

# Nonlinear Evolution and Radial Propagation of the Energetic Particle Driven GAM

by

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In collaboration with

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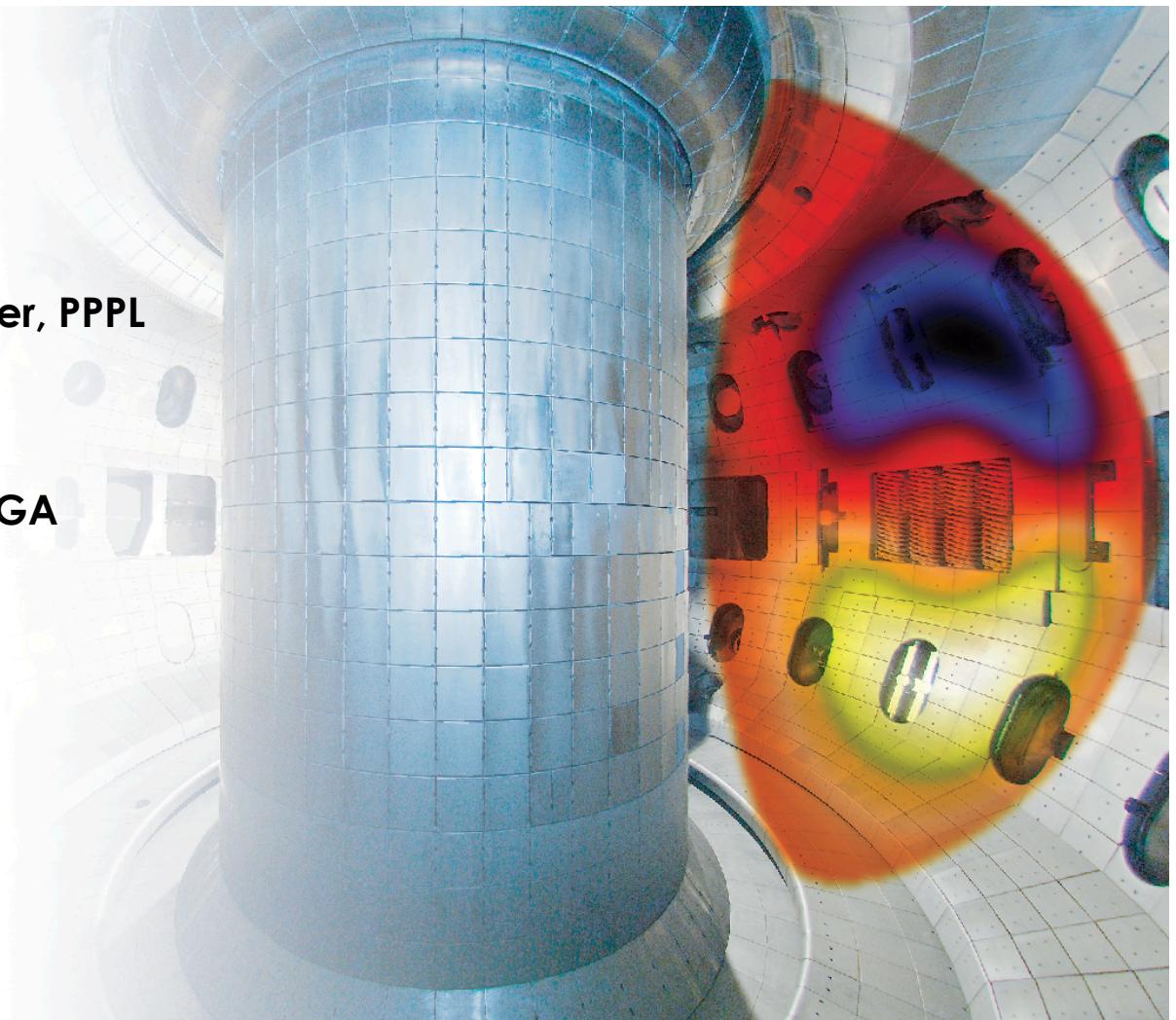
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R. Fischer, M.A. Van Zeeland, GA

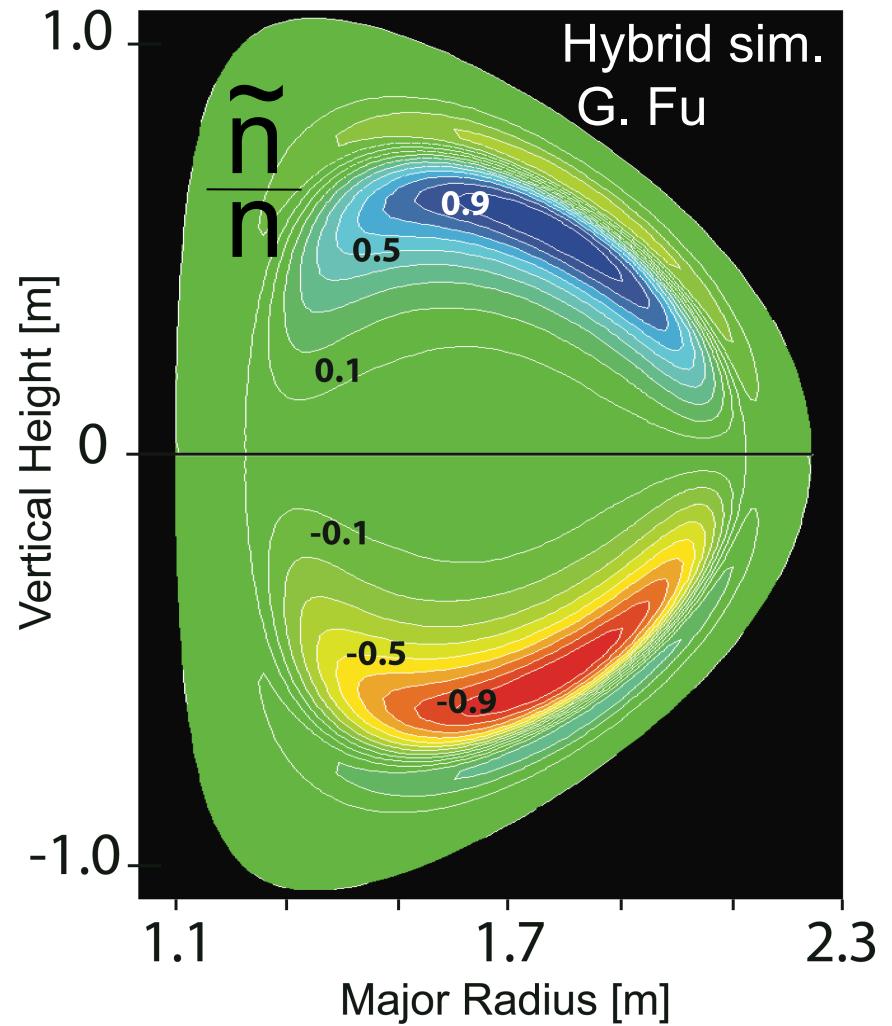
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April 8, 2011



