

# **Linear Stability Analysis of an EDA H-mode Edge Plasma: A Quest for the Quasi-Coherent Mode**

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acknowledgement: B. LaBombard (MIT)

*presented at the TTF Meeting, Apr. 6 - 9, 2011, San Diego*

*work supported by DOE grant DE-FG02-07ER84718*

# Introduction

- Enhanced D-Alpha (EDA) H-modes in Alcator C-Mod are of interest
  - good energy confinement
  - quasi-steady ELM-free operation
  - see: Greenwald, et al., Phys. Plasmas **6**, 1943 (1999).  
Terry, et al., Nucl. Fusion **45**, 1321 (2005).
- EDA thought to be enabled by the quasi-coherent mode (QCM)
  - QCM is an edge oscillation with  $k_{\theta} \sim 1 - 2 \text{ cm}^{-1}$  and  $f \sim \text{few } 100\text{'s kHz}$
  - may regulate the pedestal gradient and particle transport
- key question: is the QCM related to a linear unstable mode
  - weak instability  $\sim$  weak nonlinearity  $\Rightarrow$  quasi-coherent oscillation (?)

**this poster: use the edge eigenvalue code 2DX to  
conduct a systematic search for candidate linear modes**

## The 2DX code:

- solves linearized eigenvalue equations in the R-Z plane for each toroidal  $n$ 
  - discretize using finite difference  $\Rightarrow$  sparse matrix
  - solve using an existing eigenvalue package SLEPc
    - Krylov-Schur algorithm
    - Cayley spectral shift often employed
  - typically have 10's to 100's of grid-points per dimension
  - run times are 10's of seconds to a few hours on a single processor
- uses realistic X-point/divertor geometry (edge + SOL)
  - similar capabilities to BOUT and BOUT++
- has a specialized equation parser  $\Rightarrow$  easy to change physics model
  - present study uses a variety of fluid-based physics models
- has been benchmarked against analytical theory and BOUT
  
- more 2DX info: Baver et al., Lodestar Report #LRC-10-137  
[www.lodestar.com/LRCreports](http://www.lodestar.com/LRCreports)
- this study: use C-Mod geometry with EDA experimental plasma profiles

## Physics models explored here

- RMHD = reduced resistive MHD
- RB = add e-inertia
- (RB-ES = add e-inertia but electrostatic limit  $\delta_e \rightarrow \infty$ )
- RBi = add  $\omega_{*i}$  = ion FLR
- RBiE = add  $E_r$  shear
- RBiEK = add KH = Kelvin-Helmholtz drive
- RDBiEKM = add EM DW

### Instability mechanisms included:

- curvature-driven resistive and ideal ballooning
- gradient-driven collisional and inertial drift waves
- perpendicular flow-driven Kelvin-Helmholtz

### Suppression mechanisms included:

- ion diamagnetic current (FLR)
- $E_r$  shear

### Instabilities not included:

- parallel KH  
[Rogister NF 2004]
- current-driven peeling  
[see poster P25]

## Equation set (optional poster)

- 3-field model for vorticity (electrostatic potential), density, and parallel vector potential (parallel current)

$$\gamma \left( \overbrace{\nabla_{\perp}^2 \delta\Phi + \frac{1}{n} \nabla_{\perp}^2 T_i \delta n}^{\text{ion FLR}} \right) = \overbrace{-\delta \mathbf{v}_E \cdot \nabla \varpi - \mathbf{v}_E \cdot \nabla \left( \nabla_{\perp}^2 \delta\Phi + \frac{1}{n} \nabla_{\perp}^2 T_i \delta n \right)}^{\text{KH}} + \overbrace{\frac{2B}{n} C_r (T_i + T_e) \delta n + \frac{B^2}{n} \partial_{\parallel} \delta J + \mu_{ii} \nabla_{\perp}^4 \delta\Phi}^{\text{E}_r \text{ shear}}$$

