

# Simulation of Reverse Shear Alfvén Eigenmodes using a gyrokinetic ion/fluid electron hybrid model

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Simulation Center

# Outline

- Fluid electron model in GEM
- Experimental observation of RSAE in DIII-D
- GEM linear simulation results
- Conclusion

# Mass-less fluid electrons

Electron continuity equation:

$$\frac{\partial n_e}{\partial t} + n_0 B \nabla_{\parallel} \frac{u_{\parallel e}}{B} + v_E \cdot \nabla n_0 + \frac{1}{m_e w_e B^2} B \times \nabla B \cdot \nabla (dp_{\perp} + dp_{\parallel}) + \frac{2n_0}{B^3} B \times \nabla B \cdot \nabla \phi = 0$$

Evolution equation for vector potential:  $\frac{\partial A_{\parallel}}{\partial t} = -E_{\parallel} - \nabla_{\parallel} \phi$

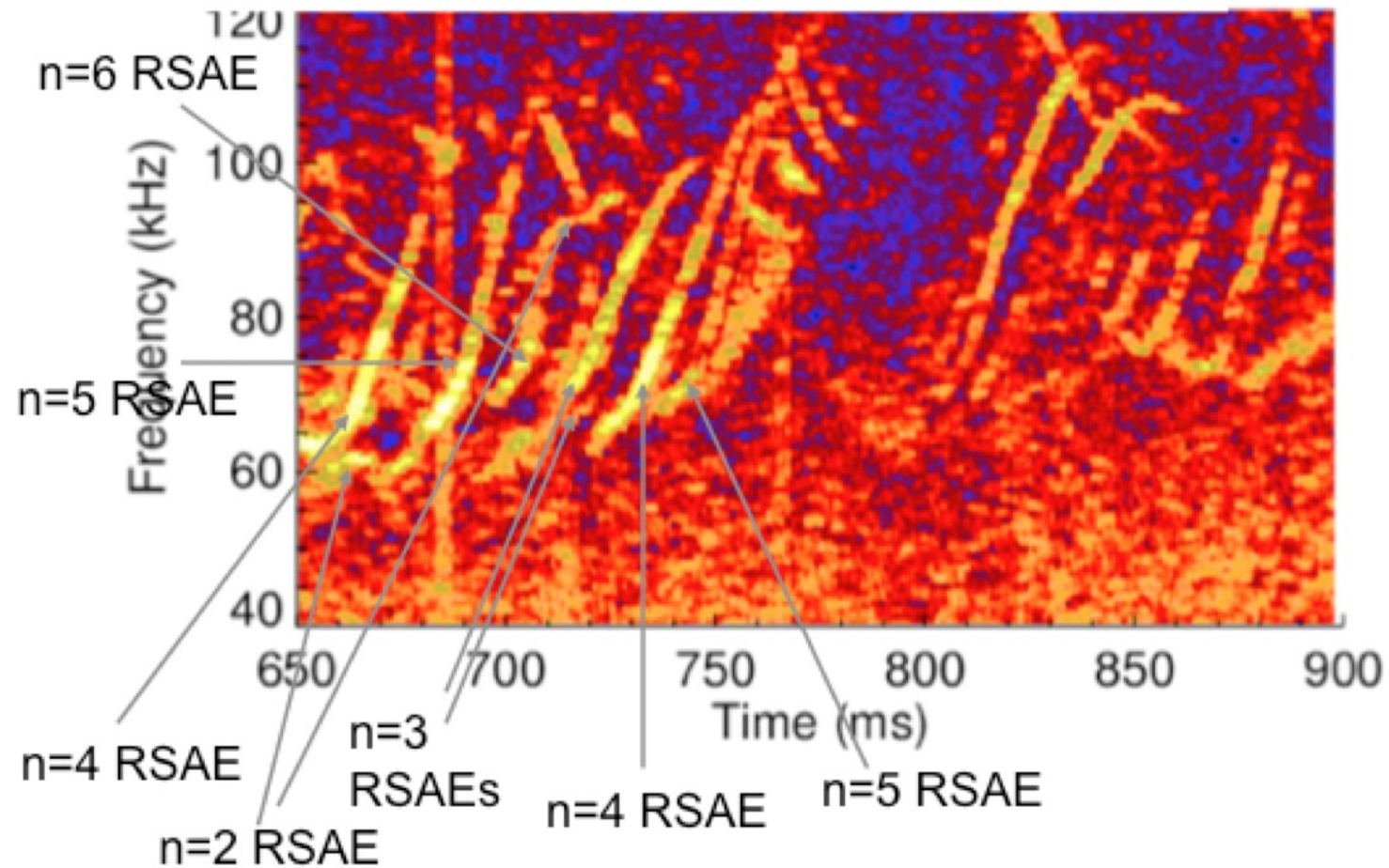
Ohm's law:  $en_0 E_{\parallel} = -\frac{\delta B_{\perp}}{B} \cdot \nabla p_0 - b \cdot \nabla \delta p_{\parallel e}$

Solve Ampere's law backwards:  $u_{\parallel e} = \nabla_{\perp}^2 A_{\parallel} + u_{\parallel i}$