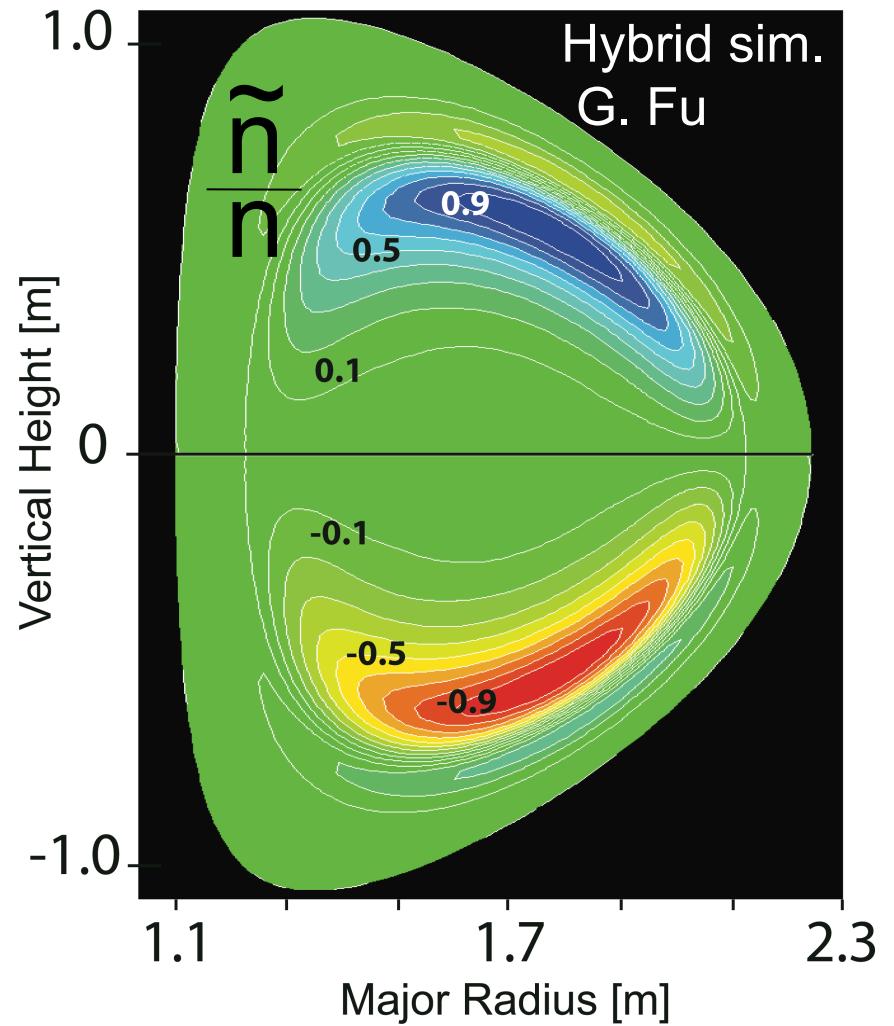
# Outline

- Mode excitation/structure
- Comparison to linear E-GAM theory
- Nonlinear E-GAM evolution

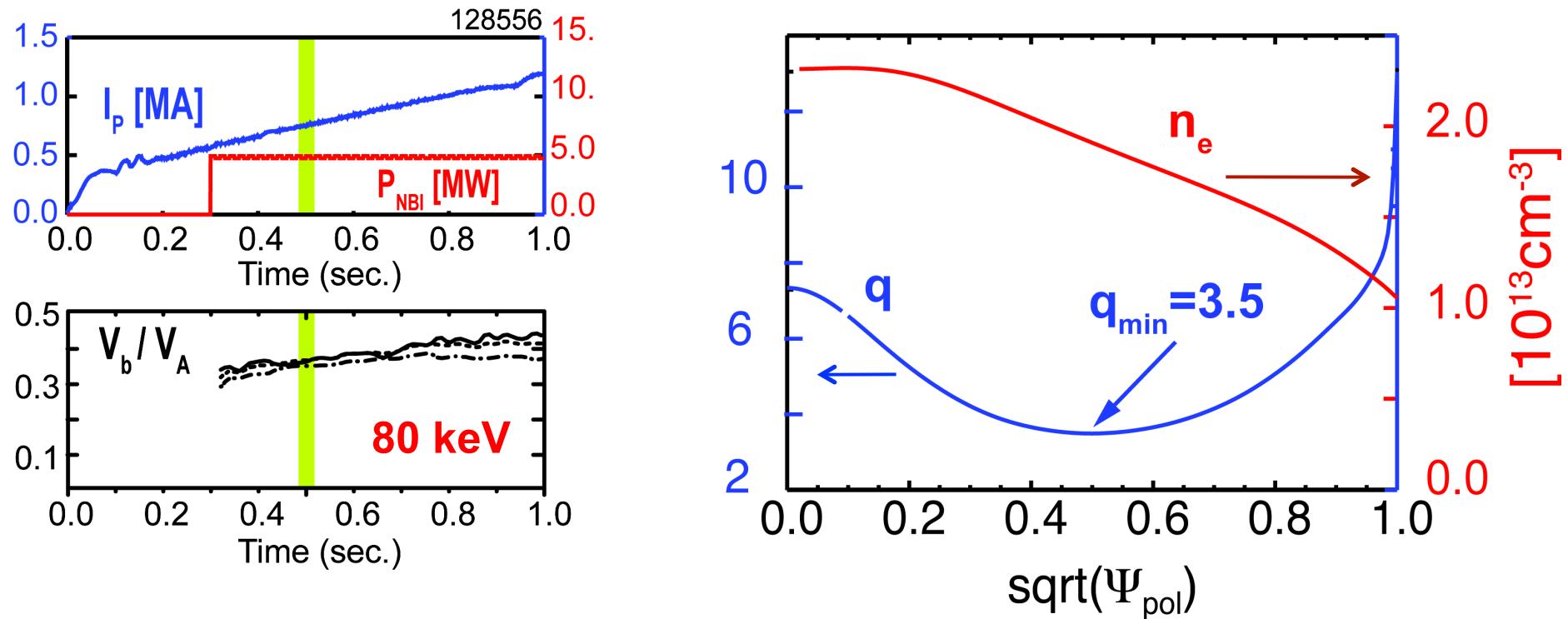


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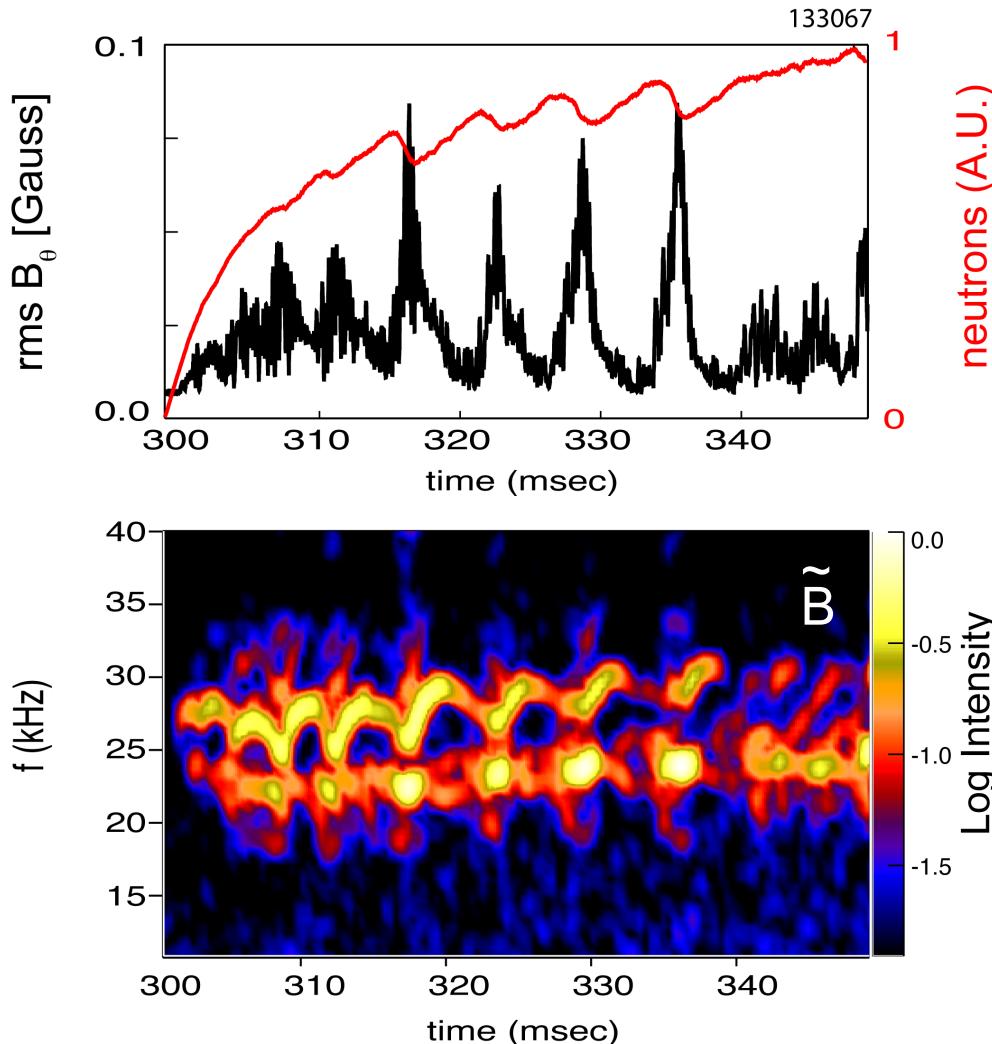