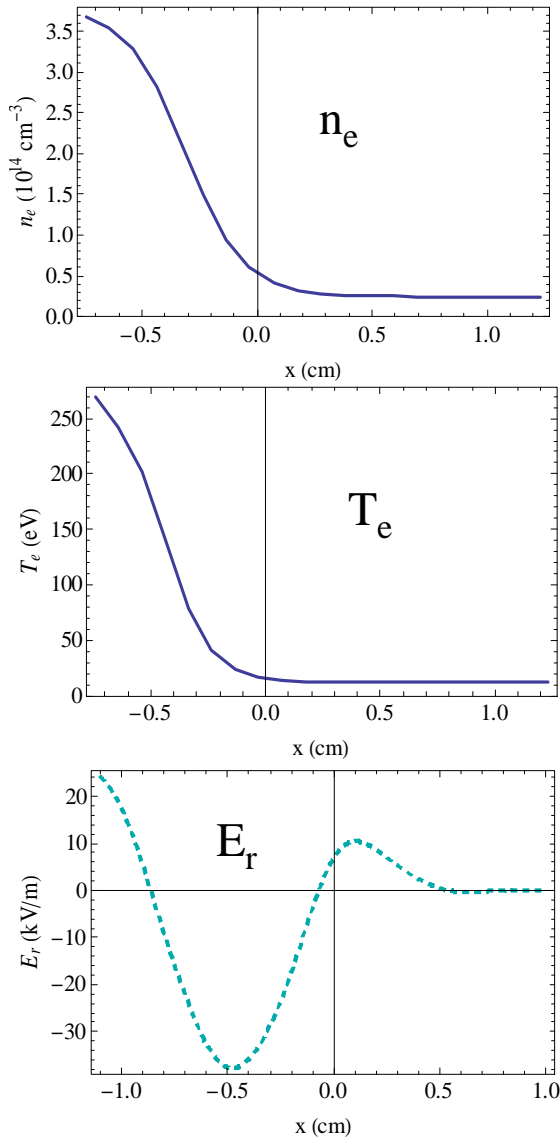
$$\gamma \delta n = \overbrace{-\mathbf{v}_E \cdot \nabla \delta n}^{\text{E}_r \text{ shear}} - \delta \mathbf{v}_E \cdot \nabla n + \overbrace{\partial_{\parallel} \delta J}^{\text{DW-ES}}$$

$$\gamma \left( \frac{n}{\delta_{er}^2} - \nabla_{\perp}^2 \right) \delta A = \overbrace{-\mathbf{v}_E \cdot \nabla \left( \frac{n}{\delta_{er}^2} - \nabla_{\perp}^2 \right) \delta A}^{\text{E}_r \text{ shear, e-inertia}} + v_e \nabla_{\perp}^2 \delta A - \mu n \nabla_{\parallel} \delta\Phi + \overbrace{\mu T_e \nabla_{\parallel} \delta n}^{\text{DW-ES}} + \overbrace{T_e \mu \delta \mathbf{b} \cdot \nabla n + 1.71 n \mu \delta \mathbf{b} \cdot \nabla T_e}^{\text{DW-EM}}$$

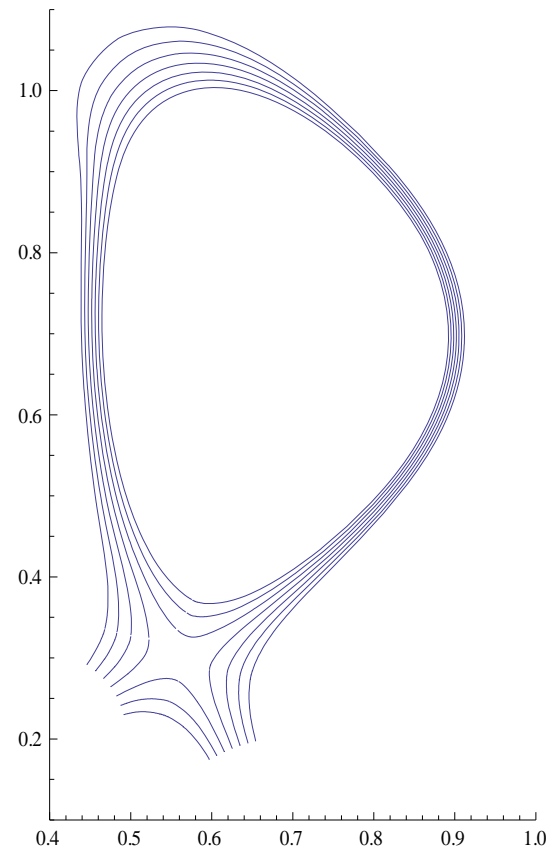
where

$$\delta J = -\nabla_{\perp}^2 \delta A \quad \varpi = \nabla_{\perp}^2 \Phi + \overbrace{\frac{1}{n} \nabla_{\perp}^2 P_i}^{\text{ion FLR}} \quad \delta \mathbf{b} \cdot \nabla Q = i \frac{k_b (\partial_r Q)}{\mu \delta_{er}^2 B} \delta A$$

