

Measurement and Modeling of Intrinsic Torque on DIII-D

By

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In Collaboration with

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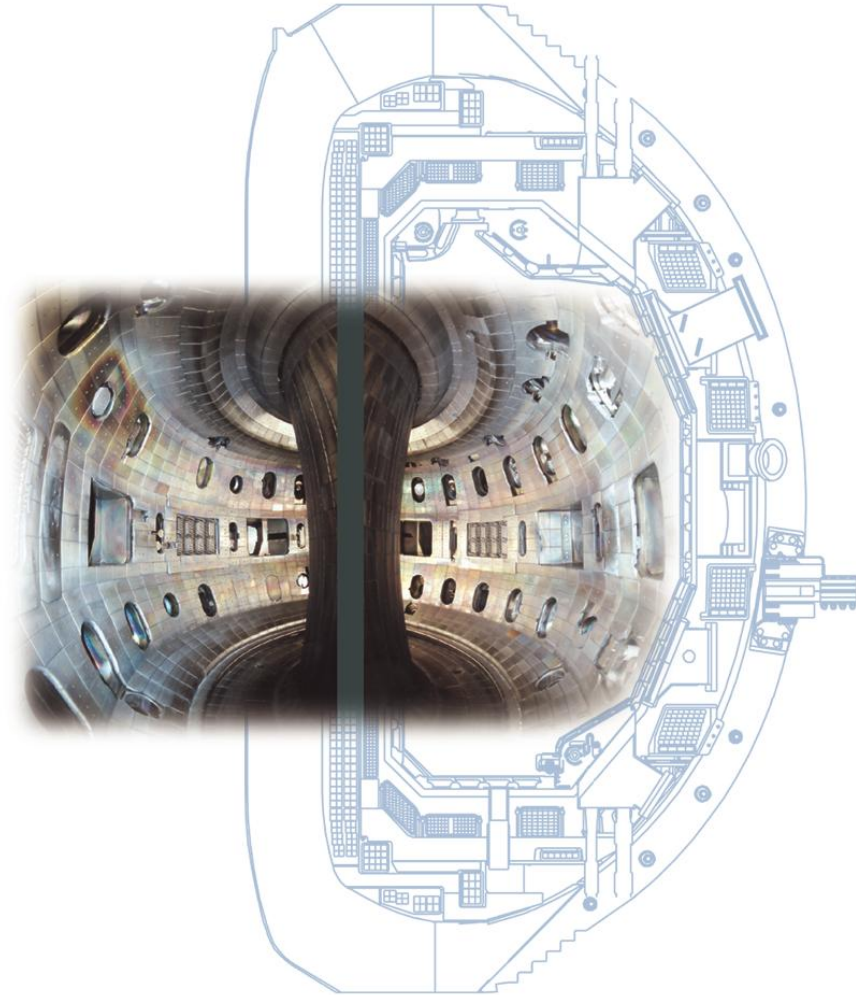
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Motivation

- **Toroidal rotation can enhance fusion performance through improvements in stability and confinement**
- **In present devices, rotation is usually driven by external means through neutral beam input, as a by-product of heating**
- **In future burning plasmas including ITER, torque driven by beams becomes comparatively smaller relative to moment of inertia**

Intrinsic Rotation Must Manifest Itself From Terms in Toroidal Angular Momentum Balance Equation

$$mR \frac{\partial n V_\phi}{\partial t} = \underbrace{\sum \eta}_{\text{Torque densities}} - \underbrace{\nabla \cdot \Pi_\phi}_{\text{Transport}} + \dots$$

Rate of change of angular momentum density

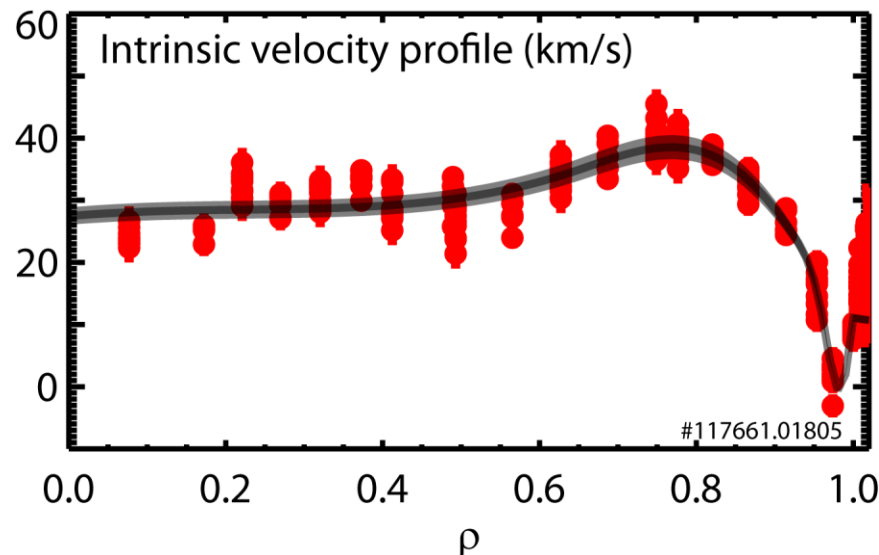
Intrinsic drive

$$\Pi_\phi = -mnR \left(\underbrace{\chi_\phi \frac{\partial V_\phi}{\partial r}}_{\text{diffusion}} - \underbrace{V_\phi V_{pinch}}_{\text{pinch}} \right) + \underbrace{\Pi_{RS}}_{\text{Residual stress}}$$