# Recipe for E-GAM Excitation in DIII-D: Counter Tangential Beam Injection with High $q_{\min}$



- 80 keV beam ions,  $\beta_{\text{fast}} \sim \beta_{\text{thermal}} < 1\%$

# Intense Bursting observed with Counter beam injection in DIII-D

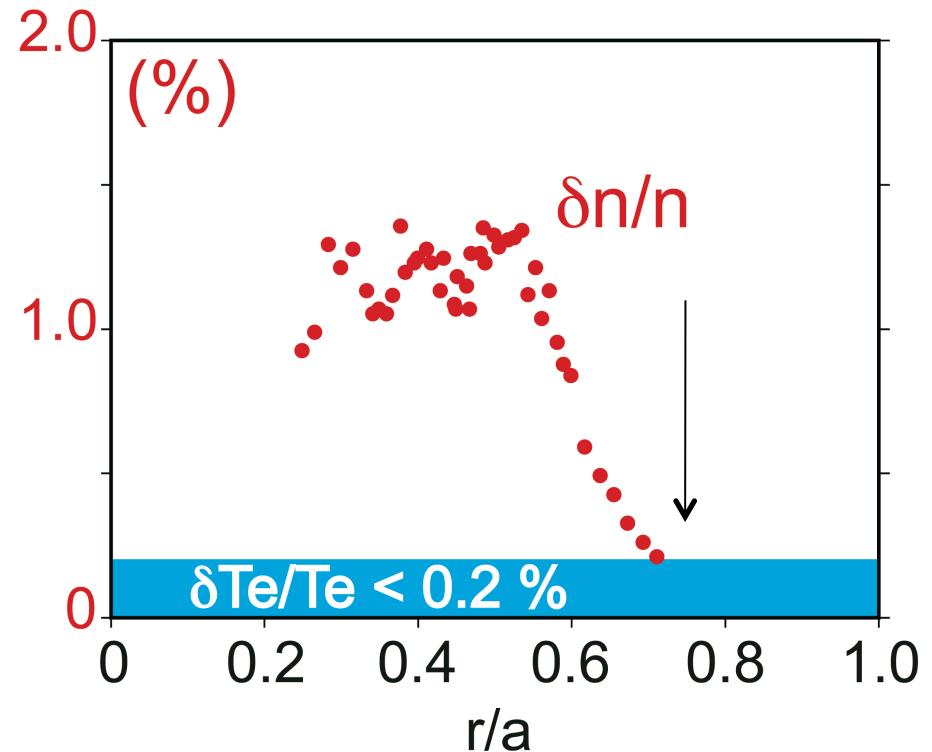
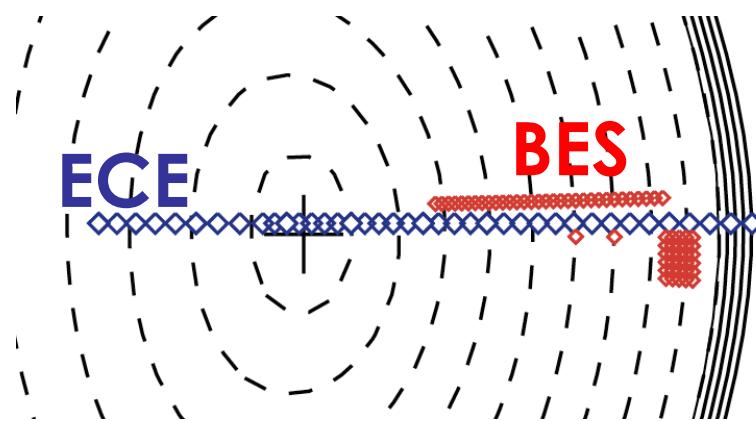


- 10-15 % neutron drops with each mode burst
- Possible evidence for hole/clump formation

(H.L. Berk and B. Breizman)

# Radially Resolved BES Measurements Reveal Global $n=0$ mode, no $T_e$ fluctuations

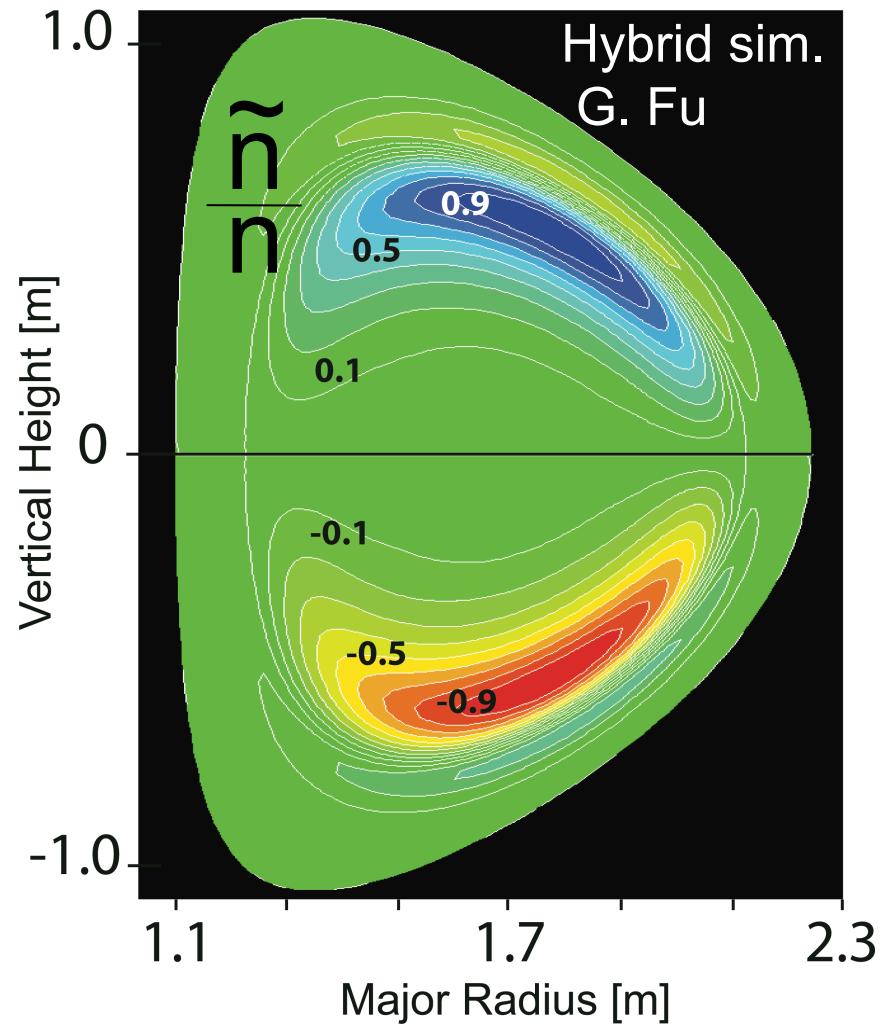
ECE array measures  $\Delta T_e$   
BES array measures  $\Delta n_e$