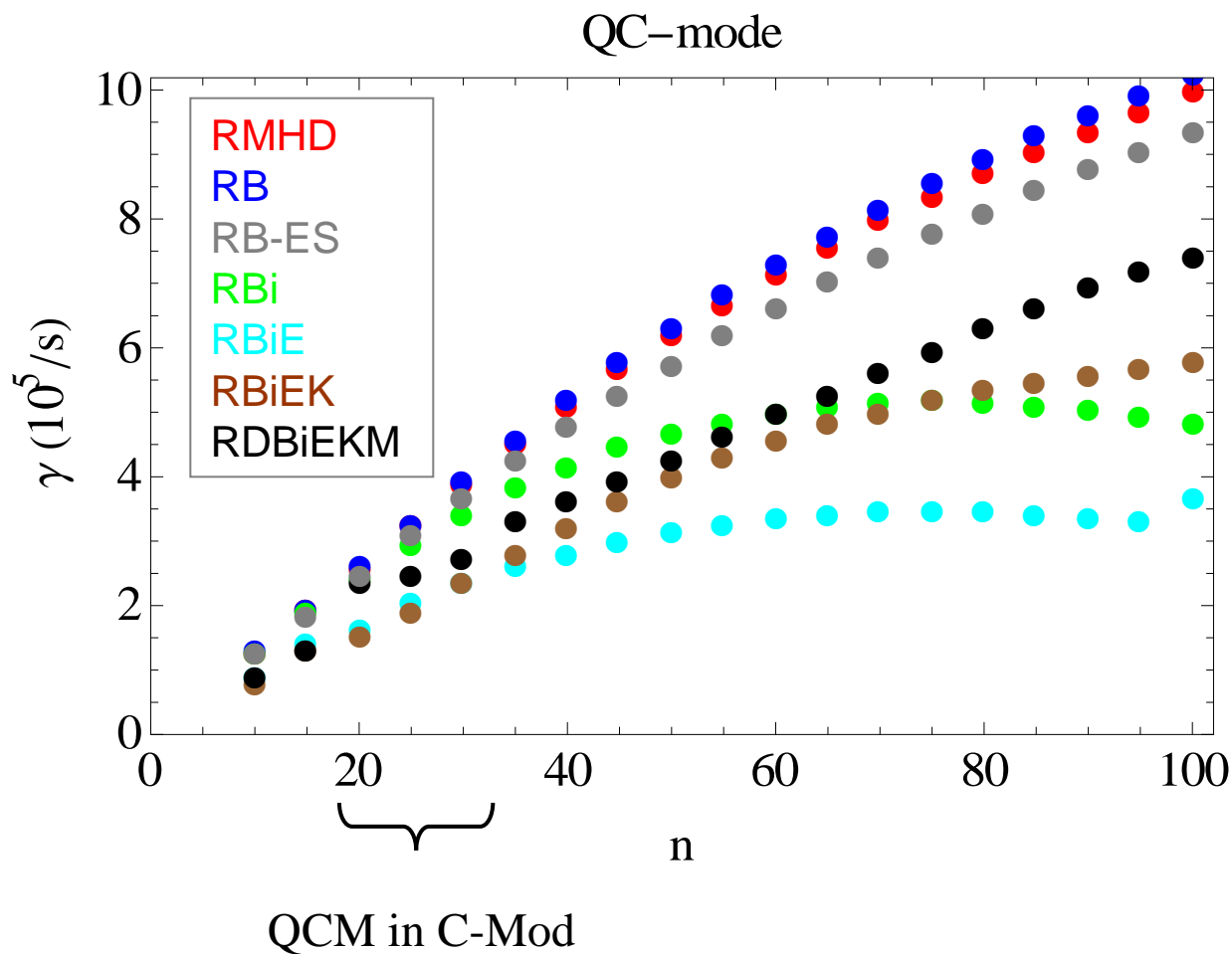
## Input profiles and geometry



- typical C-Mod EDA discharge conditions
- $E_r$  fit to McDermott et al. PoP 2009