- Turbulence driven
- Independent of velocity

$$\sum \eta = \eta_{NBI} + \dots ?$$

- Other unspecified torques

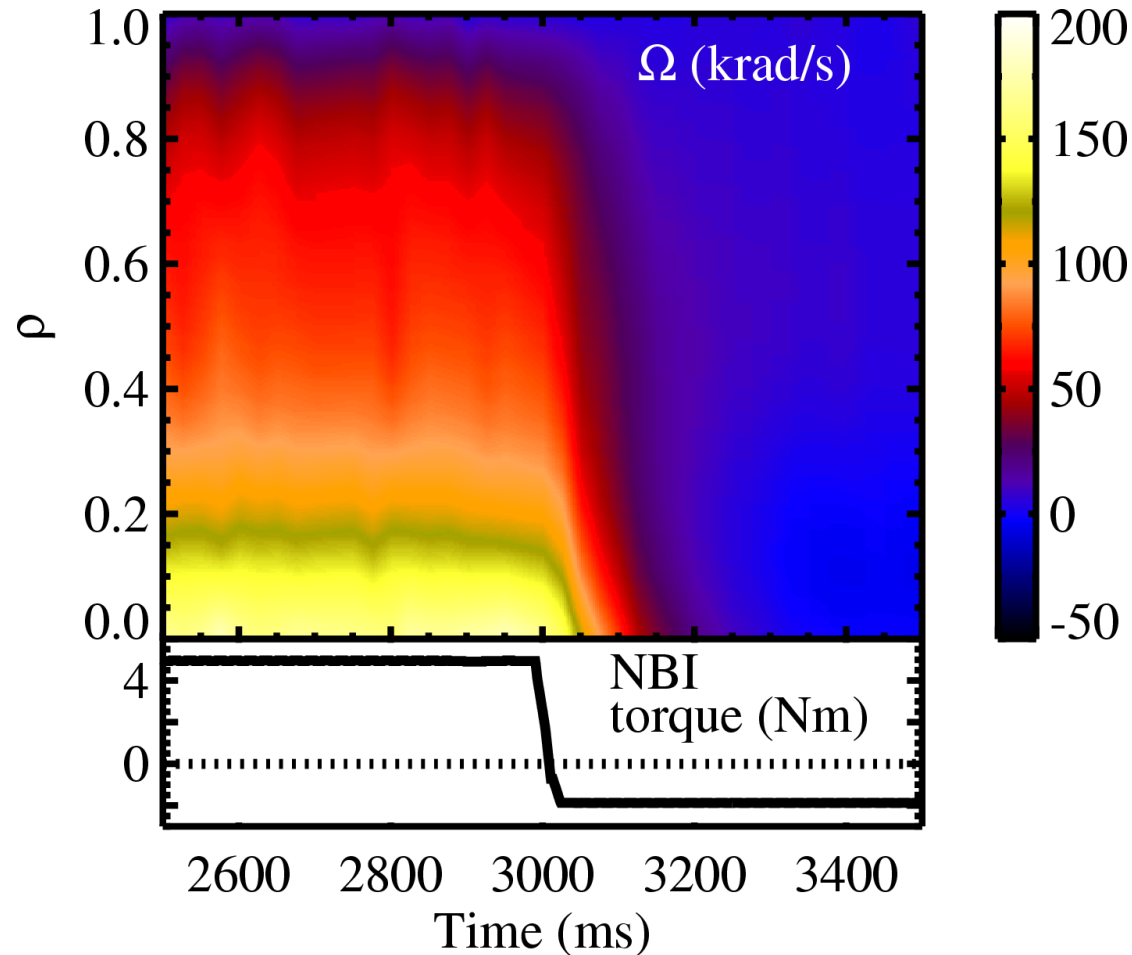


Intrinsic Torque Profile Can Be Measured With Beams By Zeroing Out Rotation Profile

- With co-current NBI torque, rotation is also co- I_p
- By adjusting torque slightly counter, rotation is essentially zero across profile
- Intrinsic torque balanced by beam torque