Obtain  $\phi$  from quasi-neutrality

Gyrokinetic thermal ions and alpha particles ->  $u_{\parallel i}, \delta n_i$

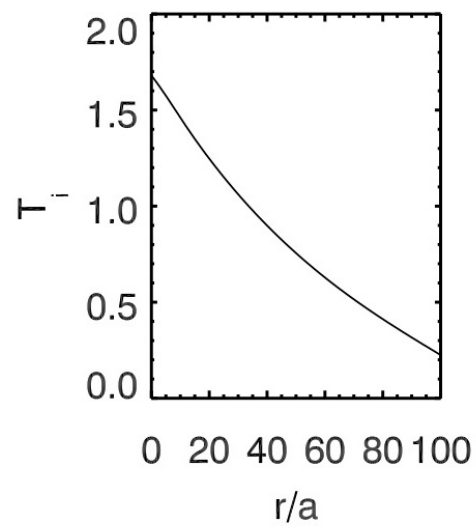
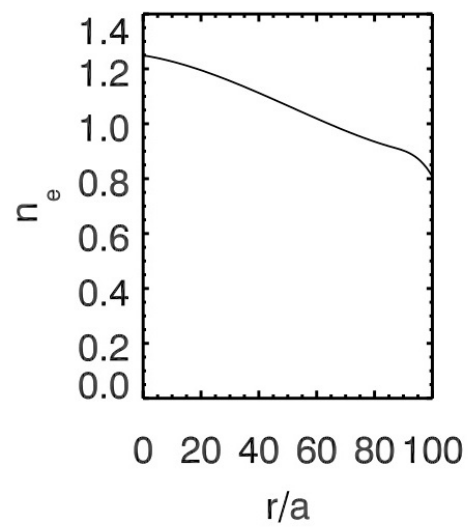
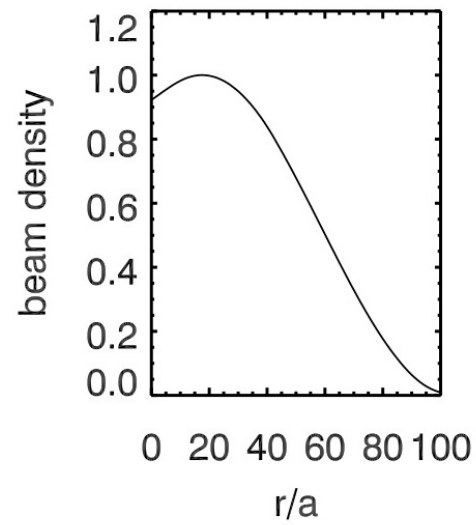
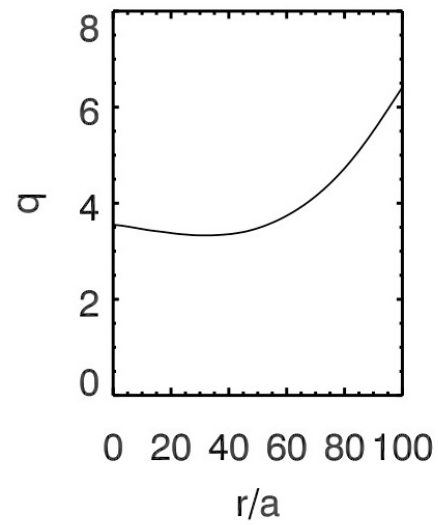
- DIII-D Shot #142111,  $t=725\text{ms}$
- $B_0=2.01254$  Tesla,  $a=0.63\text{m}$ ,  $R_0=1.65\text{m}$
- Elongation=1.6, triangularity=0.08
- Main ion D, beam D