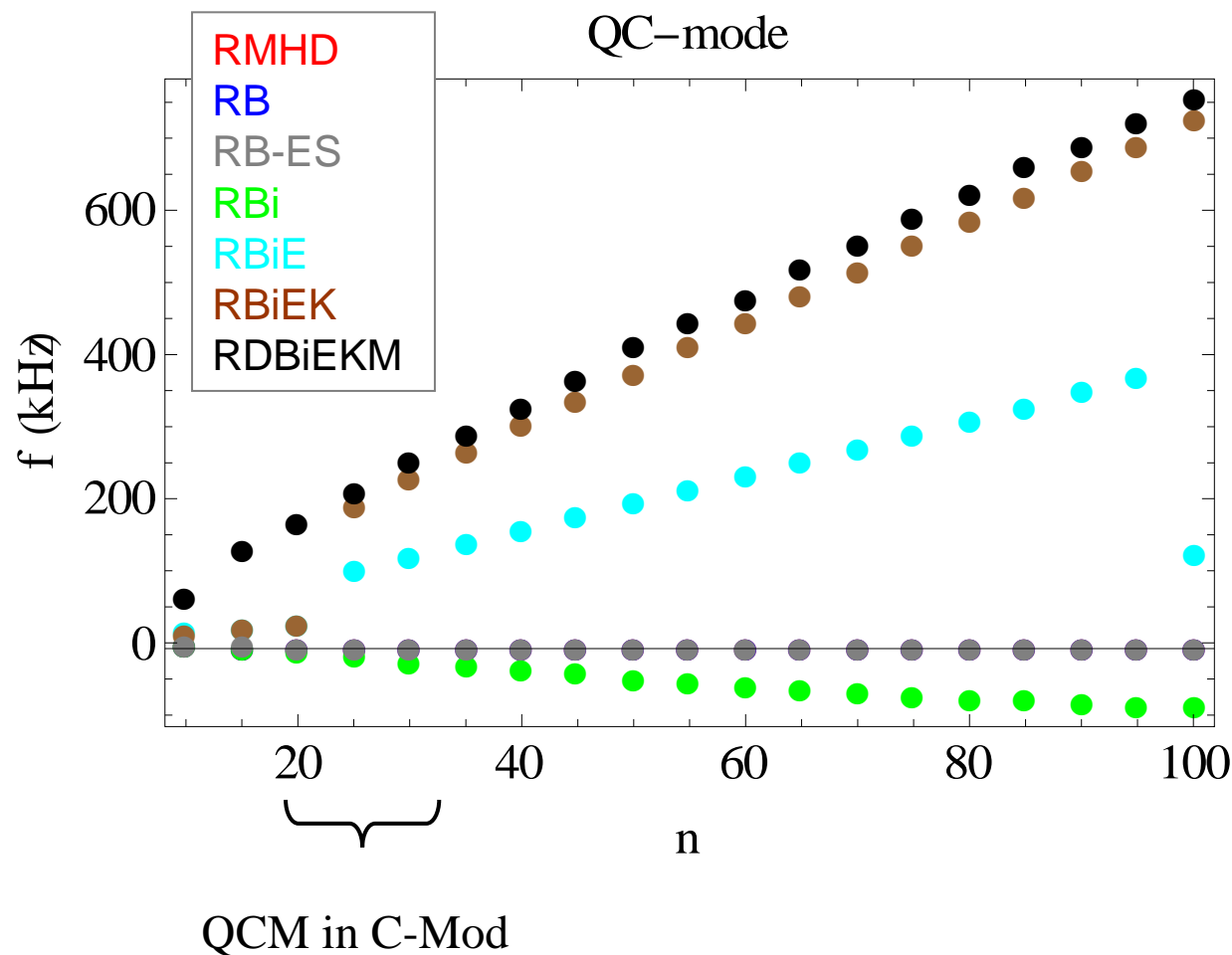


## Growth rate spectra show some insensitivity to the model



- RB models show expected increase of  $\gamma$  with  $n$
- ion FLR reduces growth at larger  $n$
- spectral peak sensitive to  $T_i$ 
  - see p. 10
- $E_r$  shear further reduces  $\gamma$
- KH not very significant
- DW restores nearly linear growth with  $n$