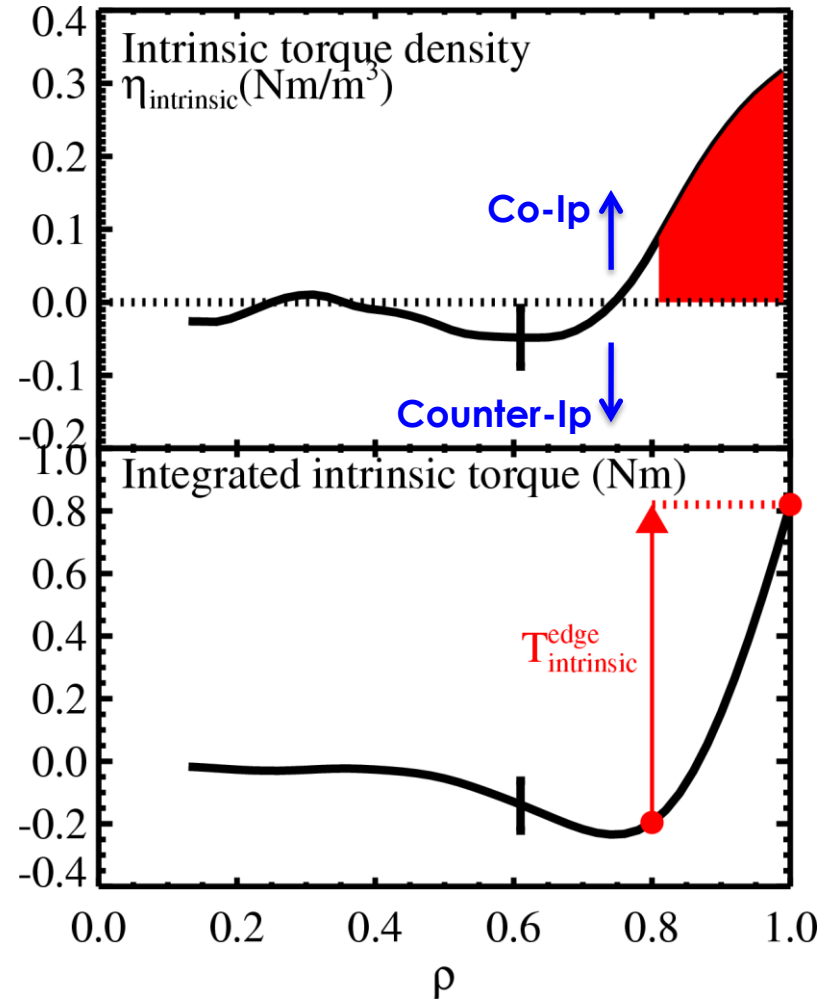
$$\eta_{NBI} + \eta_{intrinsic} = 0$$

$$\rightarrow \eta_{intrinsic} = -\eta_{NBI}$$



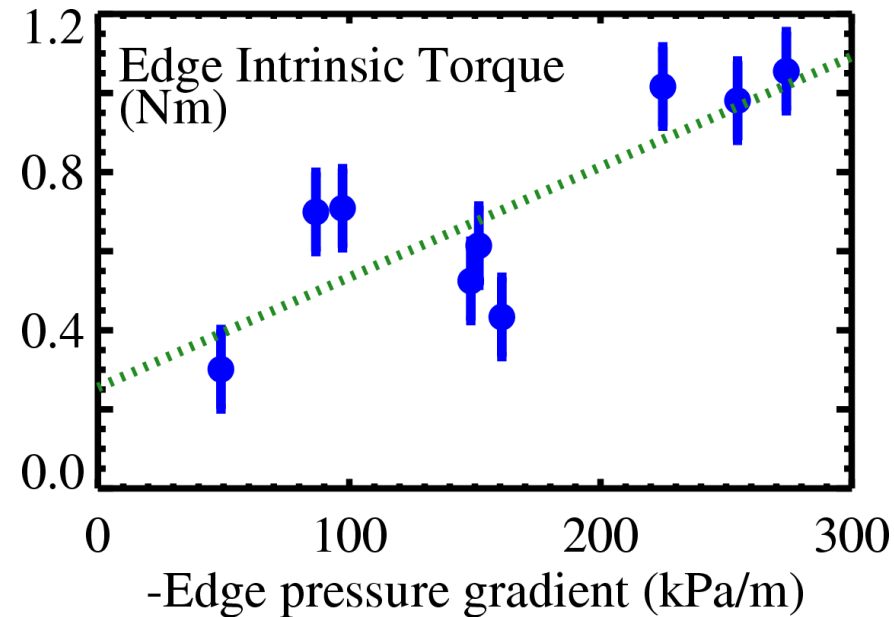
Intrinsic Torque Profile in H-Mode Plasmas Always Peaked at the Edge

- **Intrinsic torque at the edge ($0.8 < \rho < 1$) found to be**
 - Always co-current directed
 - Typically comparable to between 0.5-1 NB source
- **Torque inside of mid-radius typically negligible by comparison**
- **Empirically, what processes contribute to the intrinsic torque?**