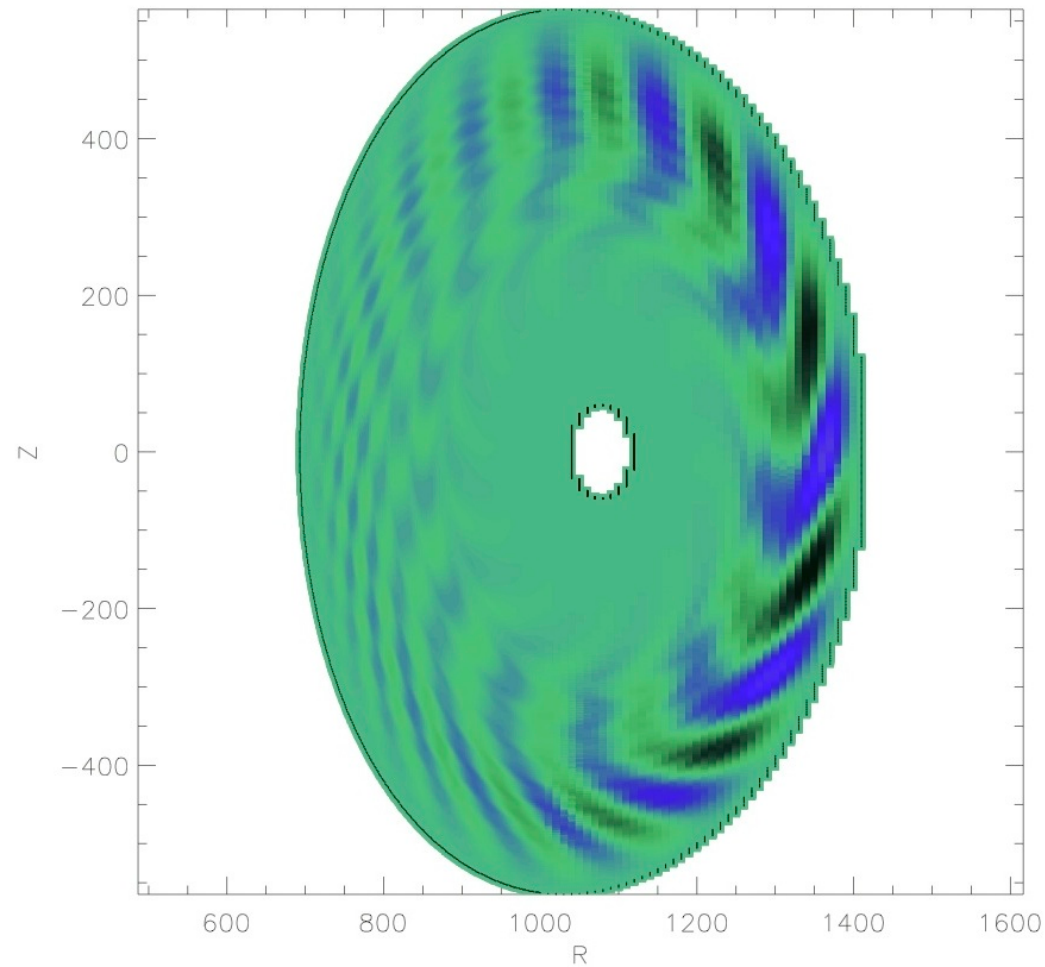
From M. Van Zeeland

Simulations are done for  $n=3$  at  $t=725\text{ms}$

# Experimental profiles from TAEFL.142111.725.inp

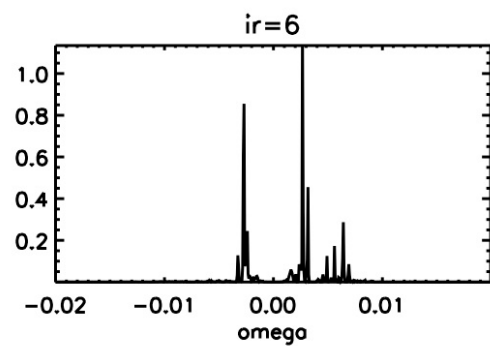
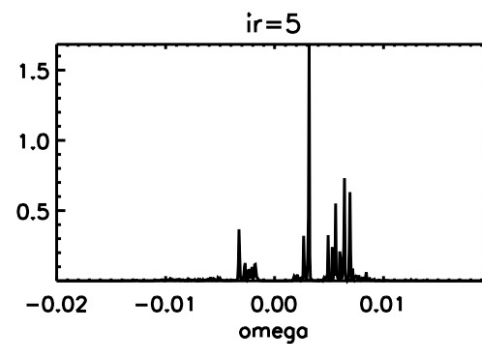
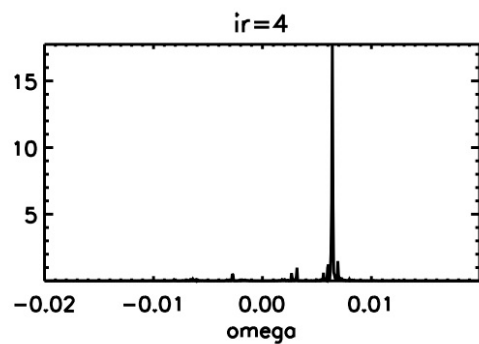
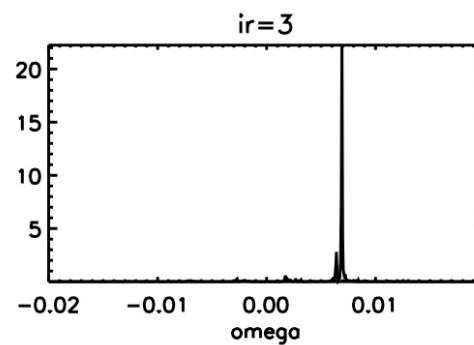
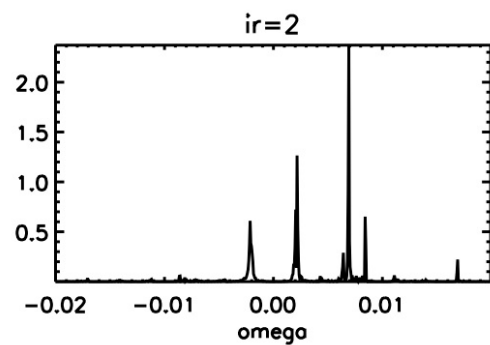
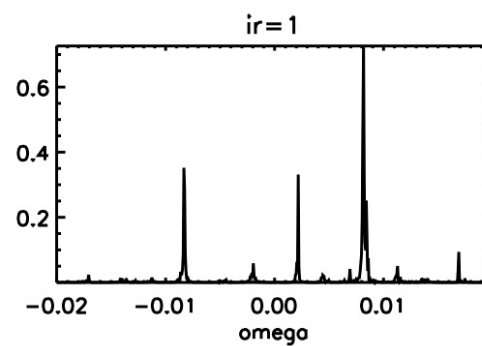
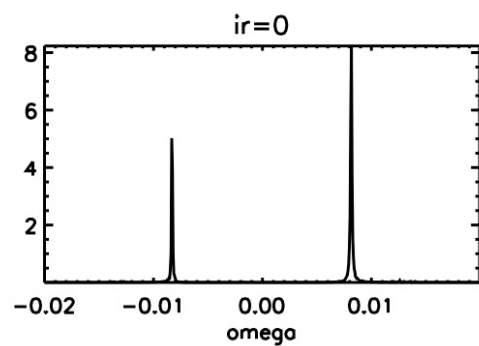


With experimental beam density, mode localized  
near  $r/a \sim 0.75$ ,  $f \sim 56\text{KHz}$