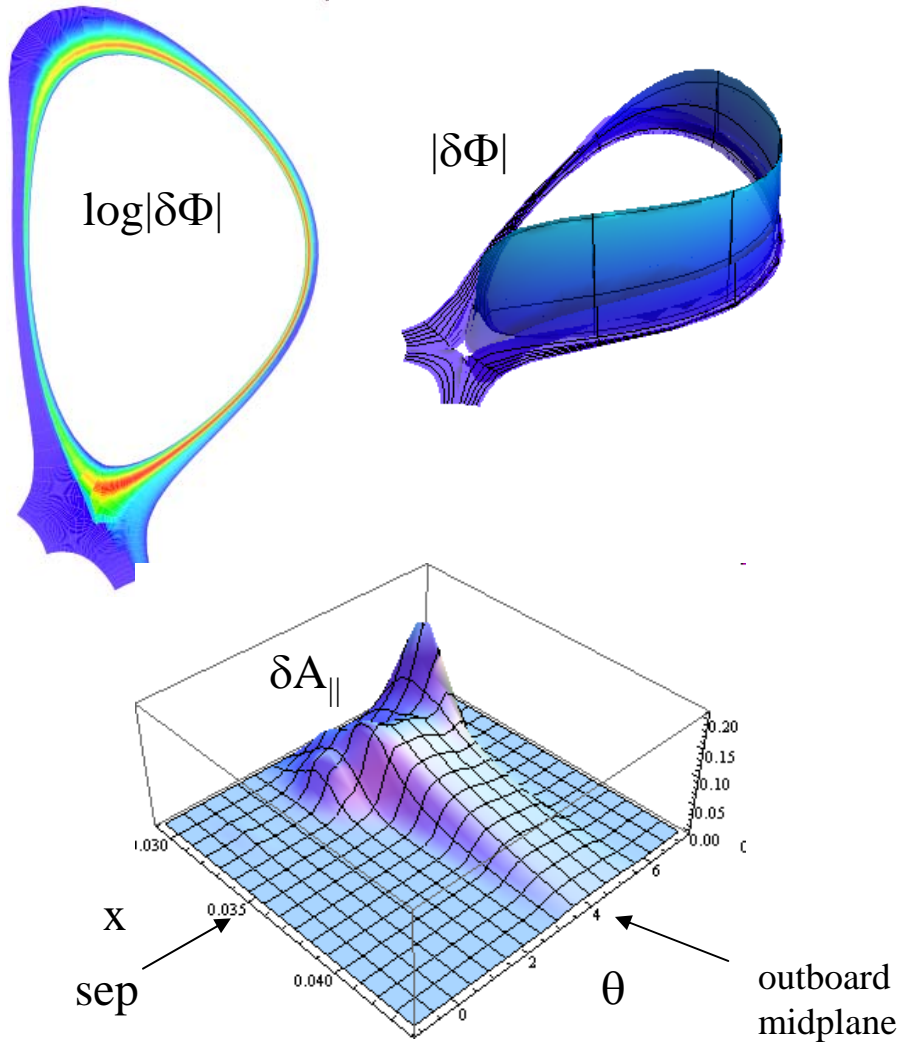
## Frequency spectra are dominated by Doppler shifts



- RB models show small  $f$  as expected
- ion FLR  $\Rightarrow f < 0$  (ion direction)
- $E_r \Rightarrow$  Doppler shift to electron direction
- DW  $f$  increases linearly with  $n$
- freqs are comparable to C-Mod (almost trivial due to Doppler)



