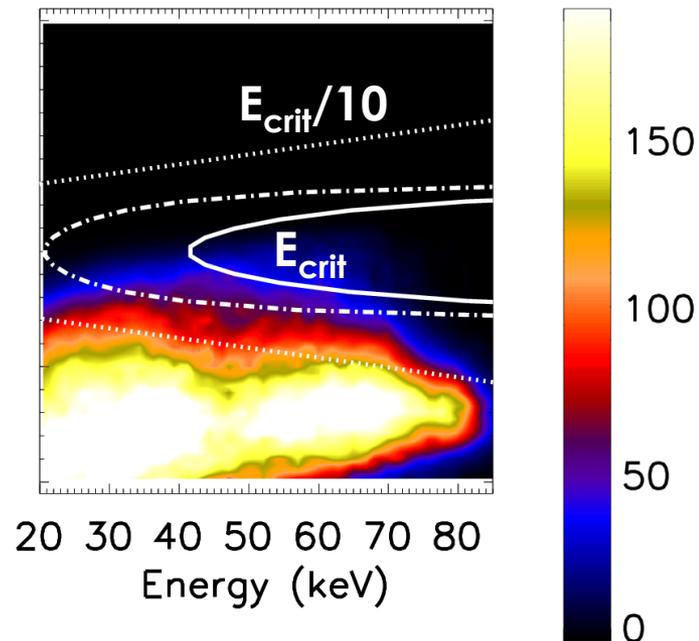
Co-passing

- Almost all detected particles satisfy $E \ll E_{crit} \approx 200$ keV
- Large transport expected



Counter-passing

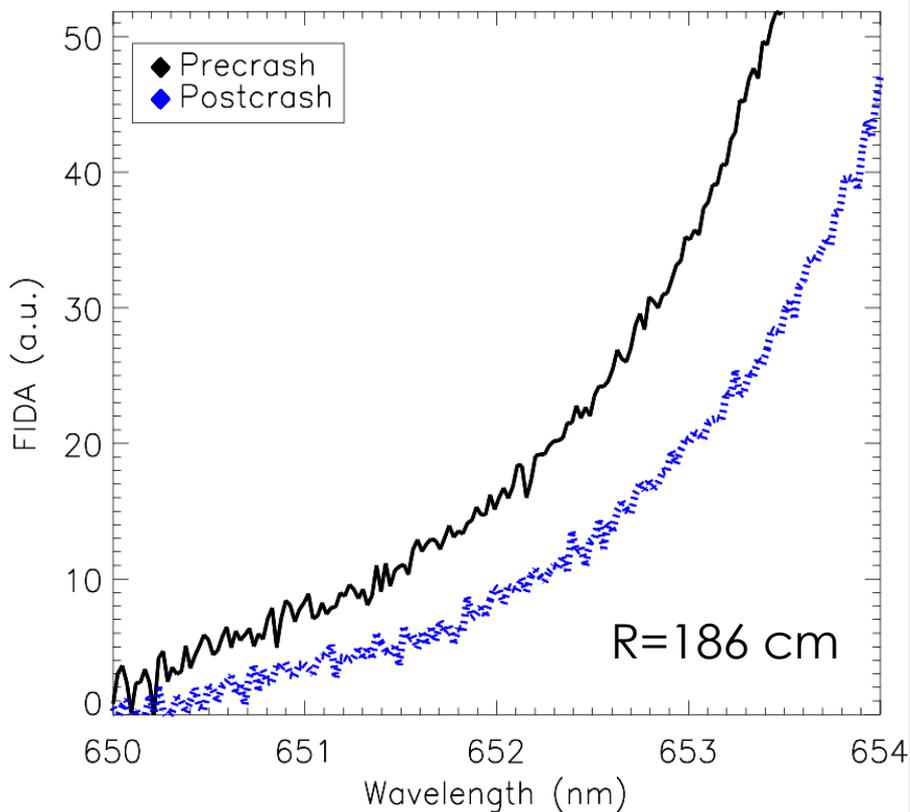
- Almost all detected particles satisfy $E \ll E_{crit} \approx 200$ keV
- Large transport expected



Evidence for E_{crit} Observed in FIDA Spectra

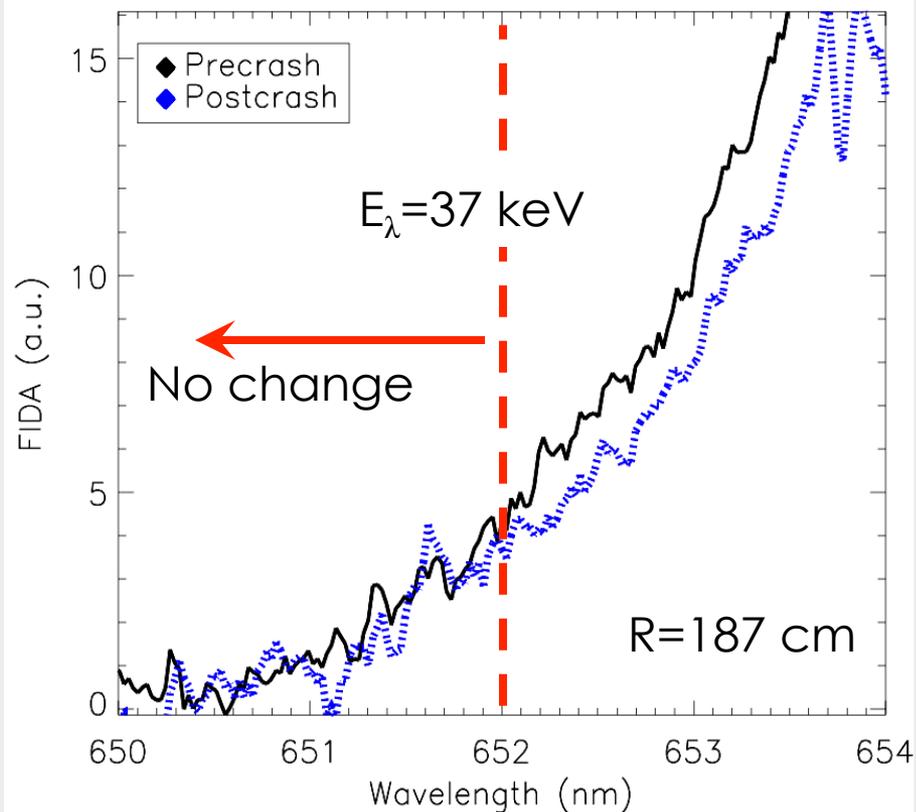
Co-passing spectrum

- Ions in the entire spectral range are redistributed
- $E_{\text{crit}}^{\text{passing}} > E_{\text{injection}}$



Mostly-trapped spectrum

- Depletion in spectrum observed for $E_{\lambda} \lesssim 40$ keV
- $E_{\text{crit}}^{\text{trapped}} < E_{\text{injection}}$



Summary

- The DIII-D FIDA suite incorporates 3 systems which weight velocity-space differently
- Experiments indicate that passing fast ions experience stronger transport than trapped
- Drift-kinetic simulation reproduces experimental observation of stronger passing fast-ion transport
- Mechanism differentiating trapped/passing transport: **Particle drifts and finite orbit width tend to decouple an ion from the evolving flux surfaces and weaken the effective transport**