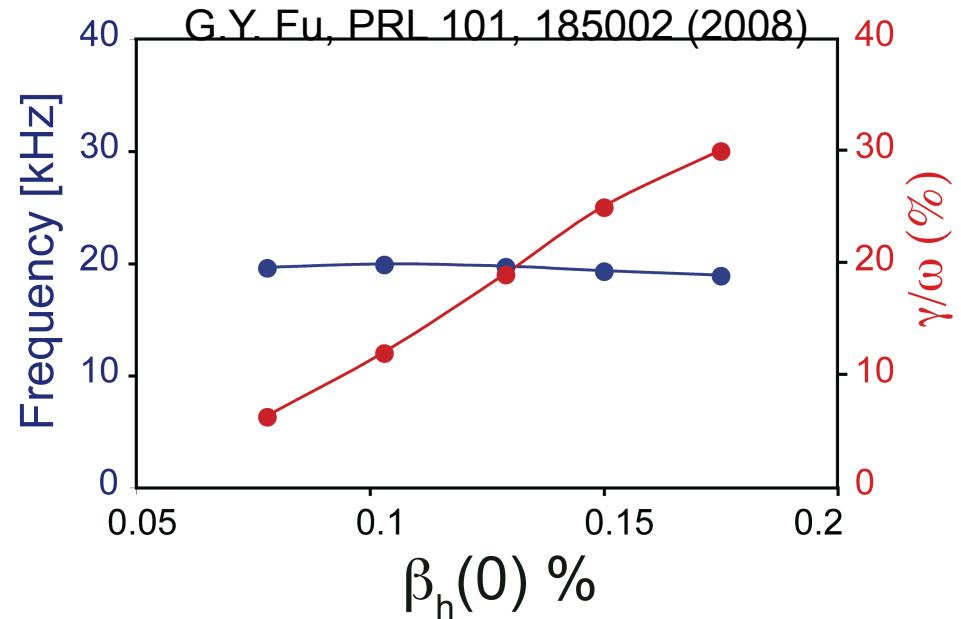
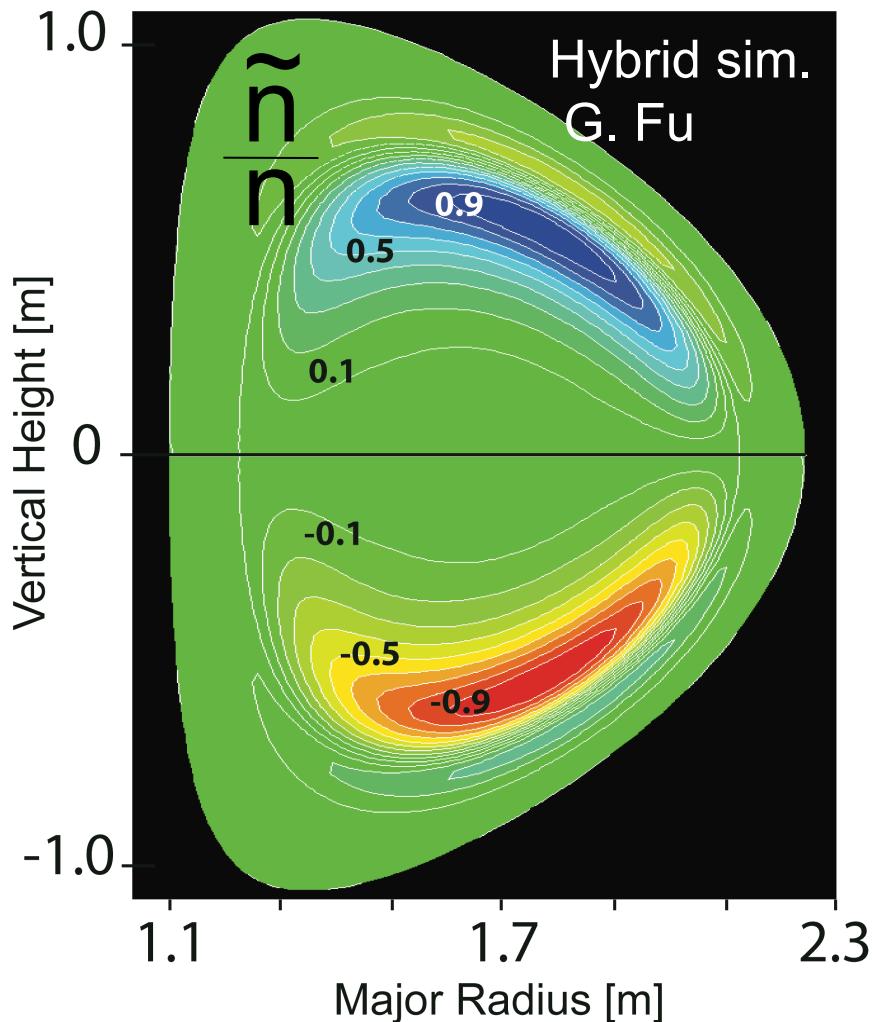
- Peak density mode amplitude near midplane can be as high as 5-8 %
- upper bound on temperature fluctuation set by ECE photon noise