Edge Intrinsic Torque Is Well Correlated with Pedestal Pressure Gradient

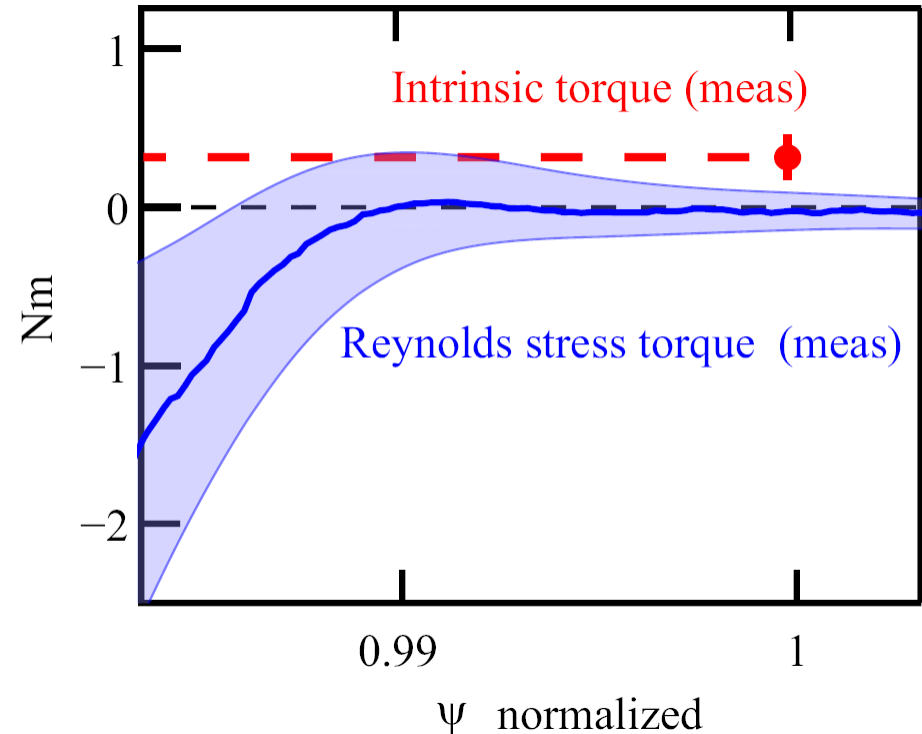
- Data obtained from power and plasma current scans
- **Qualitatively suggestive of turbulence driven stress generating intrinsic rotation**
 - Turbulent residual stress can be driven via $E \times B$ shear or other profile shear
- **Shear in H-mode pedestal may provide mechanism to drive intrinsic rotation in future devices**



Solomon et al, PoP (2010)

But... Probe Measurements Find Turbulent Stress Does Not Match Intrinsic Torque

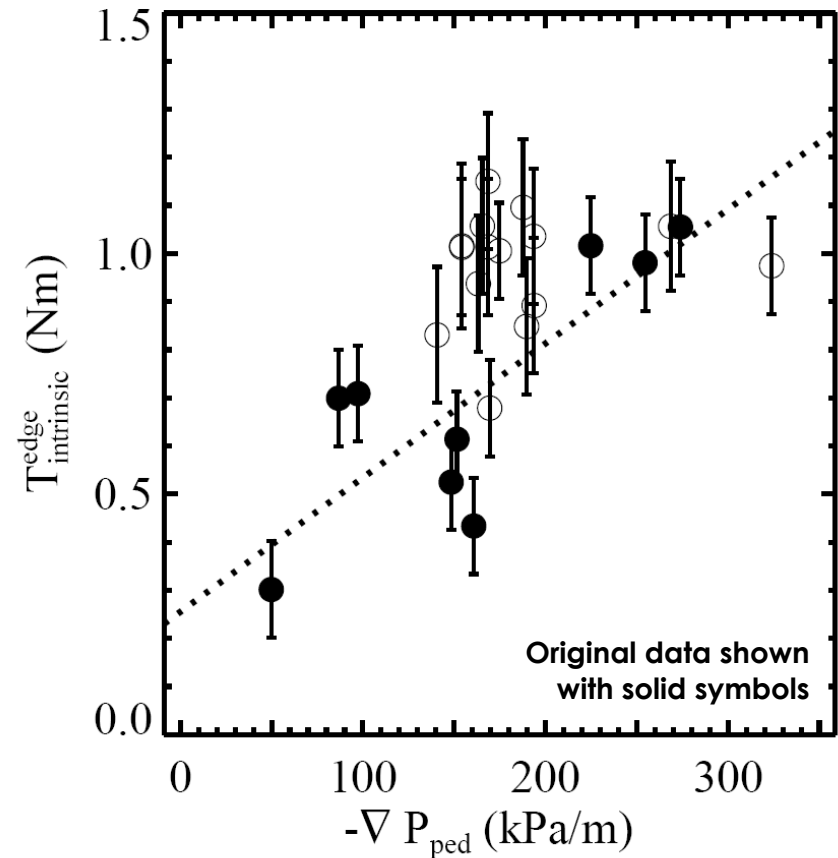
- **Multi-tip reciprocating probe measures all terms of fluid stress tensor**
 - Mostly arises from Reynolds stress contribution
- **Discrepancy implies there are additional torques at edge contributing to intrinsic drive**