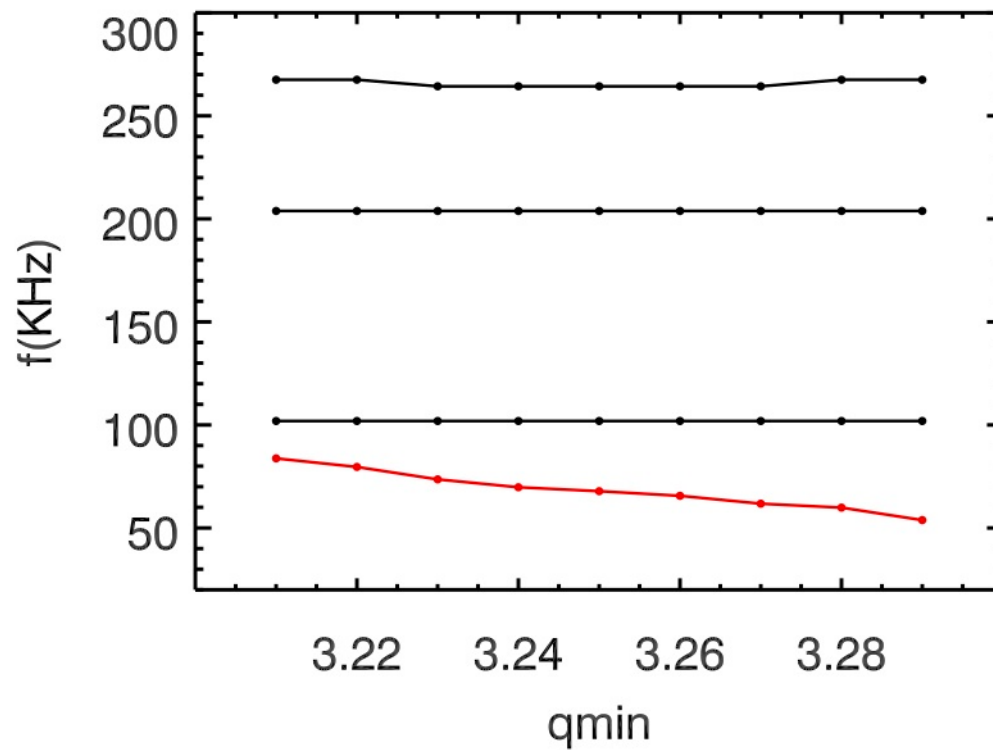


# Are there chirping modes when $\beta_{beam}=0$ ?

- Set  $\beta_{beam} = 0$ ,
- Vary  $q(r)$  by adding a small constant
- Fourier transform  $\phi(r_i, n=3, \theta=0, t)$  in time to find eigenmode frequencies