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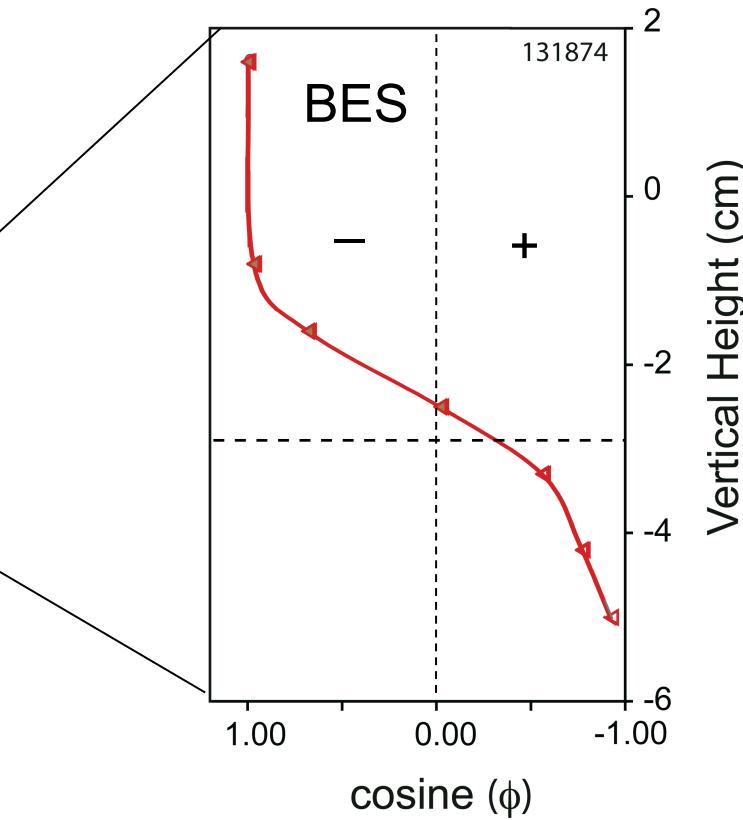
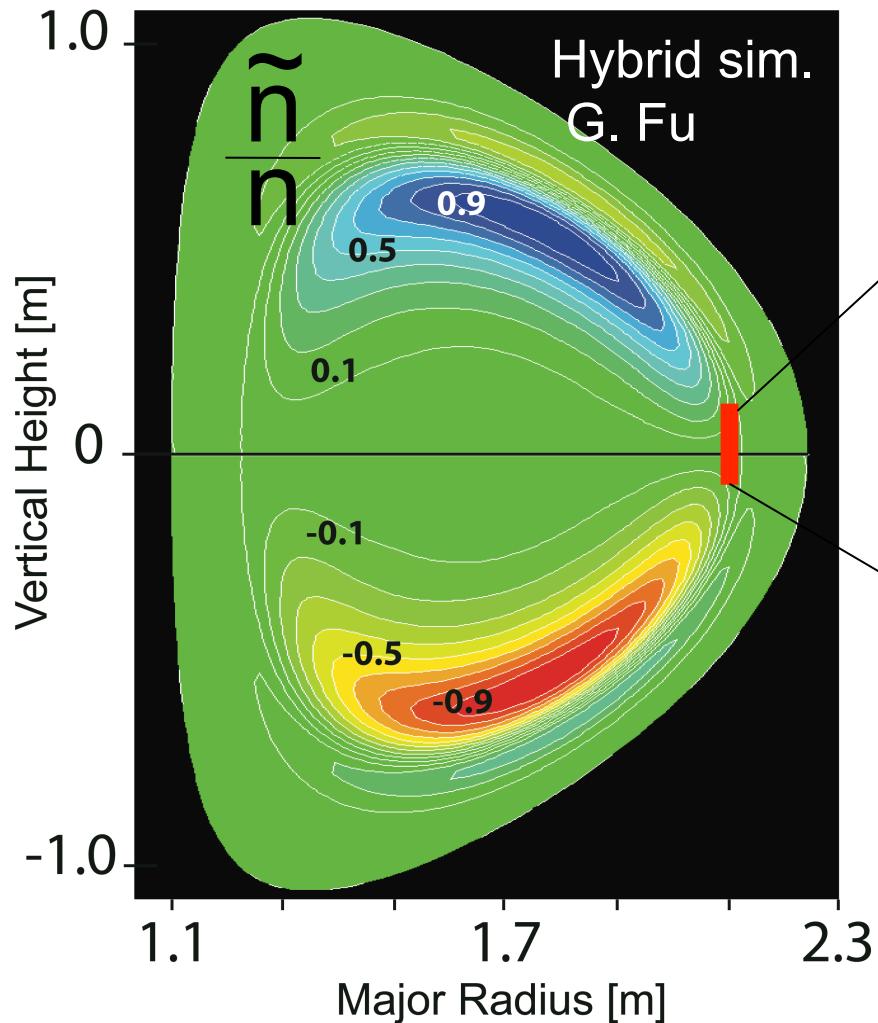


# Theory Predicts Global nonperturbative GAM Driven via Beam Ion Bounce Resonance



- Mode exists for  $\omega_b \sim \omega_{\text{GAM}}$
- pure zonal flow, no  $T_e$  component
- Large linear growth rate (30%) consistent with bursting/chirping

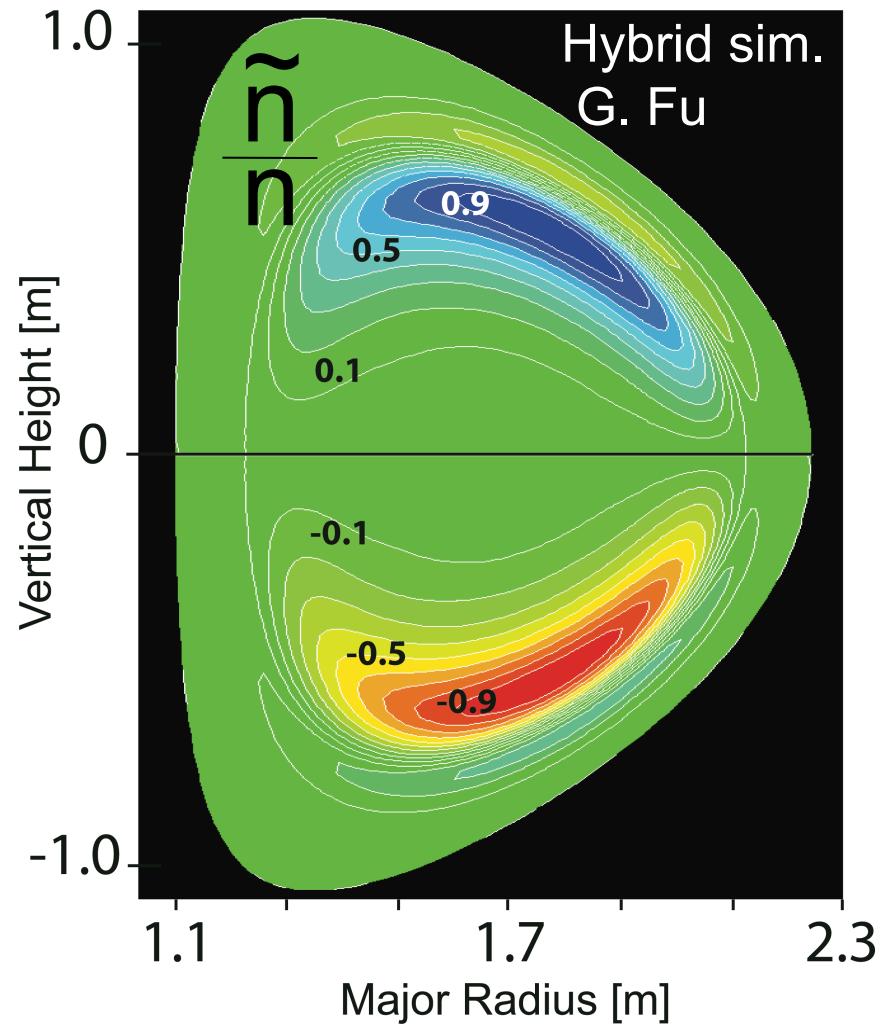
# Up/Down Standing Wave Prediction Confirmed Using Vertical BES Detector Array



- flip of sign observed across midplane, consistent with standing wave pattern

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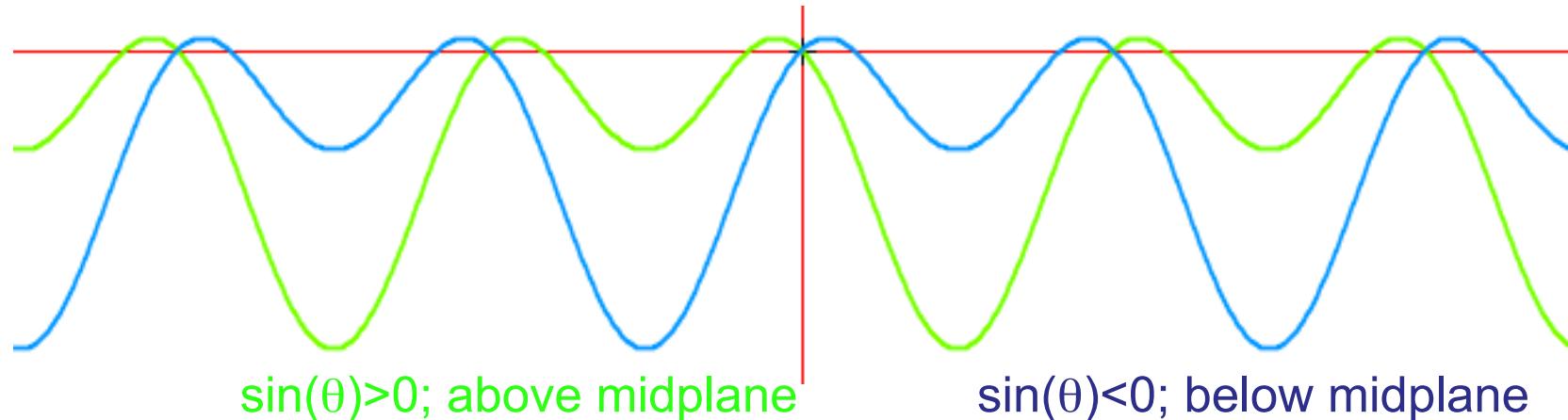