Muller et al, PRL 2011

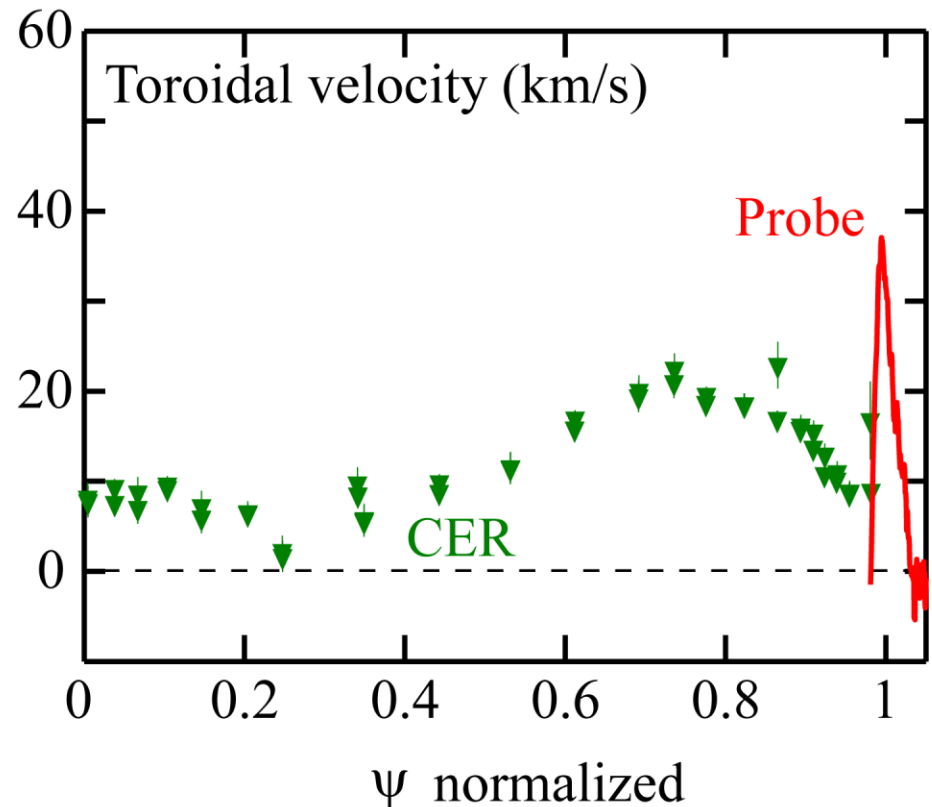
Additional Physics Is Required to Understand Edge Intrinsic Torque from Wider Data Set

- Include QH-mode, hybrid plasmas, different shapes (USN, LSN, DN) and toroidal rotation levels
- Relationship between edge intrinsic torque and pressure gradient becomes much less clear
- Almost factor of 3 variation for fixed $\nabla P_{ped} \sim -160$ kPa/m



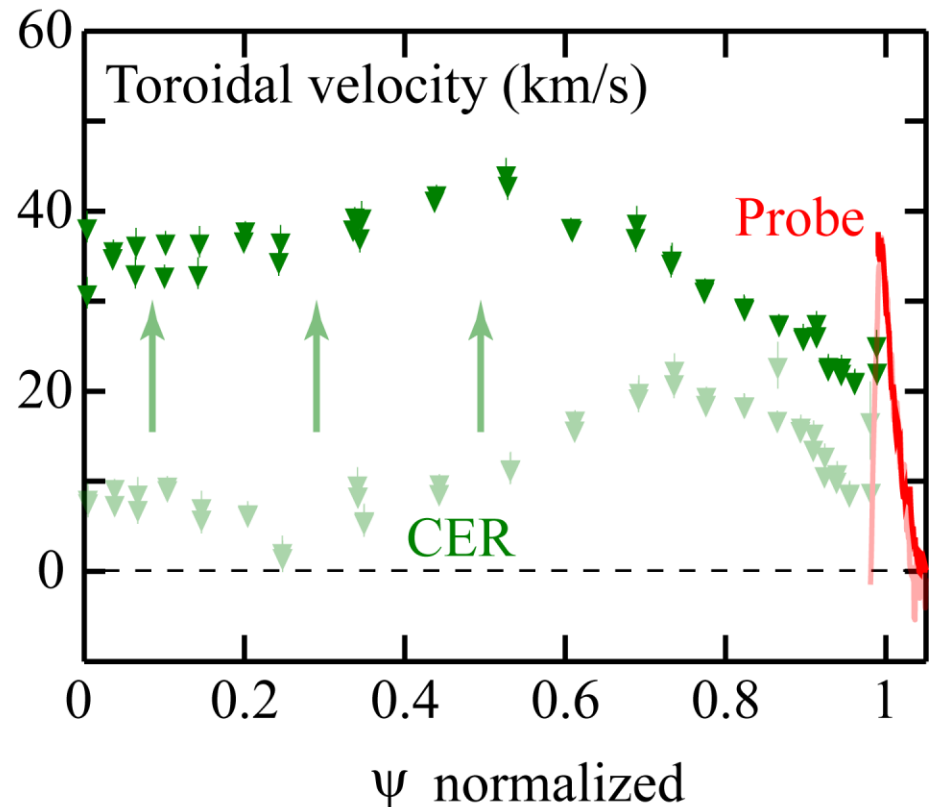
Intrinsic Drive Appears to Originate from Narrow Region at the Edge