# Only the lowest frequency wave chirps

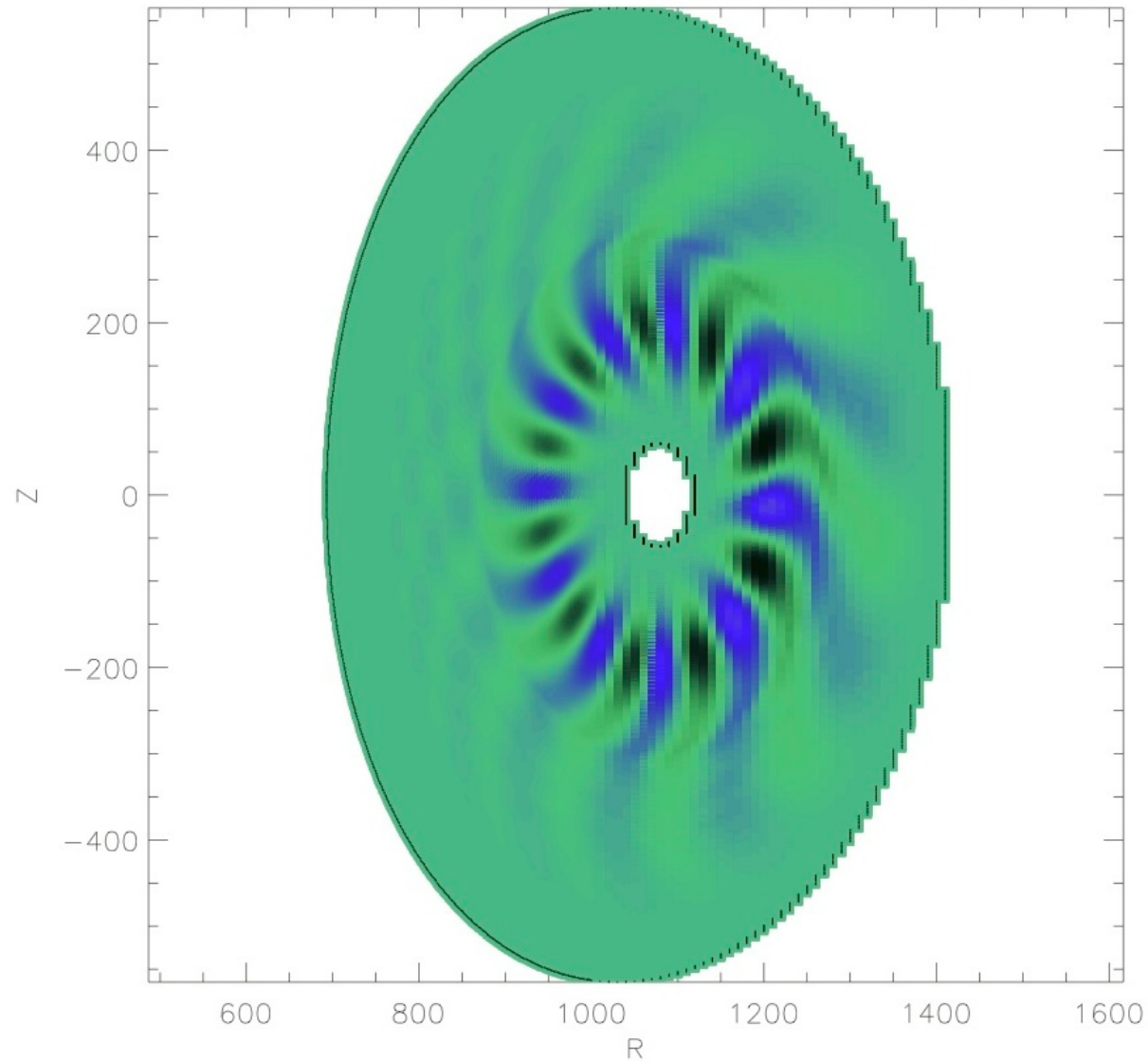


# Can RSAE be excited?

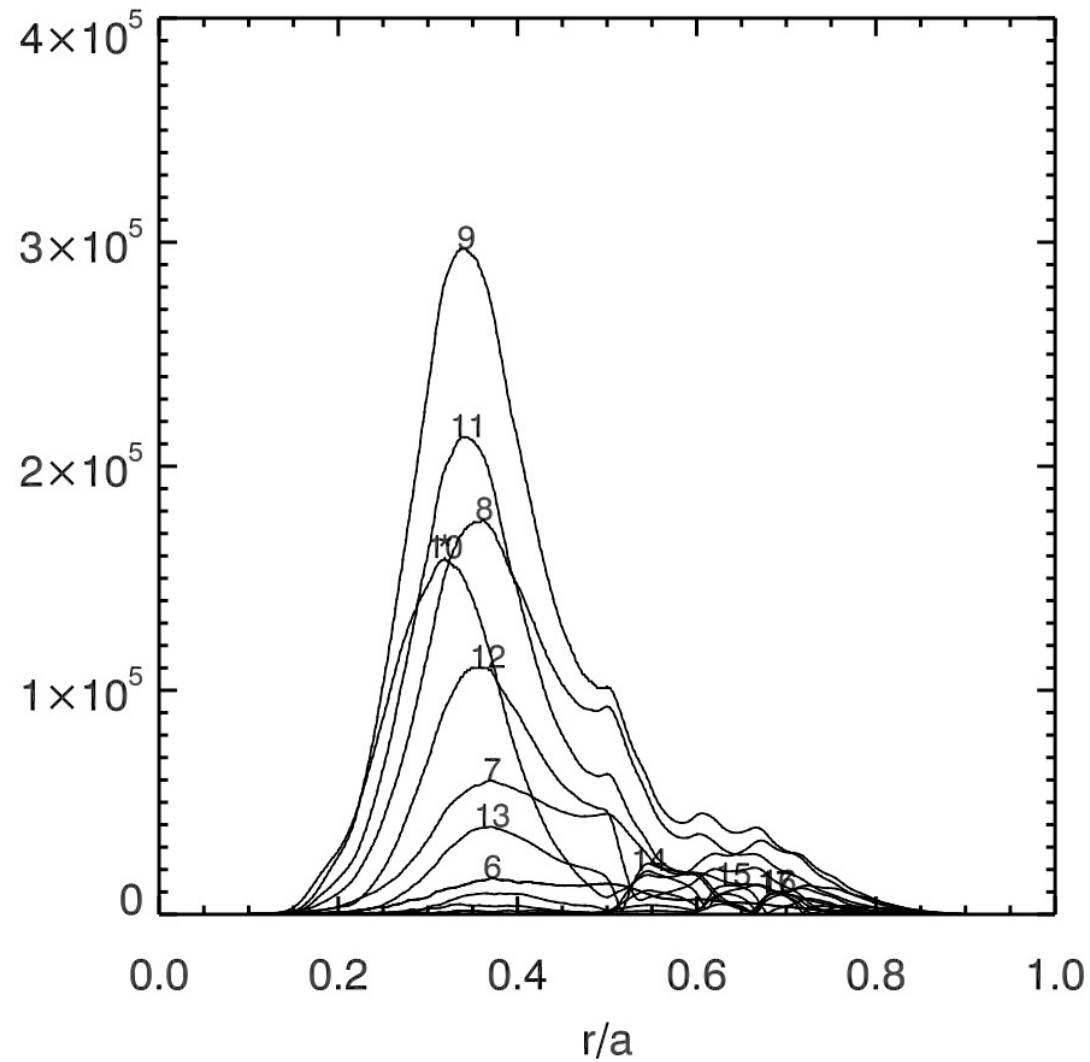
- Modify beam distribution according to

$$\beta_{beam}(r) = \beta_{beam}^{taefl}(r) \exp(-1.3r/a)$$

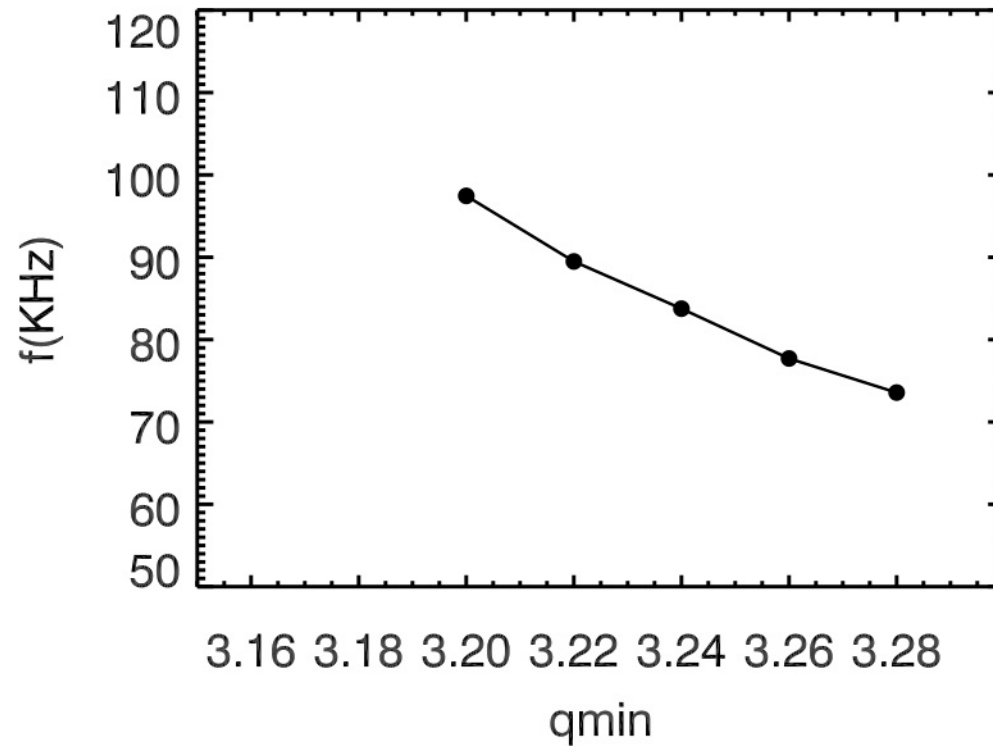
$$q'(r) = q(r) - 0.05$$



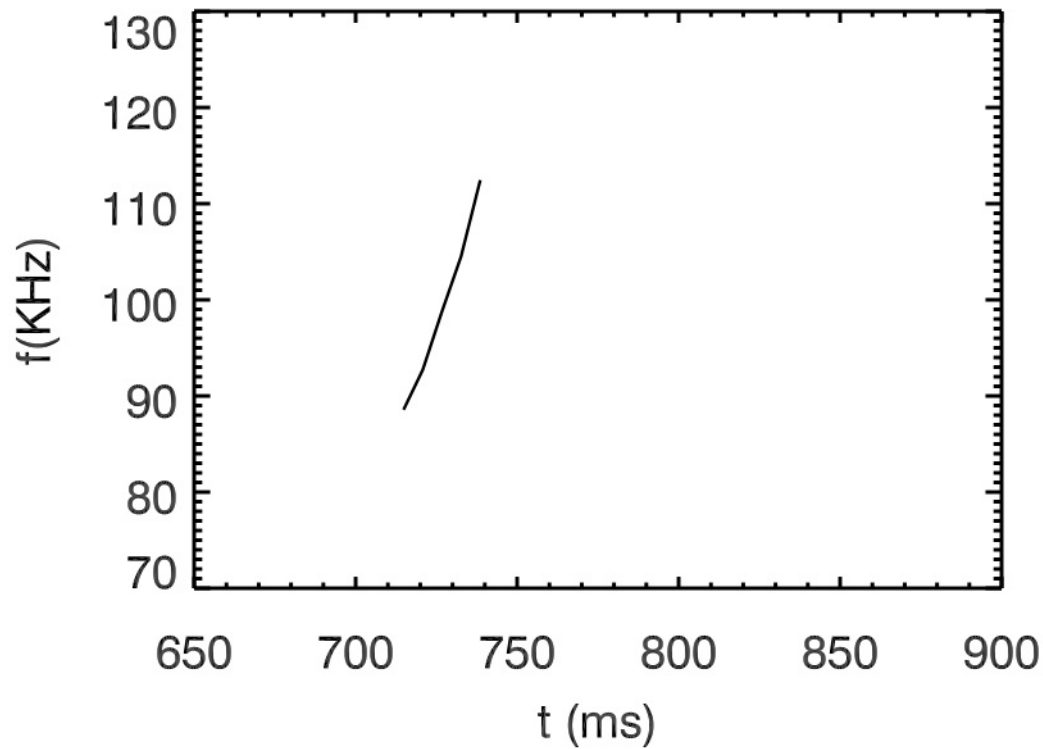
Mode not dominated by a single poloidal harmonics