# Typical eigenmodes are localized to outboard edge and give rise to $\delta B$

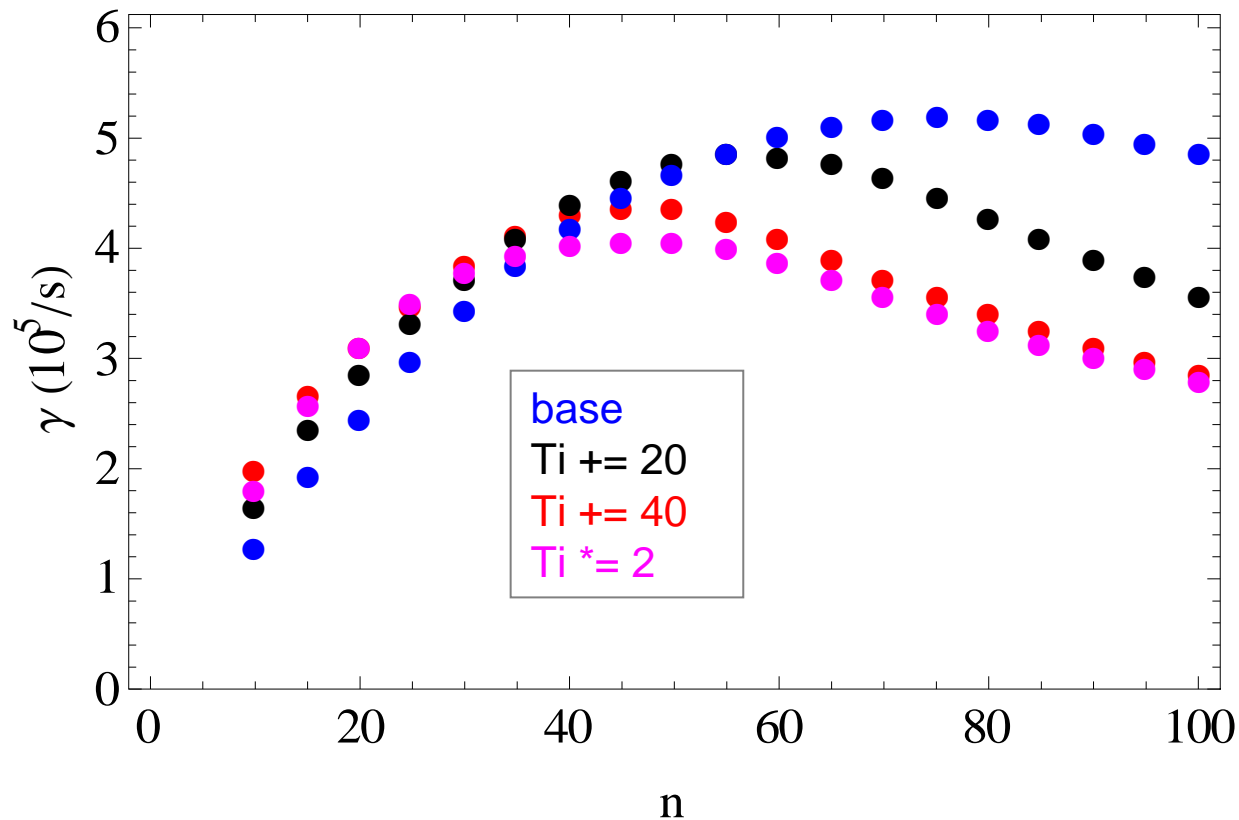


- mode structure qualitatively as observed in C-Mod
- modes (in both EM & ES models) have  $\delta J_{||}$  and hence generate fluctuating  $\delta B$  like C-Mod observations

## Best linear candidate is RBi mode

- Study  $T_i$  sensitivity for the RBi model
  - Resistive ballooning with ion diamagnetic drift