- **Edge rotation layer observed within 50 ms of L-H transition**
 - At time when core rotation remains low



Intrinsic Drive Appears to Originate from Narrow Region at the Edge

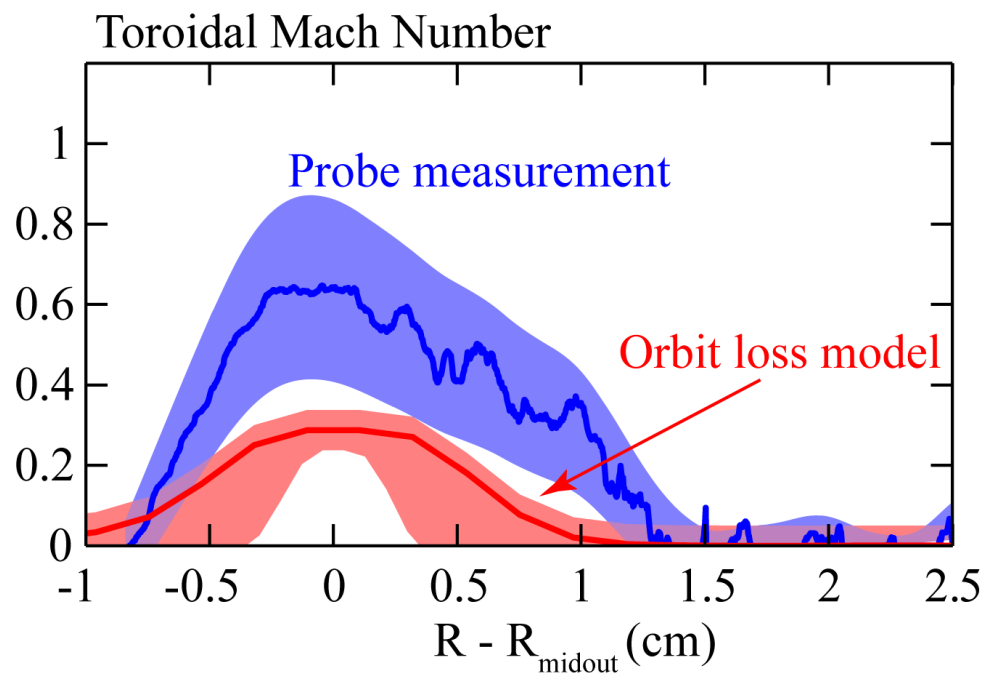
- **Edge rotation layer observed within 50 ms of L-H transition**
 - At time when core rotation remains low
- **Core intrinsic rotation develops over time**
- **Therefore, edge layer may contribute “seed” to core intrinsic rotation**



See Grierson, after lunch for details on new main ion CER measurements

Simple Model of Thermal Ion Orbit Loss Qualitatively Reproduces Edge Rotation Layer

- Estimate velocity resulting from loss cone of counter-going thermal ions whose orbits are lost to divertor
- Thermal ion orbit loss may help explain missing torque



Torque from Orbit Loss Expected to Show Dependence on Edge Ion Temperature

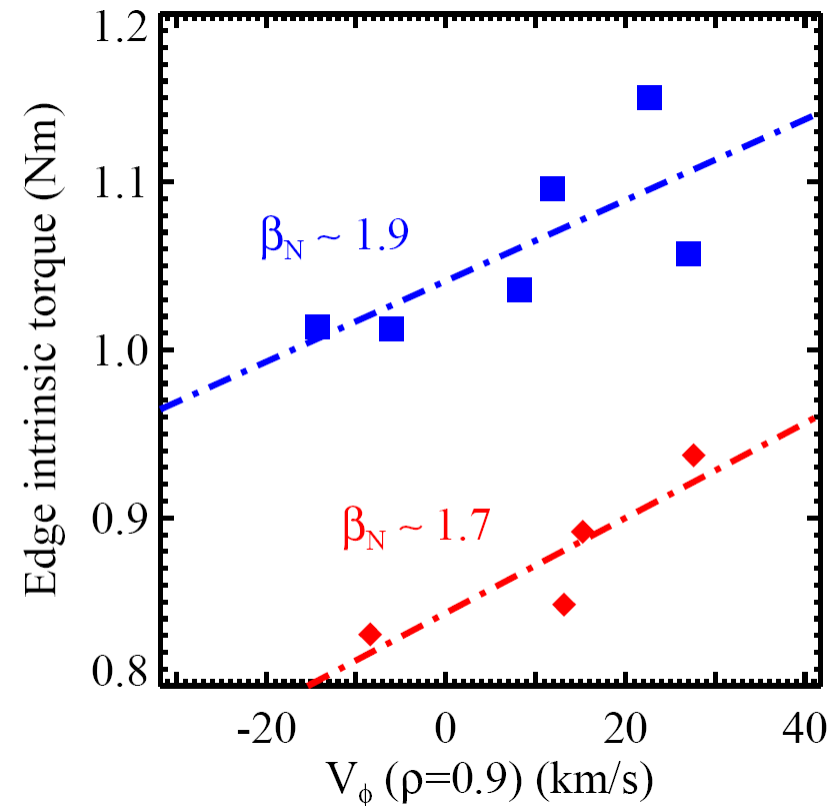
- **Measure of orbit loss torque made estimating rate at which collisions drive empty loss cone toward Maxwellian**