# Frequency vs. $q_{\min}$



Chirping in time, Doppler shift of 15KHz assumed



$$q_{\min} = -0.00337(t - 700) + 3.33$$

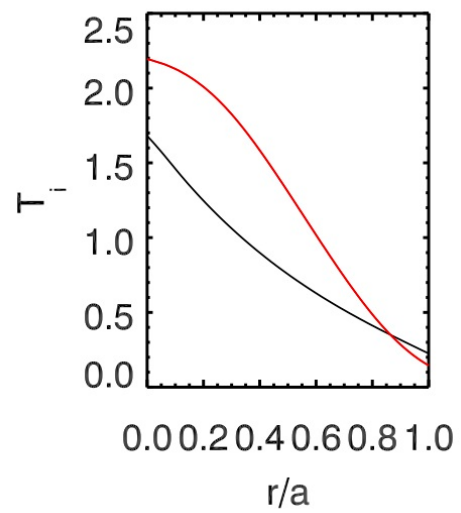
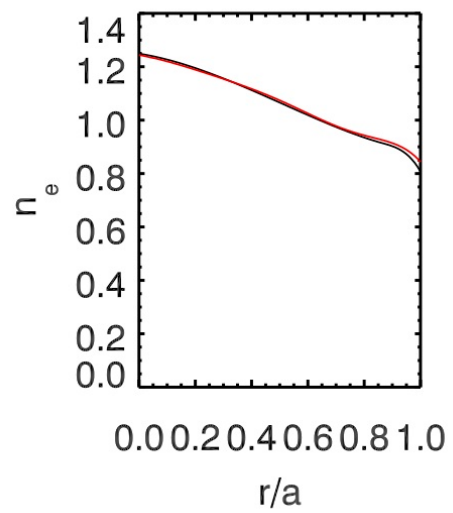
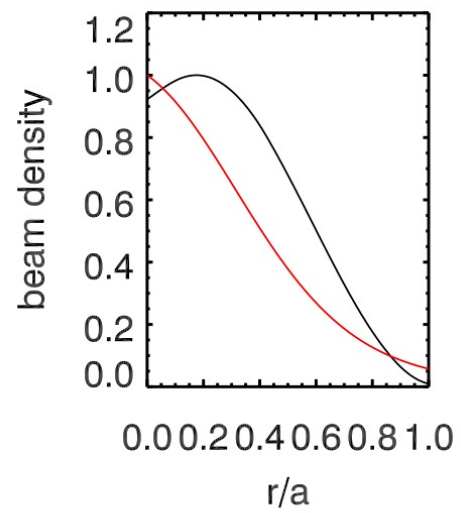
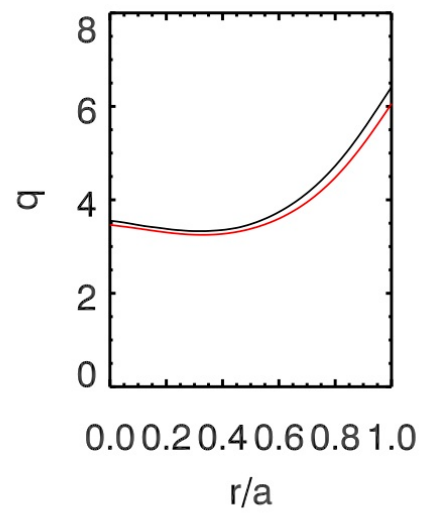
For a change of  $\Delta q_{\min}=0.08$ , f chirp range=25KHz, comparable to experiment