# Nonlinear Perturbed Density Associated with the E-GAM

G. Fu, J. Plasma Phys. 2010

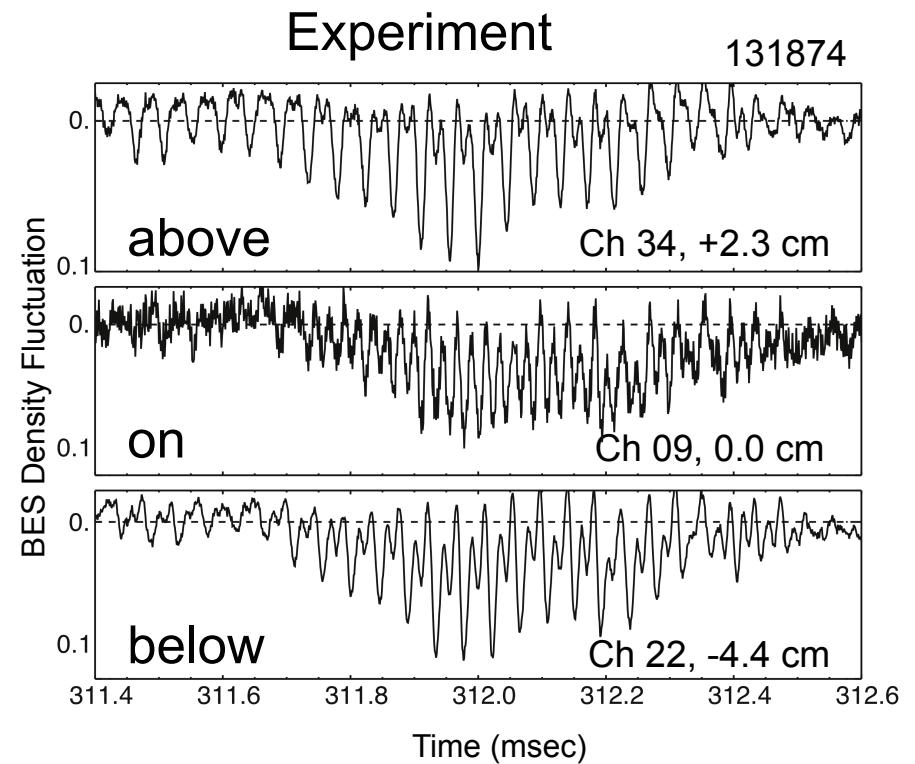
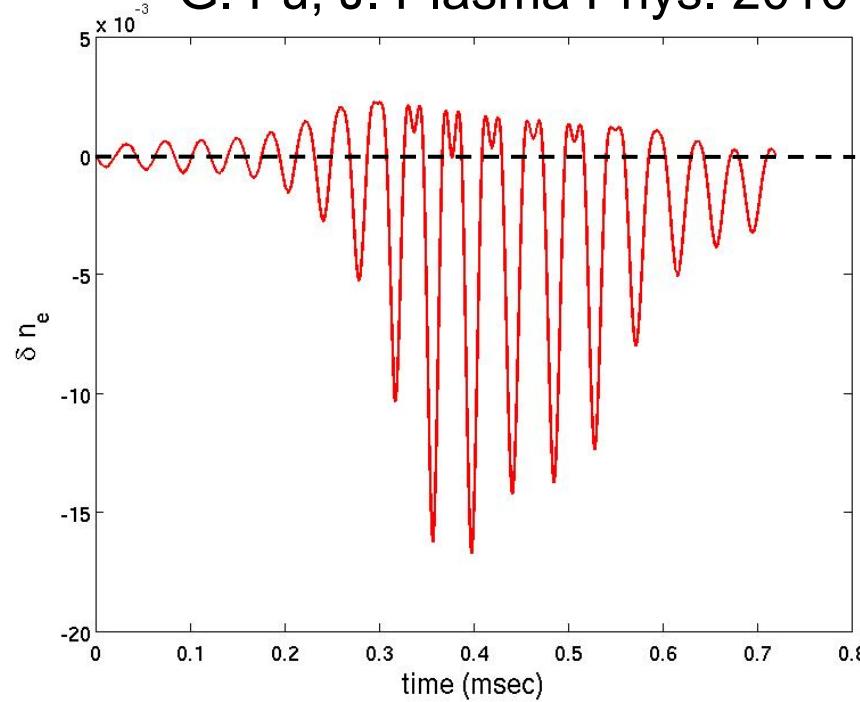
$$\frac{\delta\rho}{\rho} = -\frac{r}{R}[2\hat{E}_r \sin(\theta) \sin(\omega t) + \frac{1}{2}\hat{E}_r^2 \cos(\theta)(1 - \cos(2\omega t))]$$

- Where  $E_r$  is the normalized radial electric field.
- Note that the second term is always negative and the first term can have either sign.



# Hybrid Simulation of E-GAM Burst Consistent with Observation on DIII-D

G. Fu, J. Plasma Phys. 2010



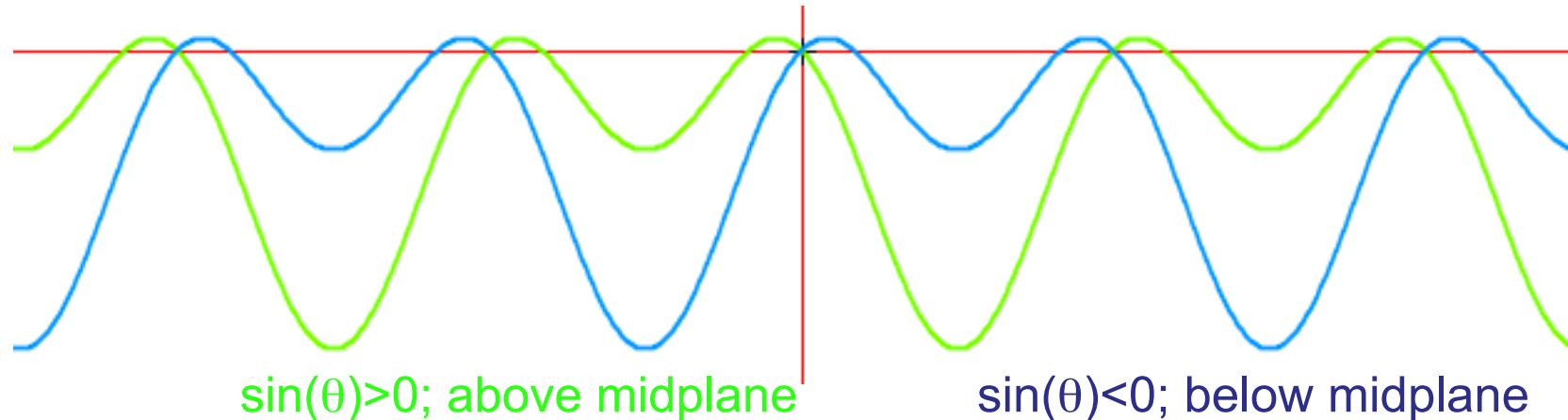
- DC density component is negative on midplane
- Second harmonic peaks on midplane, while fundamental goes through zero