$$\eta_{O.L.} \propto v_{mn} \left\langle RV_{\phi}^{\rho=1} \right\rangle$$

- **Separatrix velocity in turn dependent on**
 - Separatrix ion temperature $\sqrt{T_i^{\rho=1}}$
 - location of the x-point relative to the midplane separatrix R_x / R_{mid}
- **Empirically, add these quantities to regression analysis to understand edge intrinsic torque data set**

Intrinsic Torque Persists Even in Plasmas With Finite External Momentum Input

- **Weak dependence of intrinsic torque on rotation**
 - Enhanced at rapid rotation by approx 0.25 Nm per 100 km/s of velocity at top of pedestal
- **Intrinsic torque increases with β_N**
 - Partially due to changes in ∇P_{ped}

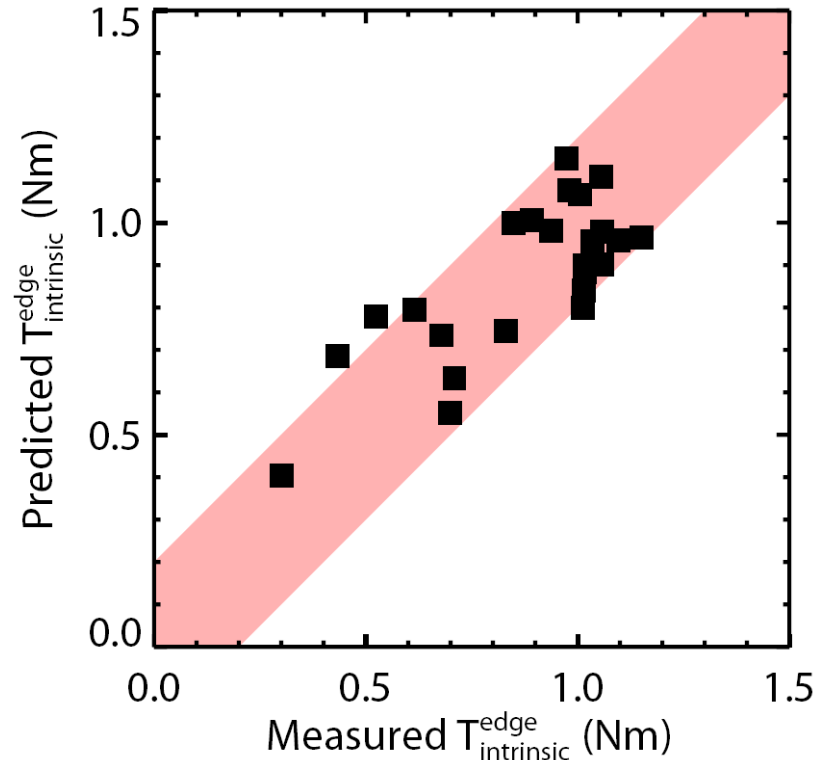


Consideration of Various Empirical Quantities Gives Excellent Predictor of Edge Intrinsic Torque

- Pedestal pressure gradient (∇P_{ped})
- Orbit loss physics (T_i, R_x)
- Finite rotation effects (V_ϕ)

$$T_{\text{intrinsic}}^{\text{edge}} = -2.80 \times 10^{-3} \nabla P_{\text{ped}} \text{ (kPa/m)} \\ + 0.38 \sqrt{T_i^{\rho=1}} \text{ (keV)} \\ + 0.56 V_\phi^{\rho=0.9} \text{ (100 km/s)} \\ + 0.16 \frac{R_x}{R_{\text{mid}}}$$

- $R^2 > 0.9$ (vs 0.34 for ∇P_{ped} only fit)
- Intrinsic torque predicted within ~ 0.2 Nm



Solomon et al, NF (submitted)