# Verification with M3D-K

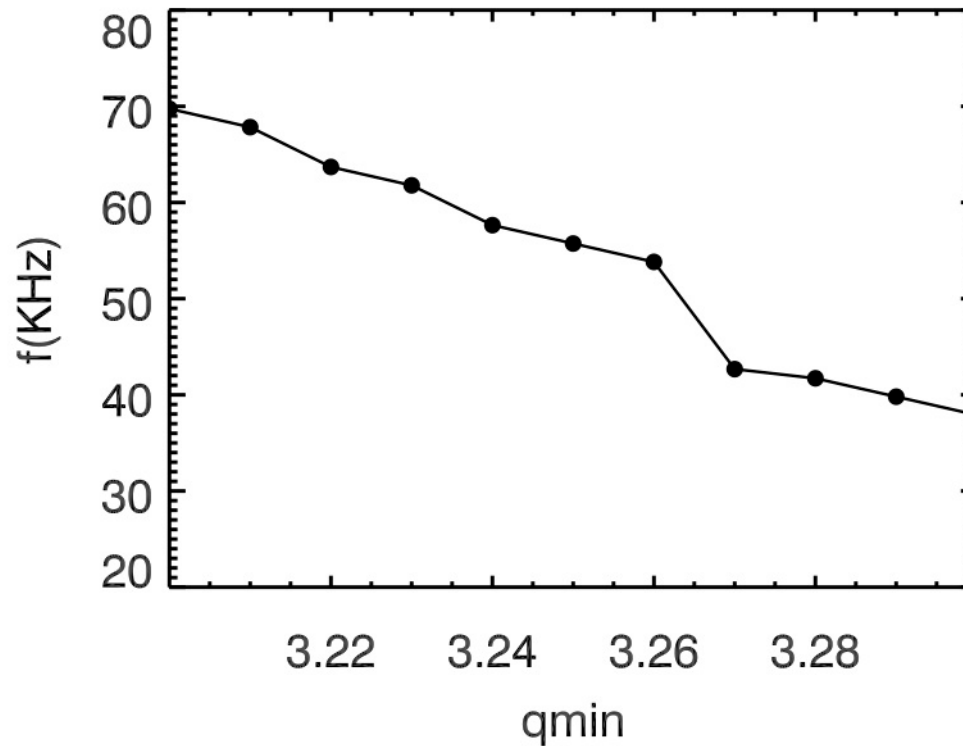
Use the same magnetic equilibrium, density and pressure profiles as in M3D-K

An analytic beam distribution

$$f = \left[ 1 + \operatorname{erf} \left( \frac{v_i - v}{v_A / 0.1} \right) \right] \exp(P_\phi / 0.25)$$