# Nonlinear Perturbed Density Associated with the E-GAM

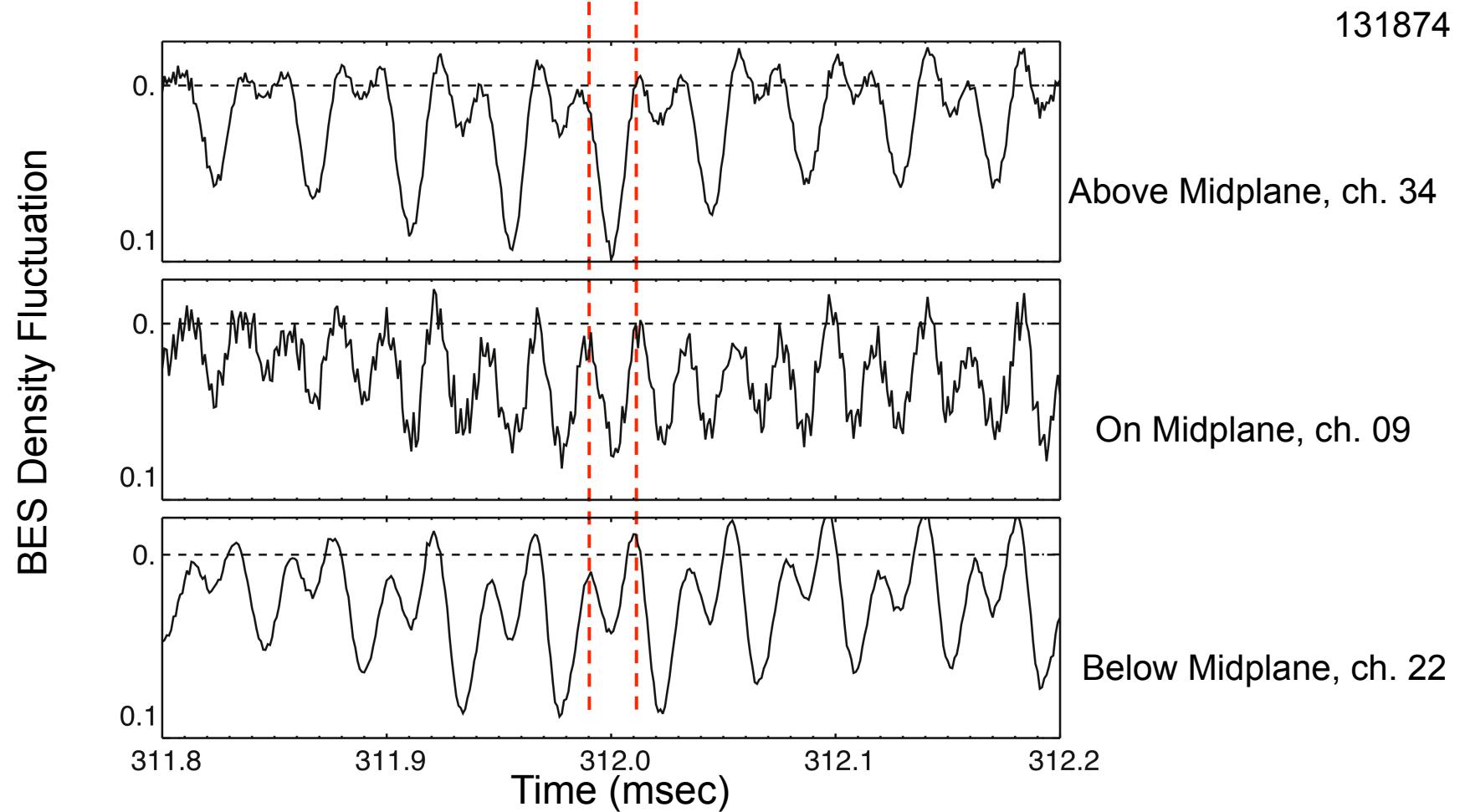
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- Where  $E_r$  is the normalized radial electric field.
- Note that the second term is always negative and the first term can have either sign.



# DC and Second Harmonic Stay in Phase, Fundamental Flips Phase, Across Midplane



- Some third harmonic is also contributing

## Nonlinear Model Predicts Amplitude of Electric Field Fluctuation and peak density fluctuation

$$\frac{\delta\rho}{\rho} = -\frac{r}{R}[2\hat{E}_r \sin(\theta) \sin(\omega t) + \frac{1}{2}\hat{E}_r^2 \cos(\theta)(1 - \cos(2\omega t))]$$

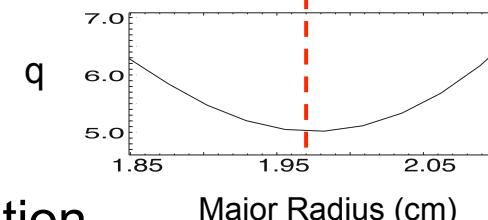
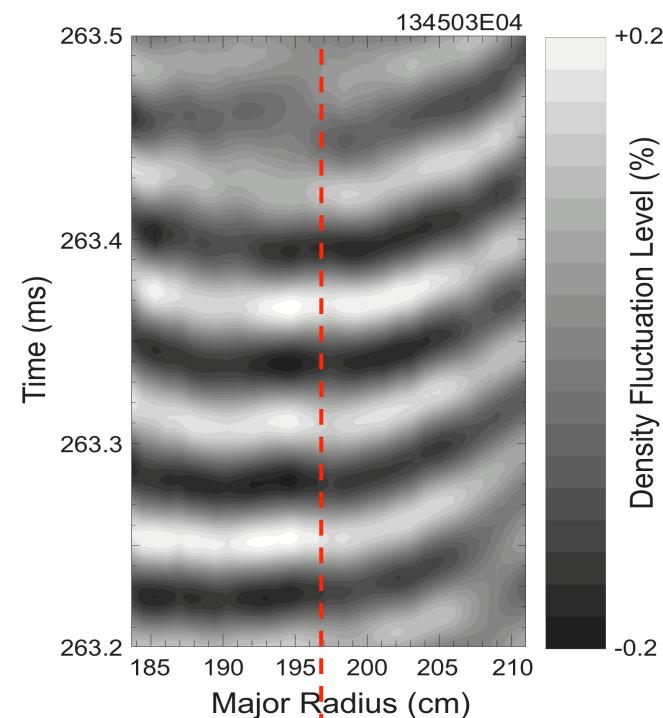
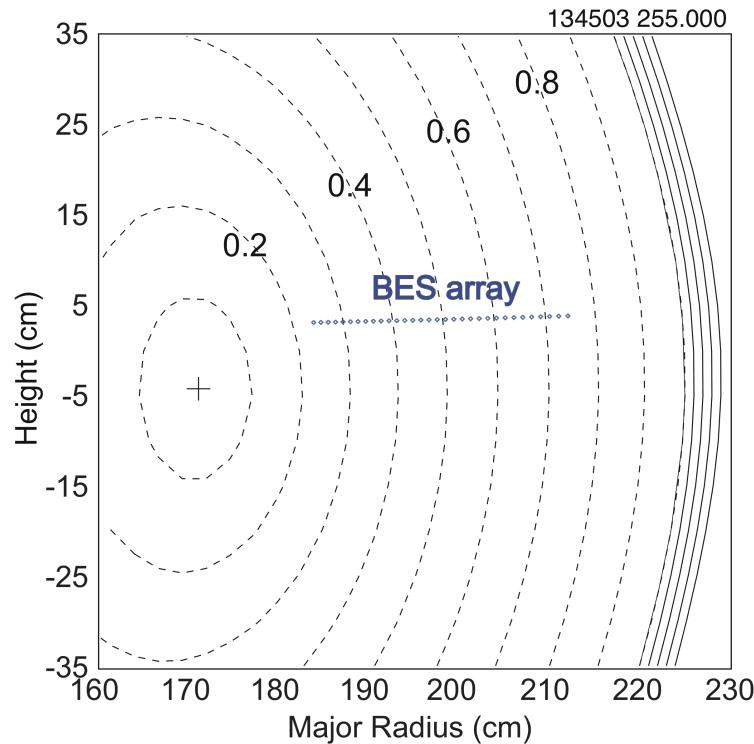
$$\left(\frac{\delta\rho_{2\omega}}{\rho}\right)_{\theta=0} = \frac{r}{2R}\hat{E}_r^2$$