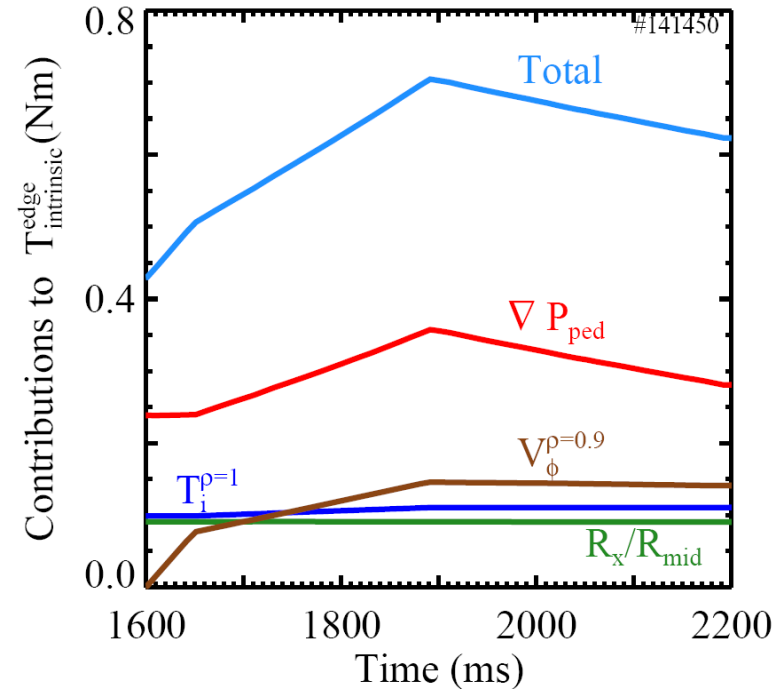
Empirical Model of Intrinsic Torque Is Used to Model Intrinsic Rotation Evolution Following L-H Transition

- **Build model based on:**

- Spatially and temporally constant χ_ϕ
- Pinch velocity V_{pinch} calculated in TRANSP based on theoretical models
 - Previously showing reasonable agreement with experiment
- Boundary condition V_ϕ from Mach probe measurement
- Intrinsic torque density profile

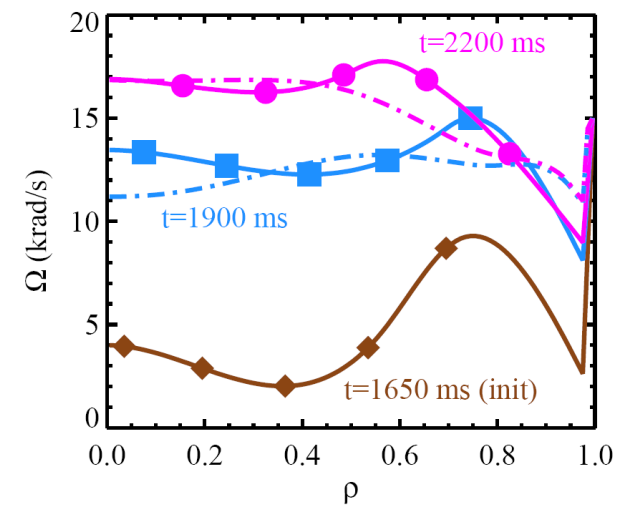
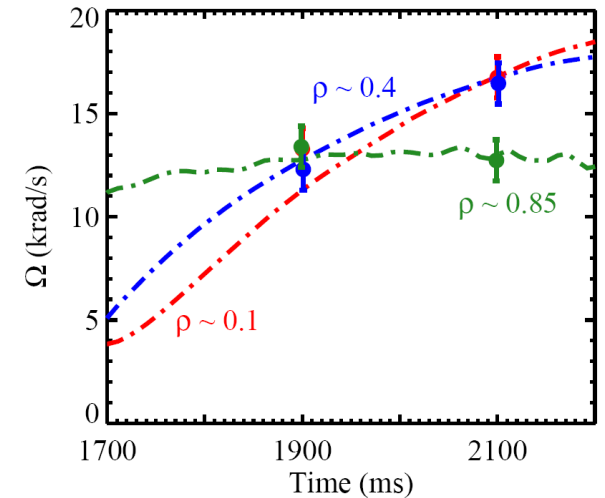
$$\begin{aligned} \eta_{\text{intrinsic}}(\rho, t) &= 0 && \text{for } \rho < 0.8 \\ &= c(t)(\rho - 0.8) && \text{for } 0.8 < \rho < 0.96 \\ &= \eta_{RS}^{\text{probe}}(\rho, t) && \text{for } \rho > 0.96 \end{aligned}$$

with c chosen so as to match model for edge intrinsic torque



Empirical Intrinsic Torque Profile Model Plus Simple Transport Model Is Sufficient to Reproduce Rotation

- Intrinsic rotation profile measured shot-to-shot with NBI blips at different delays
- Simulate intrinsic rotation evolution inside $\rho < 0.99$
- Narrow rotation layer semi-quantitatively reproduced and persists in time
 - Only possible with inclusion of intrinsic torque profile



Conclusions

- **Plasma edge capable of generating an intrinsic torque that is robustly observed in all H-modes**
- **Contributions to edge intrinsic torque include**
 - Pedestal pressure gradient (residual stress)
 - Separatrix temperature, X-point location (thermal ion orbit loss)
 - Enhancement / positive feedback with velocity
- **Empirically determined expression for edge intrinsic torque serves as excellent predictor**
- **Intrinsic rotation evolution after L-H transition consistent with modeling based on calculated intrinsic torque**