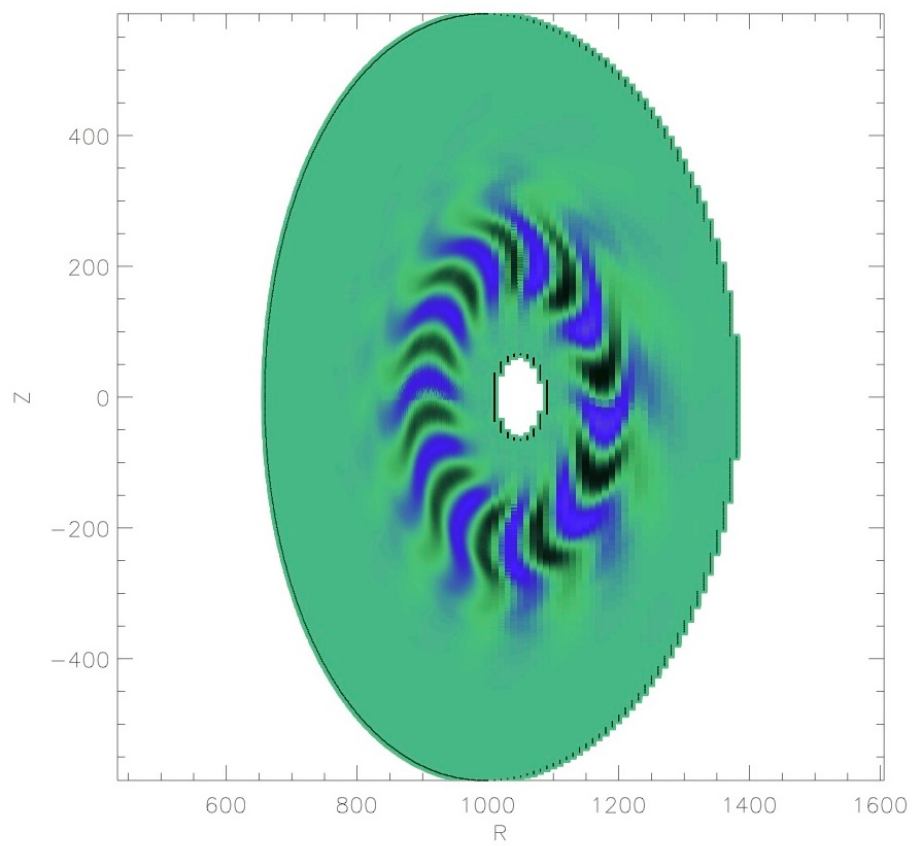


# Frequency vs. $q_{\min}$

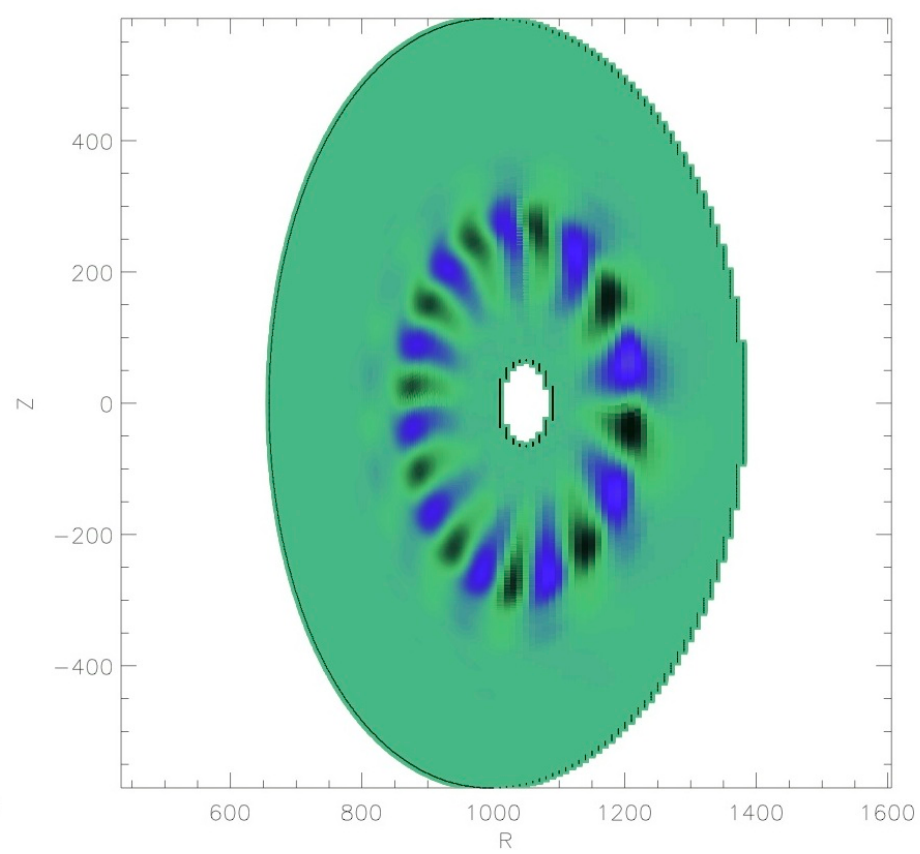


The steep drop at  $q_{\min}=3.27$  is due to change to a different mode

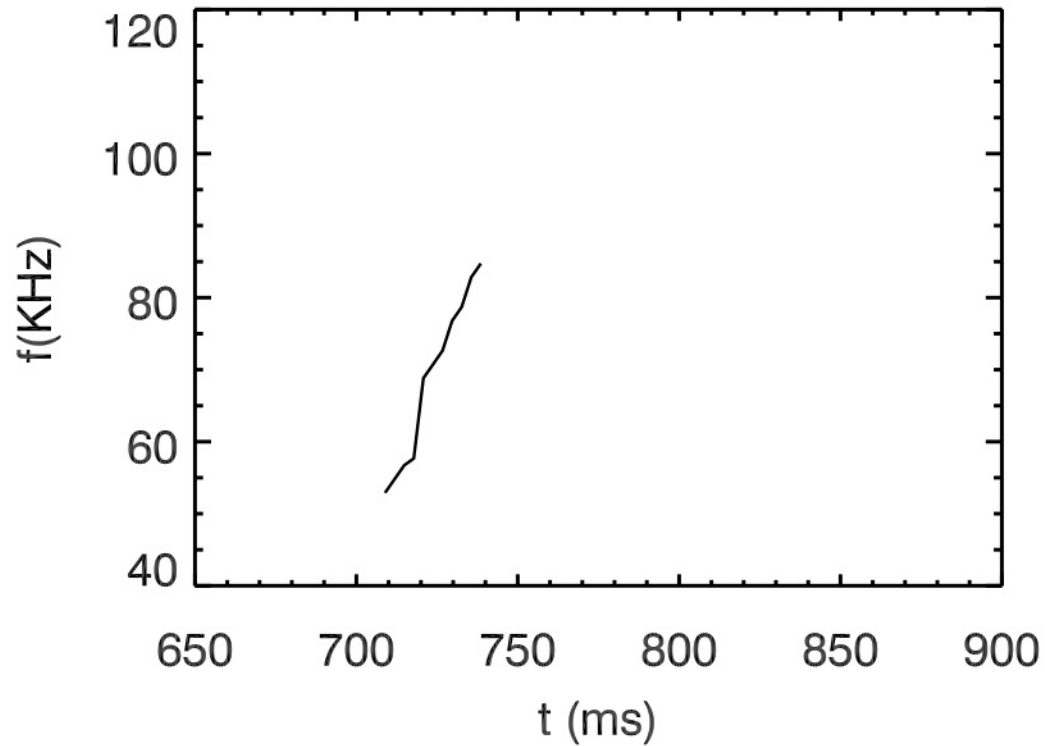
$q_{\min}=3.23$



$q_{\min}=3.27$



Chirping in time, Doppler shift of 15KHz assumed



$$q_{\min} = -0.00337(t - 700) + 3.33$$

For a change of  $\Delta q_{\min} = 0.07$ ,  $f$  chirp range = 25 KHz, comparable to experiment  
However, simulation frequency appears to be  $\sim 15$  KHz below experiment

Does the  $A_{||}/\phi$  model have the pressure effect on RSAE frequency?

Breizman et al. "Plasma pressure effect on Alfvén Cascading Modes", POP 12, 112506 (2005)

In GEM,  $\delta B_{||}=0$

However, GEM has GAM

# Summary

- Linear simulations of  $n=3$
- Using experimental (TAEFL) profiles, most unstable mode near the edge, far from  $q_{min}$
- Using more peaked beam distribution, chirping mode observed
- To do: Verification with M3D-K and validation with experimental beam distribution(?)