$\hat{E}_r$  : normalized radial electric field

- Next step is to infer  $E_r$
- In principle can compare with BES measured advection of microturbulence



# Outward and Inward Radial Propagation of E-GAM Observed in Reverse Magnetic Shear Plasmas

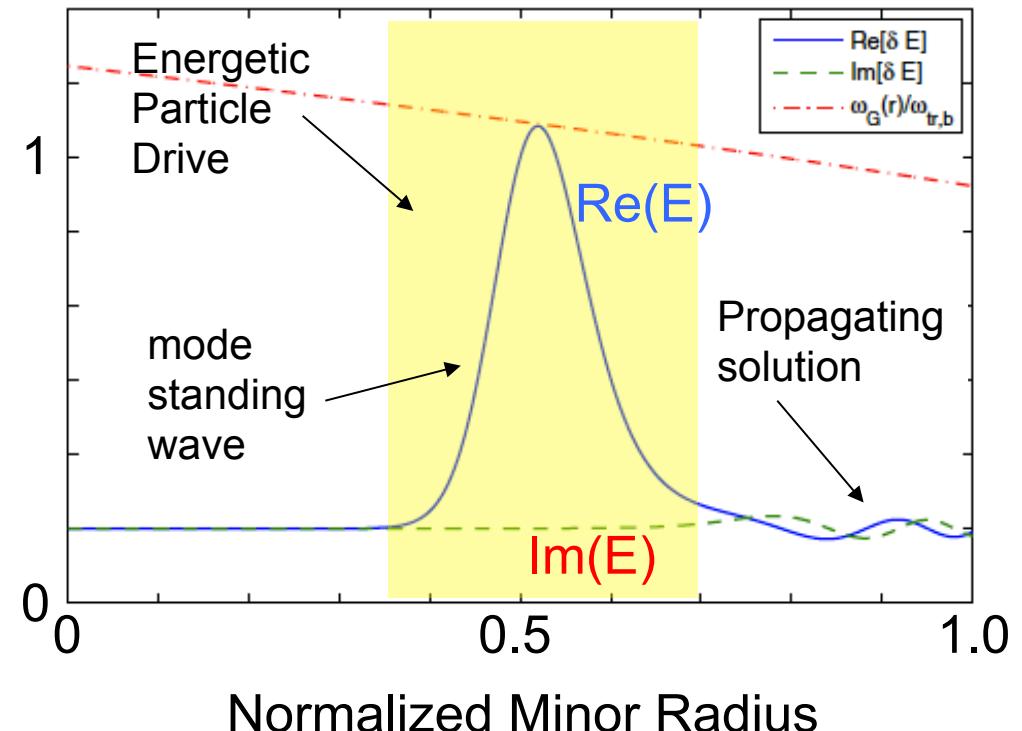


- $q_{\min}$  is not aligned with reversal of propagation

# Outward Radial Propagation Predicted Analytically, Inward Propagation Needs Understanding

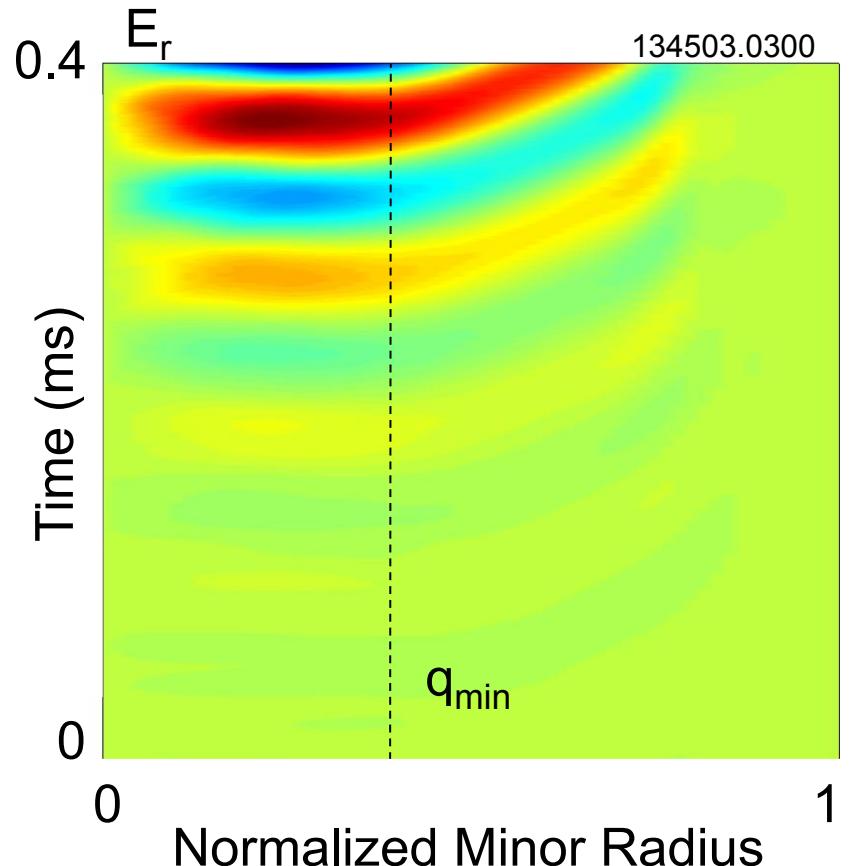
- Theory predicts GAM standing wave in region of energetic particle induced potential well
- Outward propagating solution due to tunneling out of well
- Does reverse magnetic shear induce inward propagation?
- More realistic model required.

Plasma Phys. Control. Fusion **52** (2010) 095003  
Zhiyong Qiu<sup>1,3</sup>, Fulvio Zonca<sup>2,4</sup> and Liu Chen<sup>2,3</sup>



# Recent Electrostatic Hybrid Full-f Simulation Reveals Outward Propagation Consistent with Experiment – G. Fu

- Mode exists at 15 kHz, close to experimental value
- Outward propagation and increasing  $k_r$  with radius consistent with experiment
- No inward propagation seen in simulation
  - note, inward propagation comes late in experimental data
- More realistic simulation required using actual beam deposition profile
  - currently using analytic beam



# Summary

- Key nonlinear predictions on E-GAM structure validated with experiment
  - DC, second harmonic coupling
  - outward radial propagation
- Nonlinear theory and simulation can help infer  $E_r$  from second harmonic amplitude
  - compare to turbulent advection due to  $ExB$
- Outstanding issues:
  - is inward propagation a property of strong negative magnetic shear?
- More realistic analytic and numerical modeling required