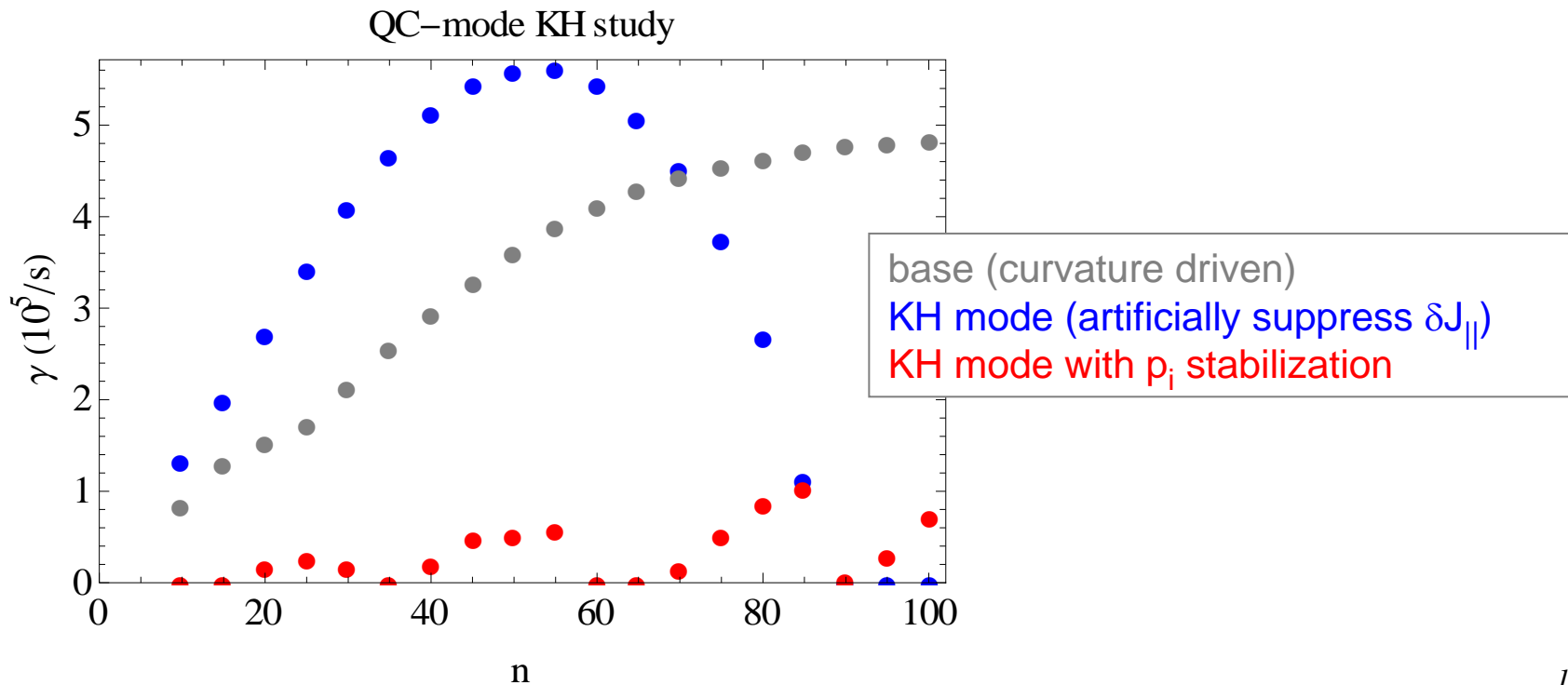
QC-mode RBi



- increasing  $T_i$  increases FLR stabilization of the high- $n$  modes  $\Rightarrow \gamma$  peak shifts to lower  $n$
- peak is roughly in the range of C-Mod observations; but, DW terms destroy the peak

## KH drive is mitigated by Alfvén physics and ion diamagnetism

- similar to [Rogers and Dorland, PoP 2005], we find that since  $\omega_a = v_a/qR \sim \omega_E$  shearing rate, the KH mode is stabilized
  - but here  $\omega_a$  arises from geometry, not specifically magnetic shear
- artificially suppressing the  $\delta J_{\parallel}$  Alfvén physics gives a robust KH mode which is stabilized by  $p_i$  (ion diamagnetism), consistent with RD-2005.



## Summary

- the unstable spectrum is not very sensitive to the physics model
- instability drives are curvature (dominant), drift (high  $n$ ), KH (unimportant)
- there are no unambiguous candidates for the QCM in the models investigated, but
- resistive-ballooning model with ion diamagnetic drifts gives peak growth rates at a wavenumber close to observations
  - perhaps higher- $n$  drift waves saturate at a low level
- present results tend to suggest a role for nonlinear effects such as the inverse cascade
  - e.g. DW modes cascade into RBi mode
  - see nonlinear reduced model by D.A. Russell et al, Sat. am, Edge-VI oral